

### Andrzej J. Buras (Technical University Munich)

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# CKM Matrix and the Unitarity Triangle

Kobayashi-Maskawa Picture of CP Violation

CP Violation arises from a single phase δ in W<sup>±</sup> interactions of Quarks



Four Parameters:  $(\theta_{12} \approx \theta_{cabibbo})$  $s_{12} = |V_{us}|, \quad s_{13} = |V_{ub}|, \quad s_{23} = |V_{cb}|, \quad \delta$ 

 $c_{ij} \equiv \cos \theta_{ij}$ ;  $s_{ij} \equiv \sin \theta_{ij}$ ;  $c_{13} \cong c_{23} \cong 1$ 



(AJB, Lautenbacher, Ostermaier, 94)

$$R_{b} \equiv \sqrt{\overline{\rho}^{2} + \overline{\eta}^{2}} = \left(1 - \frac{\lambda^{2}}{2}\right) \frac{1}{\lambda} \left| \frac{V_{ub}}{V_{cb}} \right| \qquad \frac{\text{Circle}}{(\overline{\rho}, \overline{\eta})} = (0,0)$$
$$R_{t} \equiv \sqrt{(1 - \overline{\rho})^{2} + \overline{\eta}^{2}} = \frac{1}{\lambda} \left| \frac{V_{td}}{V_{cb}} \right| \qquad \frac{\text{Circle}}{(\overline{\rho}, \overline{\eta})} = (1,0)$$

Particular Definition of  $\lambda$ , A,  $\rho$ ,  $\eta$ 

$$s_{12} \equiv \lambda$$
  

$$s_{23} \equiv \mathbf{A} \ \lambda^2$$
  

$$s_{13} e^{i\delta} \equiv \mathbf{A} \ \lambda^3 (\rho - i\eta)$$

BLO: Phys.Rev. (94); (Schmidtler, Schubert) At  $O(\lambda^5)$  equivalent to (Branco, Lavoura, 88)

Basic Virtues of this Definition:

$$\begin{aligned} V_{us} &= \lambda + 0 \left( \lambda^7 \right) \\ V_{ub} &= A \lambda^3 \left( \rho - i \eta \right) \\ V_{cb} &= A \lambda^2 + 0 \left( \lambda^8 \right) \\ V_{td} &= A \lambda^3 \left( 1 - \overline{\rho} - i \overline{\eta} \right) \end{aligned}$$
  
The apex of UT given by  $\left( \overline{\rho}, \overline{\eta} \right)$  (BLO)

### Unitarity Triangle



An Important Target of Particle Physics

$$J_{CP} = \lambda^{2} \left| V_{cb} \right|^{2} \overline{\eta} = 2 \cdot \bigtriangleup$$

Area of unrescaled UT

#### **Information from Tree Level Decays**



## Results on $|V_{ub}|$ and $|V_{cb}|$

Parameter	Value	Gaussian	Uniform
		σ	half-width
$ V_{us} $	0.221	0.002	-
$ V_{cb} $ (excl.)	42.1 · 10 <sup>-3</sup>	$2.1 \cdot 10^{-3}$	-
$ V_{cb} $ (incl.)	40.4 · 10 <sup>-3</sup> (Artuso Barberio)	$0.7 \cdot 10^{-3}$	0.8 · 10 <sup>-3</sup>
$ V_{ub} $ (excl.)	32.5 · 10 <sup>-4</sup>	$2.9 \cdot 10^{-4}$	$5.5 \cdot 10^{-4}$
$ V_{ub} $ (incl.)	40.9 · 10-4	$4.6 \cdot 10^{-4}$	3.6 · 10-4

$ V_{cb} $ (incl.) $\bigstar 41.7 \cdot 10^{-3}$ (CKM)	0.7 · 10-3	0.8 · 10 <sup>-3</sup>
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 $R_b$  = Independent of New Physics  $R_t$ ,  $\beta$ ,  $\gamma$  = Can be affected by New Physics



## Hunting $\Delta$ with Rare and CP Decays

### <u>2011:</u>





**Quark Mixing and CP Violation closely related in the St. Model** 







# Theoretical Framework

#### The Problem of Strong Interactions





 $\left\langle \overline{\mathrm{K}}^{0} \middle| \left( \overline{\mathrm{s}} \mathrm{d} \right)_{\mathrm{V}-\mathrm{A}} \left( \overline{\mathrm{s}} \mathrm{d} \right)_{\mathrm{V}-\mathrm{A}} \middle| \mathrm{K}^{0} \right\rangle = \frac{8}{3} \mathbf{\hat{B}}_{\mathrm{K}} F_{\mathrm{K}}^{2} m_{\mathrm{K}}^{2} \left[ \alpha_{\mathrm{s}}(\mu) \right]^{2/9}$ 



