

# Diffusion of Cosmic Ray Nuclei in the Galaxy and $\gamma$ -ray and $\pi$ diffuse emissions

D. Grasso (INFN, Pisa)

in collaboration with

C. Evoli (SISSA),

D. Gaggero (INFN, Pisa Un.),

L. Maccione (SISSA & INFN, Trieste)

# Multi-messenger approach to CR

Galactic cosmic rays (CRs) origin and propagation can be probed by:

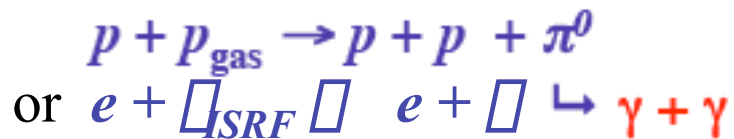
- primary direct measurements (energy spectrum, composition and angular distribution)
- or indirectly by their **secondary products**

They include:

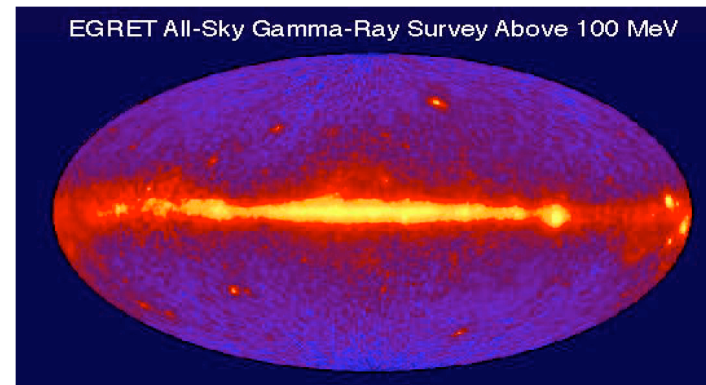
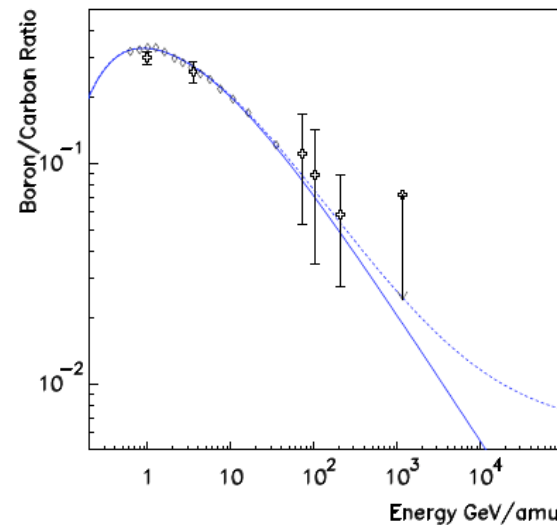
- secondary nuclei  
(e.g. B, Be, subFe... produced by spallation)

*Exp: ATIC, CREAM, TRACER...*

- Diffuse gamma-ray emission



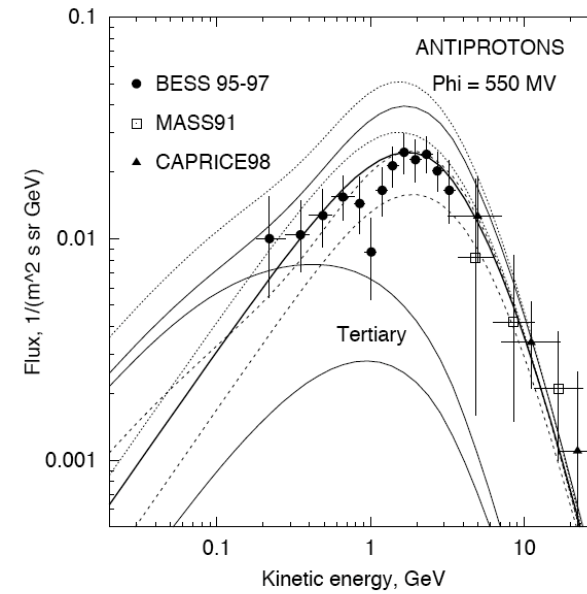
*Exp: GLAST, MILAGRO, TIBET AS... ..*



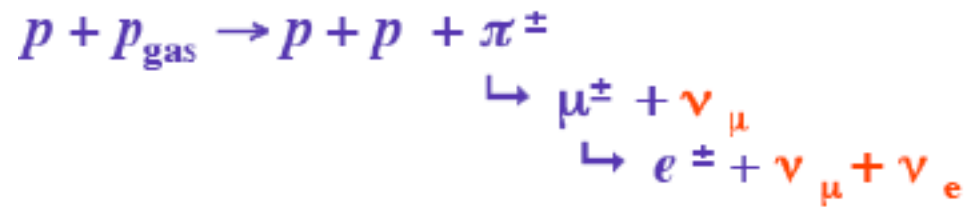
# Multi-messenger approach to CR

- secondary antimatter (antiprotons, positrons)

*Exp: BESS, PAMELA....*



- for the future also neutrino detection



*Exp: ICECUBE, ANTARES, KM3NET..*

# Diffusion models

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While simple models like the leaky-box and modified slab model can explain the s/p ratios above the GeV, more complex models are called for to provide a comprehensive description of all available data.