Possible Dirac Structures in 
$$K^0 - \overline{K}^0$$
 and  $B^0_{d,s} - \overline{B}^0_{d,s}$ 

**SM:** 
$$\gamma_{\mu} \left(1 - \gamma_{5}\right) \otimes \gamma^{\mu} \left(1 - \gamma_{5}\right)$$

**Beyond SM:** 

$$\begin{array}{l} \gamma_{\mu}\left(1-\gamma_{5}\right)\,\otimes\,\gamma^{\mu}\left(1+\gamma_{5}\right)\\ \left(1-\gamma_{5}\right)\,\otimes\,\left(1+\gamma_{5}\right)\\ \left(1-\gamma_{5}\right)\,\otimes\,\left(1-\gamma_{5}\right)\\ \sigma_{\mu\nu}\left(1-\gamma_{5}\right)\,\otimes\,\sigma^{\mu\nu}\left(1-\gamma_{5}\right) \end{array}$$

MSSM with large tanβ General Supersymmetric Models Models with complicated Higgs System

NLO 
$$\left[\eta_{QCD}^{i}\right]^{New}$$
: Ciuchini, Franco, Lubicz,  
Martinelli, Scimemi, Silvestrini  
AJB, Misiak, Urban, Jäger

## **General Structure in Models** with Minimal Flavour Violation

Ciuchini, Degrassi, Gambino, Giudice; AJB, Gambino, Gorbahn, Jäger, Silvestrini;



**No new Operators** (Dirac and Colour Structures) beyond those present in the SM



**Flavour Changing Transitions governed by** CKM. No new complex phases beyond those present in the SM

$$A(Decay) = B_i \eta^i_{QCD} V^i_{CKM} \left[ F^i_{SM} + F^i_{New} \right]$$
  
real

Examples: SM MSSM at not too large  $tan\beta =$ 

## **Universal Unitarity Triangle**

AJB, Gambino, Gorbahn, Jäger, Silvestrini (00)



**Examples** 

$$R_{t} = 0.94 \sqrt{\frac{\Delta M_{d}}{0.487/\text{ps}}} \sqrt{\frac{15.0/\text{ps}}{\Delta M_{s}}} \left[\frac{\xi}{1.15}\right]$$

$$a_{\psi K_s} = \sin 2\beta$$



# Standard Analysis of Unitarity Triangle





$$R_{t} = 0.94 \sqrt{\frac{\Delta M_{d}}{0.487/\text{ ps}}} \sqrt{\frac{15.0/\text{ ps}}{\Delta M_{s}}} \left[\frac{\xi}{1.15}\right]$$

 $\Delta M_s > 14.9 / ps$  LEP (SLD)



$$A_{\rm CP}(\psi K_{\rm S}) \equiv -a_{\psi K_{\rm S}}\sin(\Delta M_{\rm d}t)$$

$$a_{\psi K_S} = \sin 2\beta$$
 (SM)



## **Different Treatments of Errors**

Particle Data Group

Gilman, Kleinknecht, Renk

"Gaussian" Approach

Ali + London; Mele, ...

**Bayesian Approach** 

Ciuchini, D'Agostini, Franco, Lubicz, Martinelli, Parodi, Roudeau, Stocchi

Frequentist Approach

Höcker, Lacker, Laplace, Diberder

95% CL Scan Method

Plaszczynski, Shune; BaBar



### Basic Result from Working Group III (CKM Workshop, CERN, Feb. 2002)

AJB, H. Lacker, F. Parodi, A. Stocchi First report: CERN Courier, May 2002 (R. Forty)

The main difference between Bayesian and Frequentists approaches results from the different treatments of errors in the input parameters

Bayesian

<u>Convolution</u> of statistical and systematic (TH) errors

Frequentist :

: <u>Linear addition</u> of statistical and systematic (TH) errors

If the two fitting programs are fed with the same input likelihoods the allowed  $(\overline{\rho}, \overline{\eta})$  regions are very similar

## Input for the Unitarity Triangle

Parameter	Value	Gaussian	Uniform
		σ	half-width
$ V_{us} $	0.221	0.002	-
$ V_{cb} $ (excl.)	$42.1 \cdot 10^{-3}$	$2.1 \cdot 10^{-3}$	-
$ V_{cb} $ (incl.)	40.4 · 10 <sup>-3</sup> (Artuso Barberio)	$0.7 \cdot 10^{-3}$	$0.8 \cdot 10^{-3}$
$ V_{ub} $ (excl.)	32.5 · 10 <sup>-4</sup>	$2.9 \cdot 10^{-4}$	$5.5 \cdot 10^{-4}$
$ V_{ub} $ (incl.)	40.9 · 10 <sup>-4</sup>	$4.6 \cdot 10^{-4}$	3.6 · 10-4
$\Delta M_d$	0.496 ps <sup>-1</sup>	0.007 ps <sup>-1</sup>	-
$\Delta M_{s}$	>14.9 ps <sup>-1</sup> at 95% C.L.	sensitivity	19.3 ps <sup>-1</sup>
m <sub>t</sub>	167 GeV	5 GeV	-
$f_{_{B_d}}\sqrt{\hat{B}_{_{B_d}}}$	230 MeV	30 MeV	15 MeV
$\xi = \frac{f_{B_s} \sqrt{\hat{B}_{B_s}}}{f_{B_d} \sqrt{\hat{B}_{B_d}}}$	1.16	0.03	0.04
B <sub>K</sub>	0.86	0.06	0.14
sin 2β	0.78	0.08	-