The general approach:

- assume a source (typically SNR) distribution
- assume a gas distribution (while details are not so crucial to reproduce the s/p they are to model the  $\gamma$ -ray diffuse emission)
- solve the transport equation numerically in the steady state limit

$$\frac{\partial N_i(E, r, z)}{\partial t} - \vec{\nabla} \cdot (D(r, z) \vec{\nabla} N_i(E, r, z)) = Q_i(E, r, z) - n_{\text{gas}} \beta_i \sigma_i N_i + \sum_{j>i} n_{\text{gas}} \beta_j \sigma_{ji} N_j$$

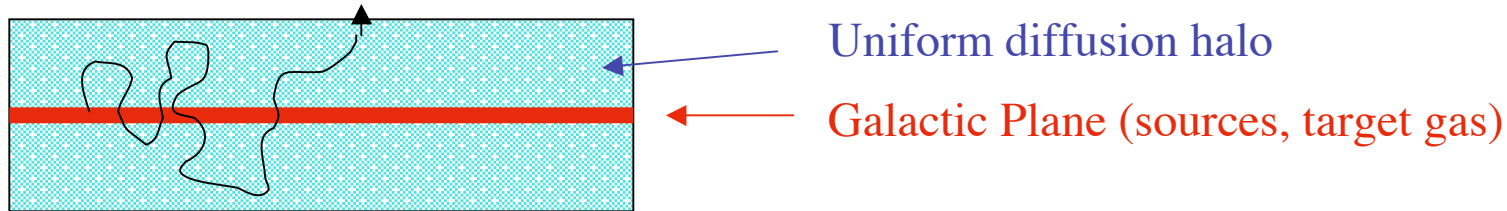
Energy losses/gains and convection are disregarded here (see below)

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# Main diffusion models

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## Two zone-diffusion model *Maurin, et al., 2001*



The diffusion equation is solved analitically

Ok for secondary/primary and antimatter; cannot model  $\gamma$ -ray emission !

## GALPROP *Strong & Moskalenko, 1998, 2004*

- It adopts realistic continuous distribution for the sources and the gas
- The diffusion equation is solved numerically
- s/p ; antimatter;  $\gamma$ -ray spectrum and angular distributions can all be modelled

**BOTH ASSUME ISOTROPIC AND UNIFORM DIFFUSION**

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# Our model

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We developed a new numerical diffusion code (DRAGON)

We adopt the same nuclei spallation, and antiproton production routines of the public GALPROP code

Differently from GALPROP

- we adopt a SNR distribution based on pulsars and progenitor stars (as in [Ferriere '01](#))
- we adopt a more realist gas distribution in the bulge region (as in [Ferriere '07](#))
- **we allow for a spatially variable diffusion coefficient**

$$\mathbf{D}(\mathbf{E}; \mathbf{r}, \mathbf{z}) = \mathbf{D}_0 \left( \frac{R}{R_0} \right)^\alpha \mathbf{f}(\mathbf{r}) \exp(\mathbf{z}/z_t)$$

$$D_0 \equiv D(r_\odot, 0) \quad r_\odot = 8.5 \text{ kpc}, \quad R_0 = 3 \text{ GeV} \text{ reference rigidity}$$

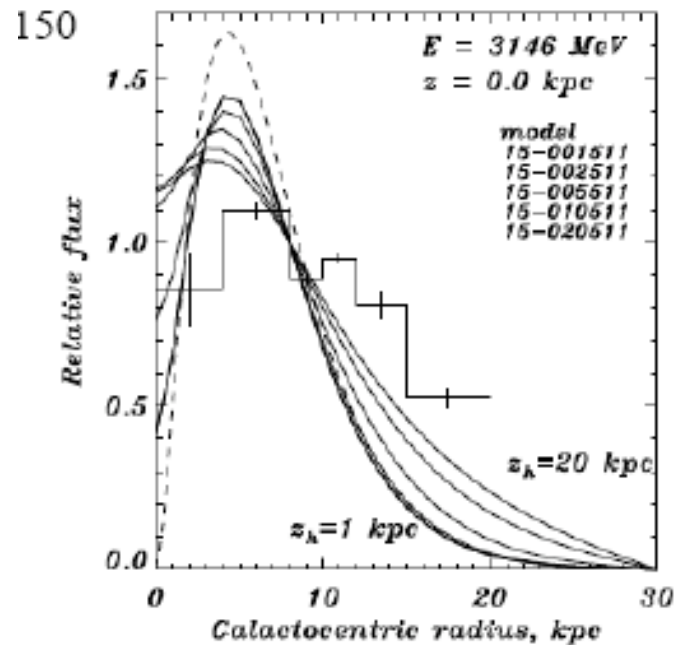
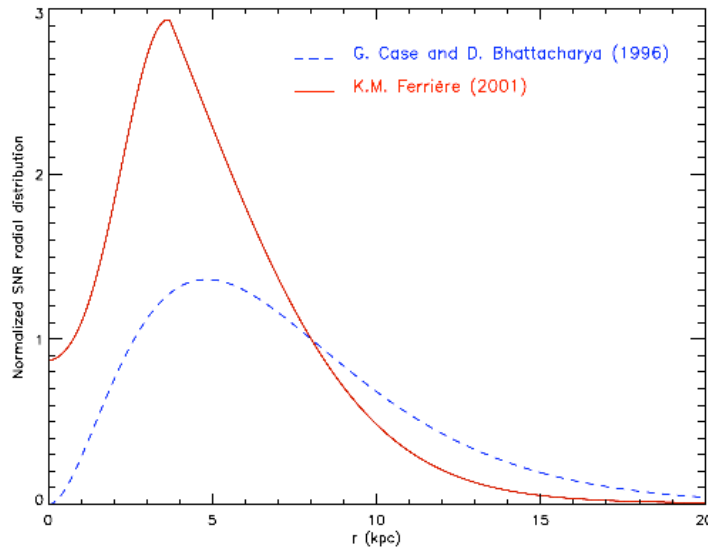
- we allow for different nuclei injection spectra  $\psi_i$
  - we focus only on  $E_k > 1 \text{ GeV}/n$  which allows to neglect low energy physics (convection, re-acceleration: poorly known)
  - so far we only consider nuclei (no electrons).
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# CR sources: *the gradient problem*

Energetic of CRs and recent X-rays and TeV observations point to SNRs as most likely sources

□ CR spatial distribution should keep same memory of that of SNR

- SNR radio shells surveys (Case & Battacharya, '96, '98) □ rather flat profile  
(Several problems: incomplete, selection effects, do not fit radioactive nuclides distribution)
- Pulsars and old stars (Ferriere '01, Lorimer '04) □ more peaked profile