$ V_{cb} $ (incl.)	★ 41.7 · 10 <sup>-3</sup> (CKM)	$0.7 \cdot 10^{-3}$	0.8 · 10 <sup>-3</sup>
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Universal Unitarity Triangle 2002

AJB, Parodi, Stocchi

Use only quantities that are independent of parameters specific to a given Minimal Flavour Violation model



#### **Standard Model Unitarity Triangle**

#### (Parodi, Stocchi)



**Bayesian Output (June 2002)** 

AJB, Parodi, Stocchi hep-ph/0206

Input: CKM-Workshop +  $sin 2\beta = 0.78 \pm 0.08$ 

#### 95% Probability Regions

	SM	UUT	
η	0.292-0.406	0.274-0.418	
ρ	0.148-0.301	0.114-0.322	
sin 2β	0.665-0.821	0.655-0.822	
$\sin 2\alpha$	-0.66-0.11	-0.78-0.29	*
$\gamma$	$(46.1-68.6)^0$	$(42.1-73.8)^0$	*
R <sub>b</sub>	0.365-0.468	0.365-0.470	
R <sub>t</sub>	0.766-0.934	0.741-0.972	*
$ V_{td} /10^{-3}$	7.0-8.4	6.7-8.8	
$\left  \text{Im}\lambda_{t} \right  / 10^{-4}$	1.08-1.46	1.00-1.53	$\left(\lambda_{t}=V_{ts}^{*}V_{td}\right.$
$\left \mathbf{V}_{\mathrm{td}}\right  / \left \mathbf{V}_{\mathrm{ts}}\right $	0.174-0.211	0.168-0.220	
$\Delta M_{s}(ps^{-1})$	15.1-21.0	14.1-22.0	





Not much room for MFV-models (low tan $\beta$ ) that differ from the SM

Measurements of  $\gamma$  and  $\Delta M_s$  will be very important to find out whether <u>new phases</u> and/or <u>new operators</u> necessary.



# Outlook

Future Targets
$$R_b$$
 $\frac{\Delta V_{cb}}{V_{cb}} \approx 2\%$  $\frac{\Delta V_{ub}}{V_{ub}} \approx 5\%$  $\Delta M_s (B_s^0 - \overline{B}_s^0); \xi_{th}$  $\blacksquare$  $\Delta \sin 2\beta < 0.05$ 

 $\alpha$ ,  $\beta$ ,  $\gamma$  from various B-Decays

$$\begin{cases} \mathbf{K}^{+} \to \pi^{+} \nu \overline{\nu} \\ \mathbf{K}_{\mathrm{L}} \to \pi^{0} \nu \overline{\nu} \end{cases} \implies \begin{cases} \sin 2\beta, \ \overline{\eta} \\ |\mathbf{V}_{\mathrm{td}}| \end{cases}$$

#### Parameters in Electroweak Gauge Sector





<u>Until 2001</u>

$$|V_{us}|, |V_{cb}|, \overline{\rho}, \overline{\eta}$$

For the next years

$$|V_{us}|, |V_{cb}|, R_t, \sin 2\beta$$

appears like a better choice. Or, even better:

$$\left|V_{us}\right|, \left|V_{cb}\right|, R_{t}, \beta$$



# Fundamental Flavour Parameters

(June 2002) AJB, Parodi, Stocchi

$$|V_{us}| = 0.221 \pm 0.002$$
$$|V_{cb}| = (40.6 \pm 0.8) \cdot 10^{-3}$$
$$R_{t} = 0.85 \pm 0.04$$
$$\beta = (24 \pm 2)^{\circ}$$

$$(\sin 2\beta = 0.74 \pm 0.05)$$



(AJB, Parodi, Stocchi)



#### Leading Strategies for $(\overline{\rho}, \overline{\eta})$

(AJB, Parodi, Stocchi)







1989-1999

### **Electroweak Precision Studies**



**CKM Precision Studies** 

 $\lambda, A, \overline{\rho}, \overline{\eta}, m_t$ 

with the hope to discover **New Physics** and learn about **Flavour Dynamics** 

# The Future until 2011 should be very exciting