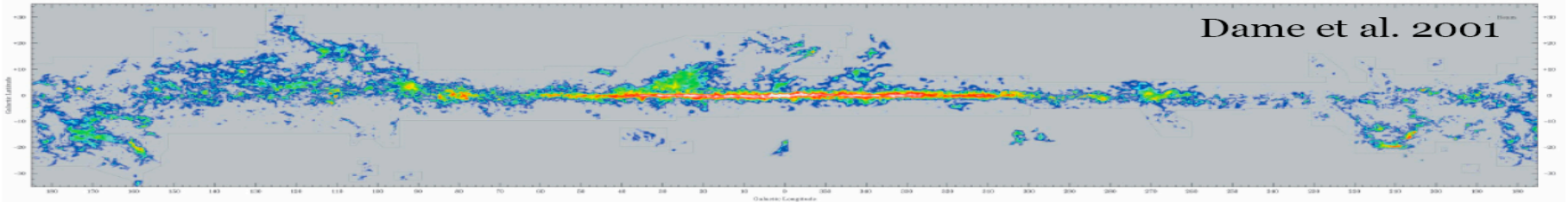
CB is already incompatible with EGRET

The problem is even more exacerbated using the more realistic pulsar based distribution

“CR gradient problem”

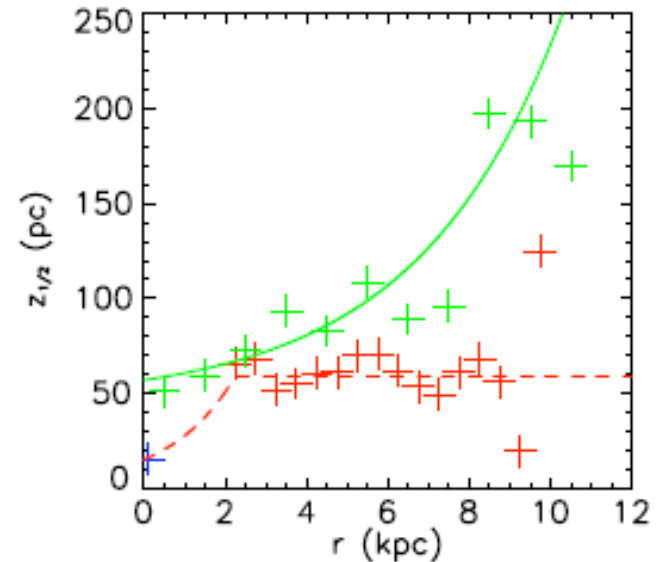
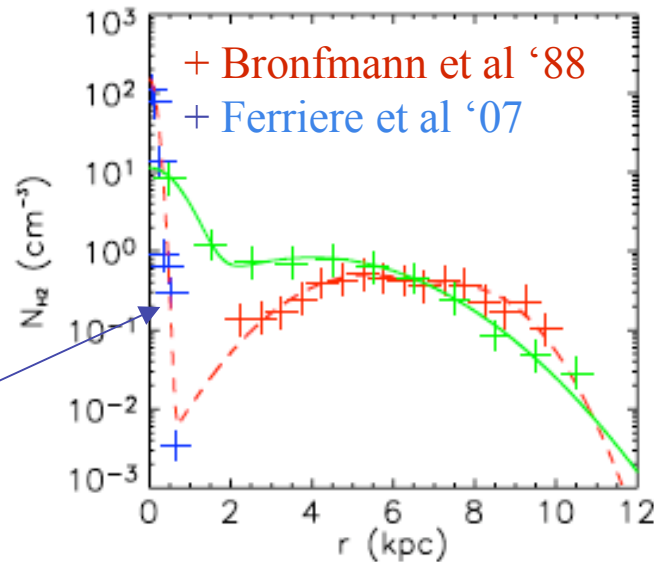
# Gas distribution

H<sub>2</sub> is the main target. Generally traced by <sup>12</sup>CO (J=1-0).



Doppler shift (velocity) + galactic rotation curve

2-D profiles:

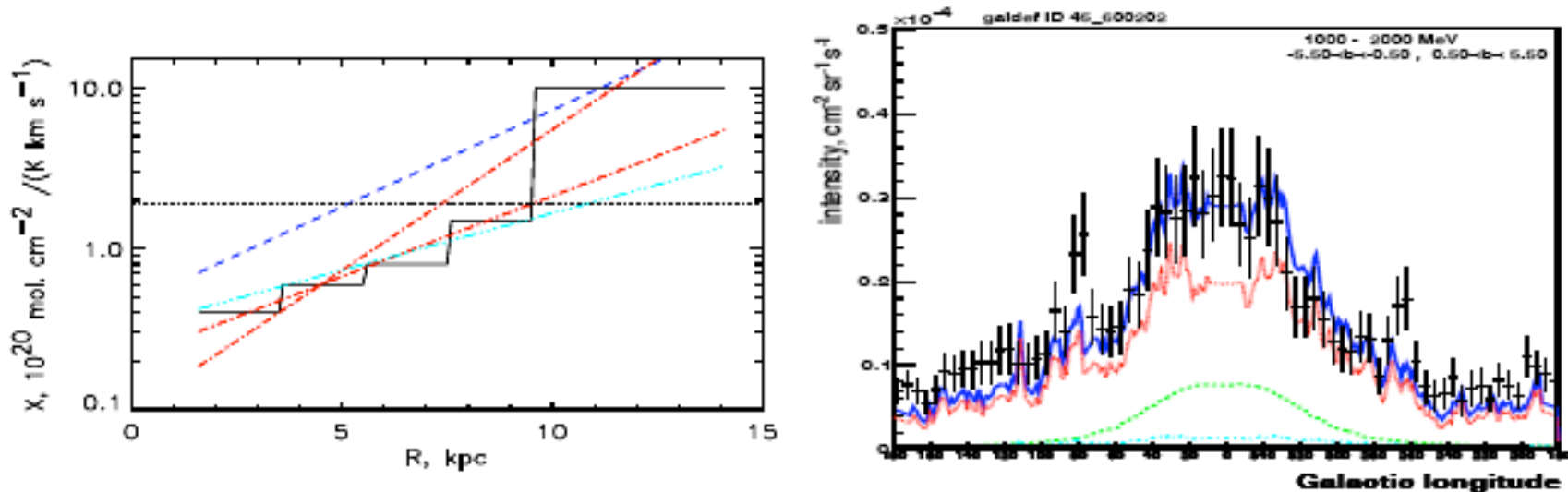


HI and HII are also considered with the same distributions as in GALPROP



# Gas distribution: $X_{\text{CO}}$

A scaling factor is needed to convert CO maps into gas column density.  
Expected to change with  $r$ , dependence on the metallicity.  
Some tuning needed to achieve agreement with EGRET measurements  
(“CR gradient” may be problem, see [Strong et al., 2004](#)).



Take in mind, however, that the uncertainty on  $X_{\text{CO}}$  is about a factor of 2

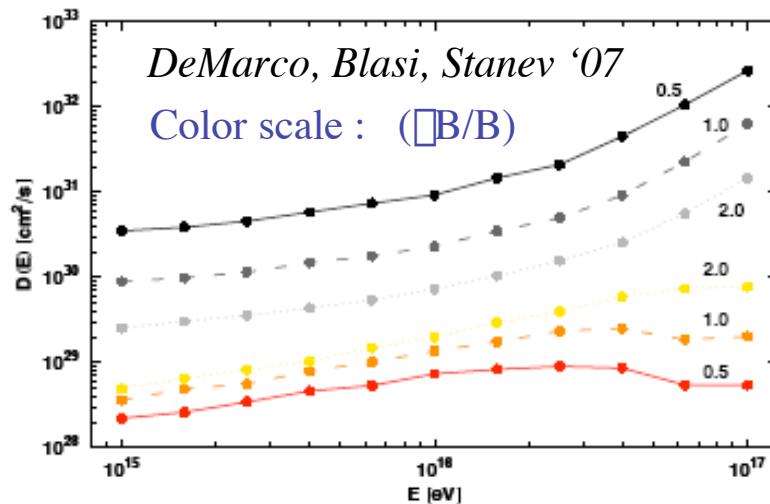
The slope of  $X_{\text{CO}}$  may be flatter outside the bulge

# Few reasons to adopt a spatially changing D

In the quasi-linear theory of diffusion

$$D_{\parallel} \simeq \frac{1}{3} c r_L \left( \frac{\delta B_{\text{res}}}{B_0} \right)^{-2} \quad D_{\perp} \approx D_{\parallel} \left( \frac{\delta B_{\text{res}}}{B_0} \right)^4 \propto \left( \frac{\delta B_{\text{res}}}{B_0} \right)^2$$

Montecarlo simulations: (see also *Casse et al. 2001*, *Candia et al. 2004*)



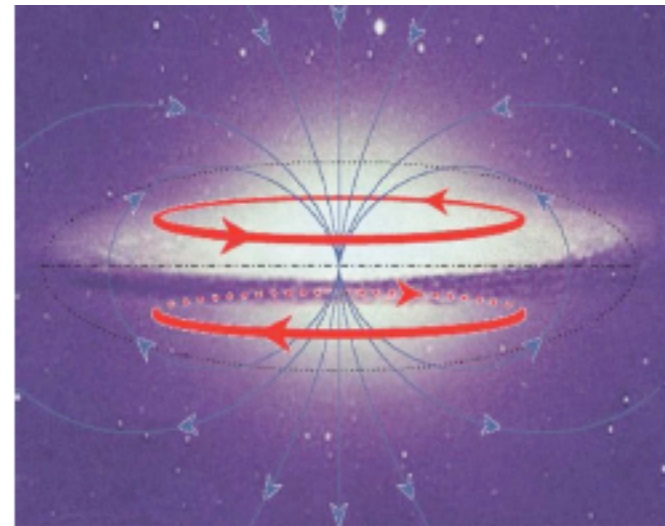
$D_{\parallel}$   $\square$

Opposite behaviour for increasing turbulence strength

$D_{\perp}$   $\uparrow$

$D_{\perp}$  should be the relevant coefficient if the regular galactic magnetic fields is prevalently azimuthally oriented as suggested from Faraday RM of pulsars

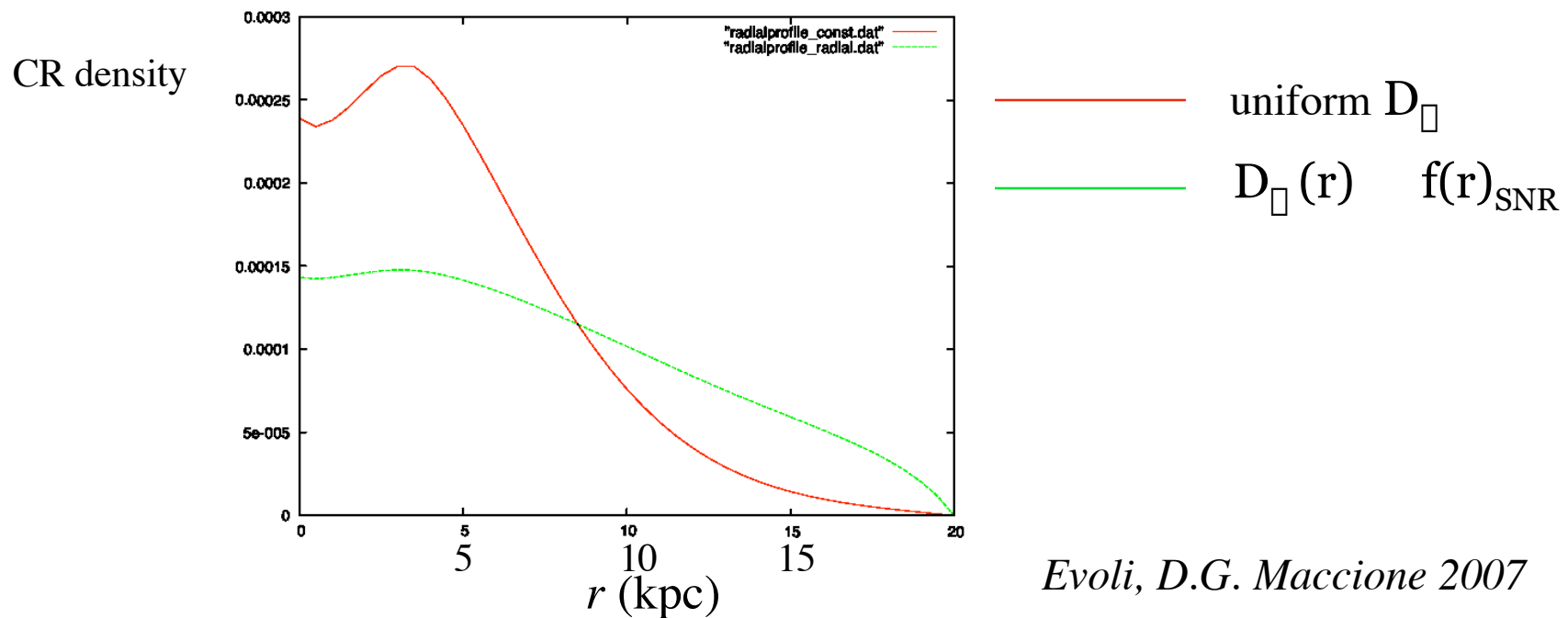
*Han et al. 2004*



# The effect of $D(r)$

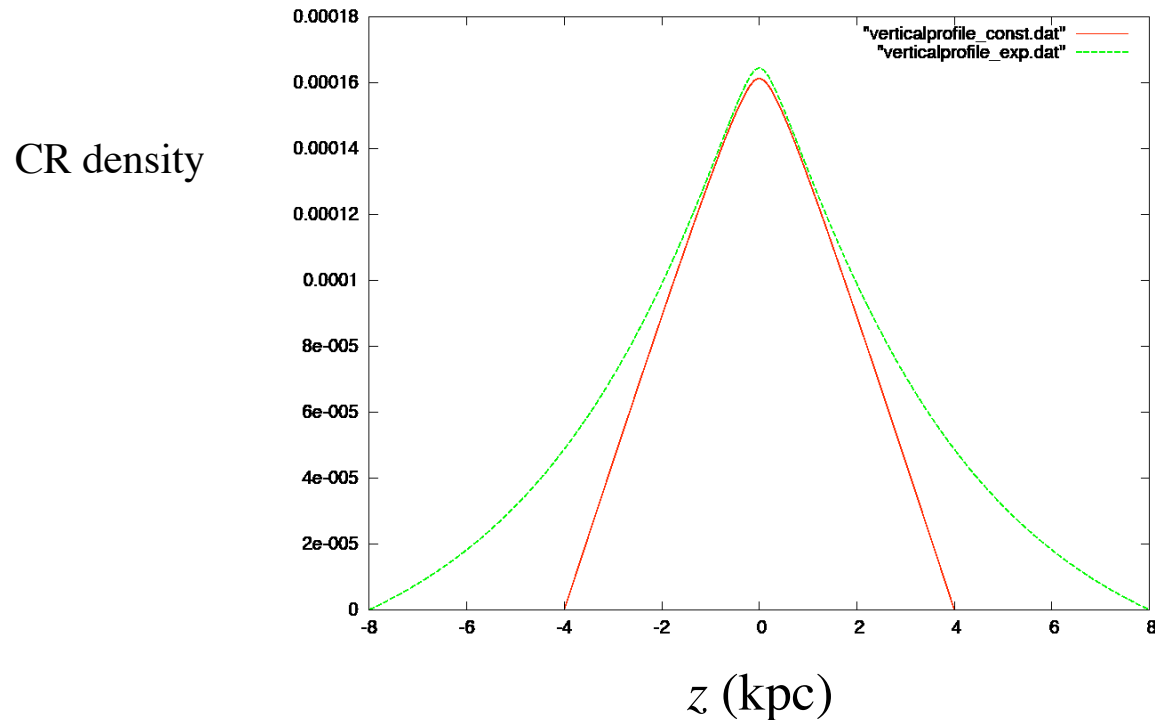
Turbulence is expected to be driven by CRs

- $B/B$ , hence  $D_{\square}$ , may be enhanced in CR (SNR) rich regions
- faster CR escape from those regions
- **smoothing of the CR distribution**



# The effect of $D(z)$

$$D(E; r, z) \quad \exp(z/z_t)$$



Not a big effect on the spallation products (production takes place for  $z \ll 1$  kpc)  
The effect may be large for the  $\gamma$ -ray emission at high latitudes and the propagation of DM annihilation products

# **Preliminar New Results**

# B/C

It is generally used to normalise the D and its energy dependence

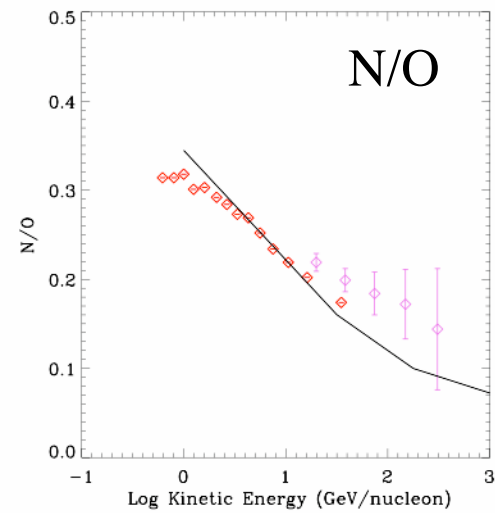
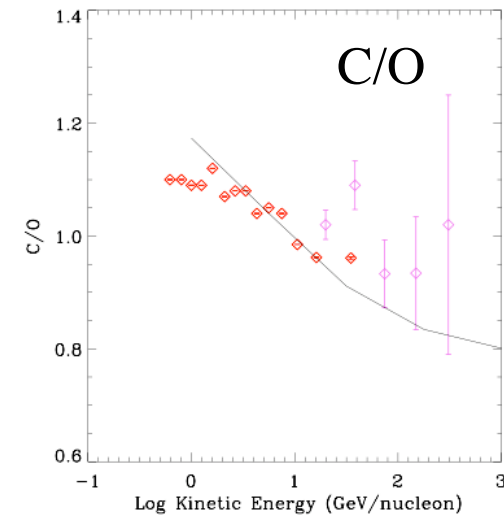
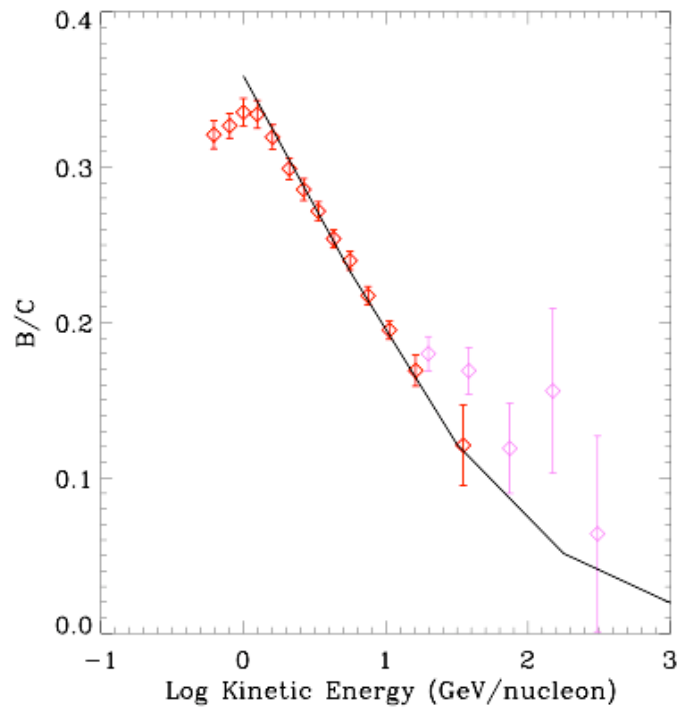
$$D_o = 2.1 \times 10^{28} \text{ cm}^2/\text{s} \quad D_o = 2.5 \times 10^{28} \text{ cm}^2/\text{s}$$

(radial + exp vertical prof.)      (uniform)

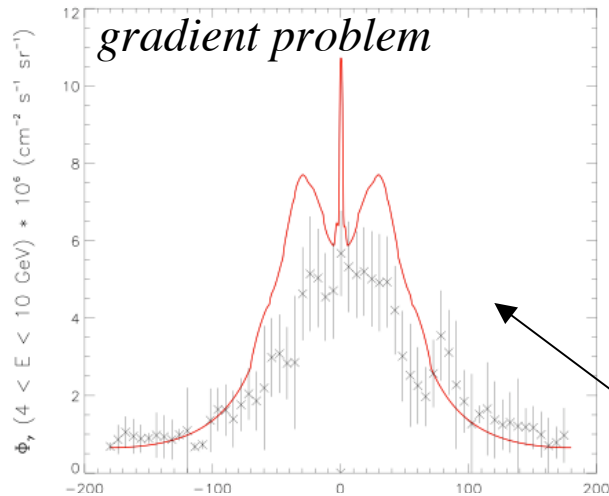
OK with GALPROP

$$Z_t / z_{\text{max}} = 4 \text{ kpc} \quad \alpha = 0.6$$

all injection spectra have the same slope  $\beta = 2.1$



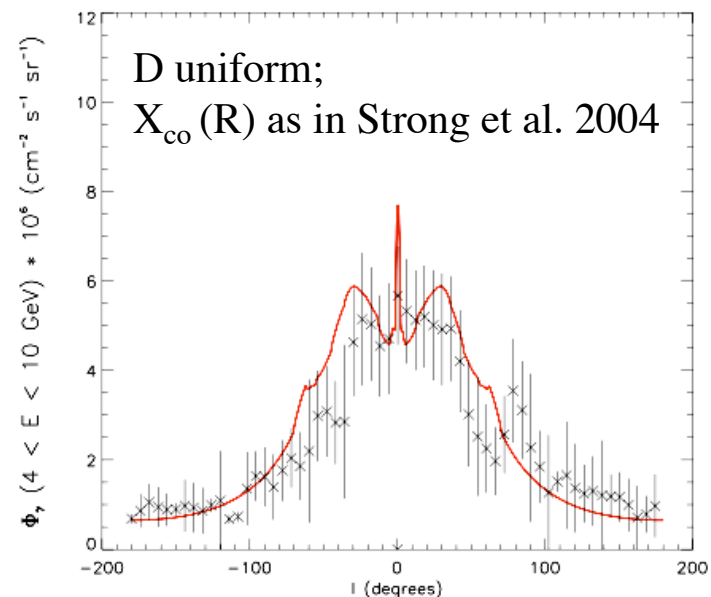
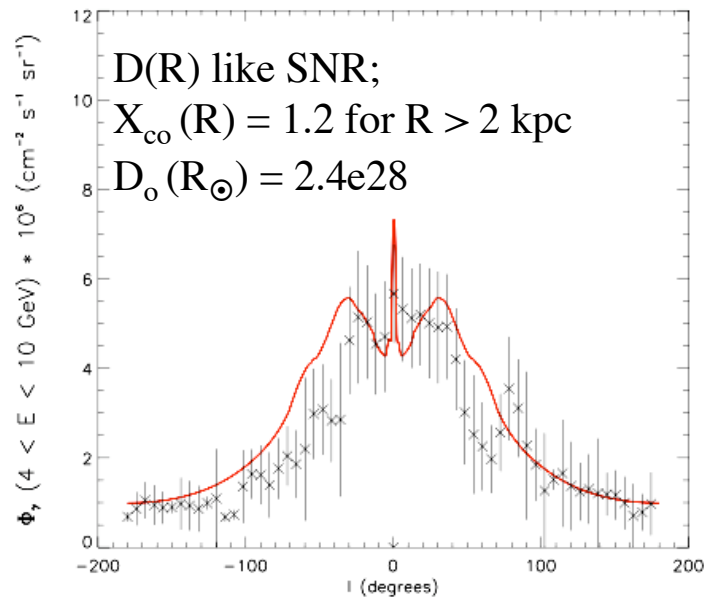
# γ-ray distribution - comparison with EGRET



$4 < E < 10 \text{ GeV}; |b| < 1^\circ$

There is a degeneracy between the  $X_{\text{CO}}$  and  $D$  radial dependences

D(R) uniform;  
 $X_{\text{CO}}$  (R) uniform



# $\gamma$ -ray and $\pi$ diffuse emission in the TeV

MILAGRO found  $\Phi_\pi(15 \text{ TeV}) = (23.1 \pm 4.5) \times 10^{-13} \text{ (TeV cm}^2 \text{ s sr)}^{-1}$   
for  $30^\circ < l < 65^\circ, |b| < 2^\circ$  *Abdo et al. 2008*

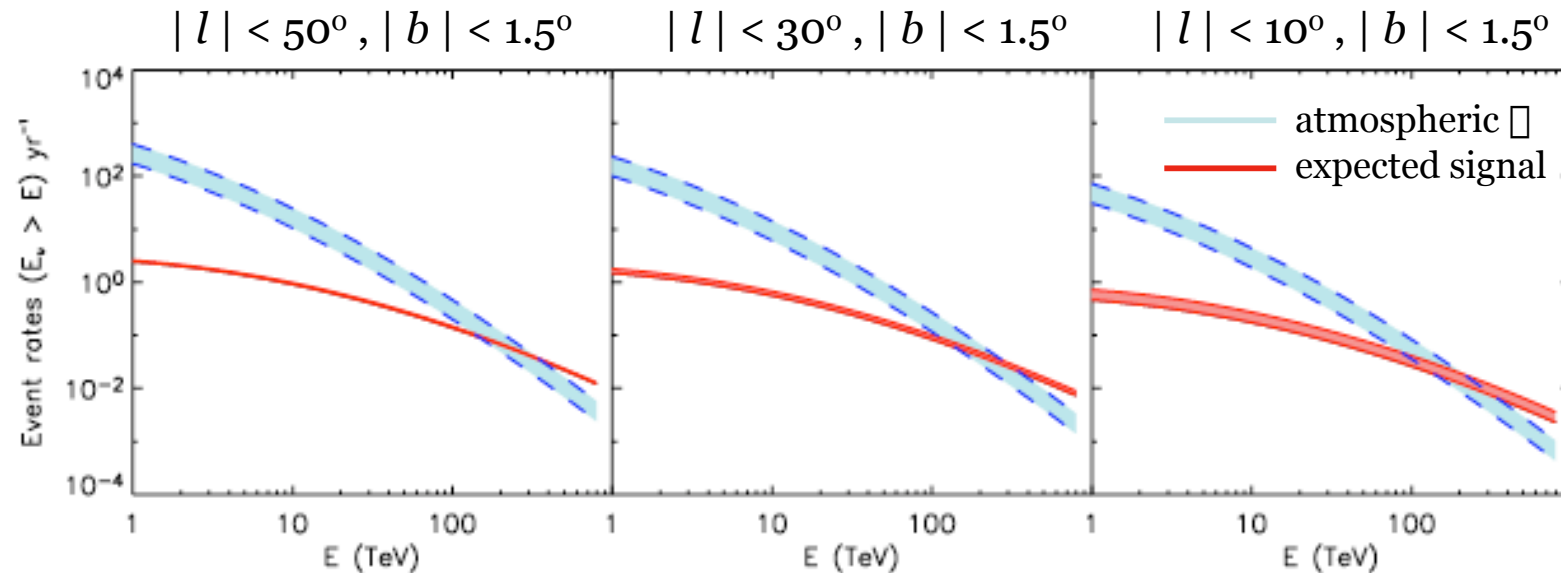
see S. Casanova talk !

Our model:  $\Phi_\pi(15 \text{ TeV}) \approx 4 \times 10^{-13} \text{ (TeV cm}^2 \text{ s sr)}^{-1}$

The same as for the conventional GALPROP model

A strong IC component or harder spectrum in the inner Galaxy have to be invoked !

For a  $\text{km}^3$  neutrino telescope in the Mediterranean we found



Hard to detect !

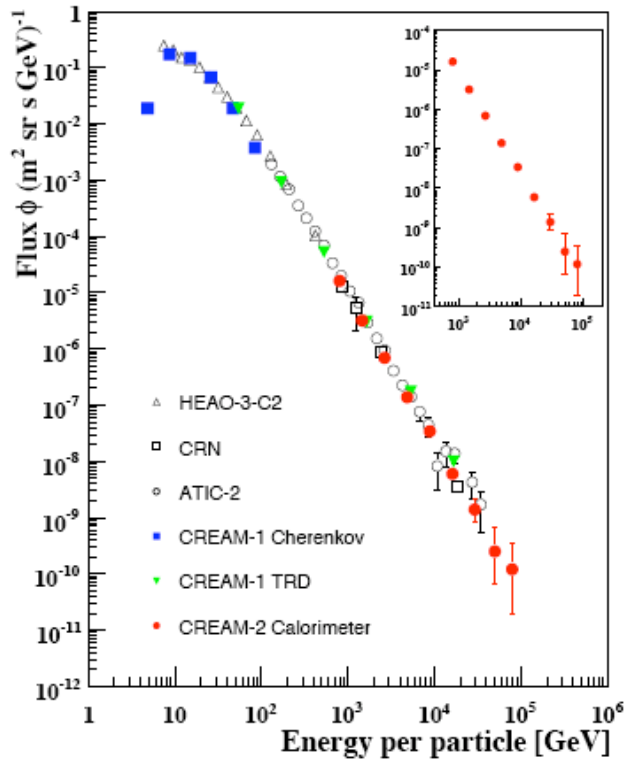
*Evoli, D.G, Maccione, 2007*



# Different spectra for C and O ?

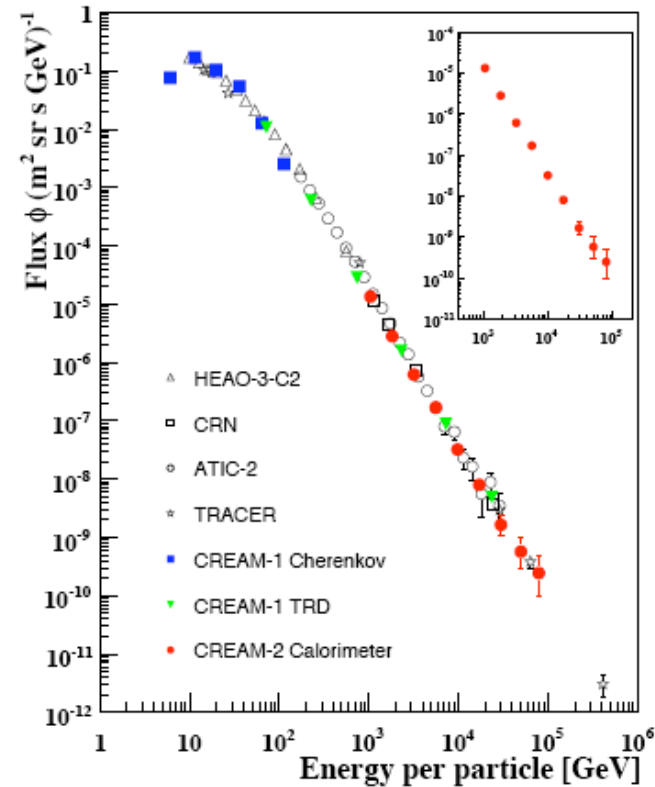
Zeigler et al. [CREAM], ICRC 2007

## CARBON



$$\Gamma_C = 2.56 \pm 0.11$$

## OXIGEN



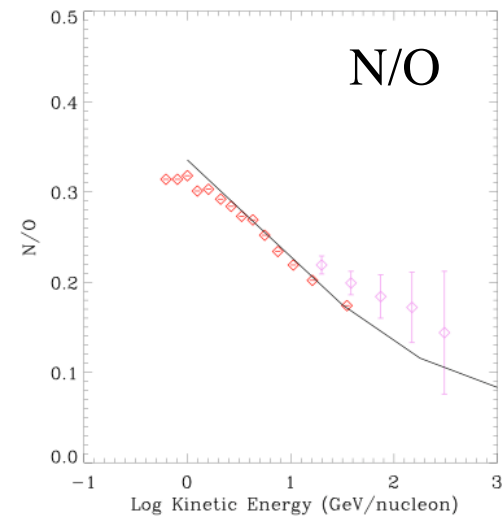
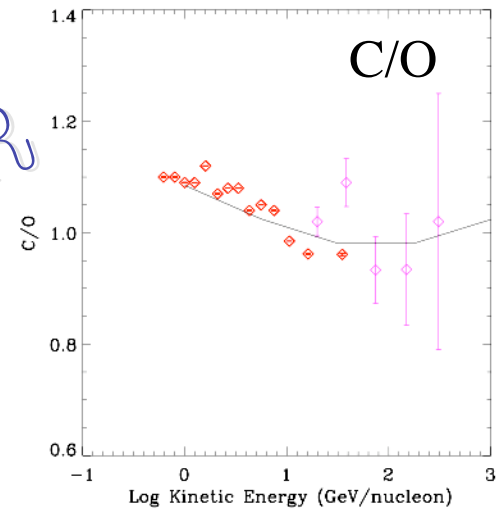
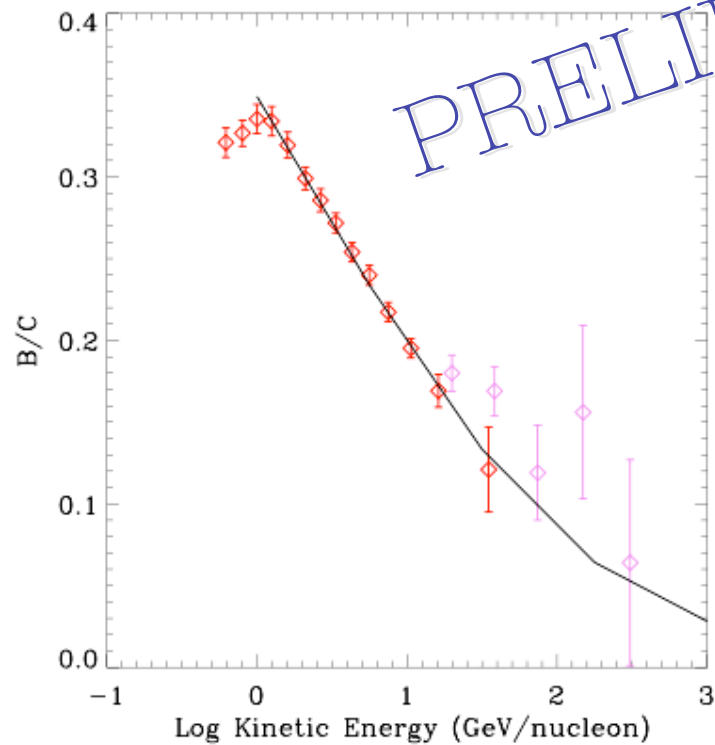
$$\Gamma_O = 2.61 \pm 0.10$$

# B/C (with a less steep C spectrum)

$$D_o = 2.5 \times 10^{28} \text{ cm}^2/\text{s}$$

$$Z_t = 4 \text{ kpc}$$

$$\alpha = 0.5$$



$\alpha = 0.5$  (Kraichnan) may be the preferred value !

# Conclusions

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- DRAGON is a new numerical code to model galactic CR nuclei propagation and interaction
- It allows for a spatially changing  $D$  both in  $r$  and in  $z$
- Observed B/C abundances and energy slopes are nicely reproduced for  $E_k > \sim 1 \text{ GeV/n}$
- ( Other secondary nuclei and antiproton spectra also reproduced - in progress)
- Re-acceleration seems not to be required to explain the B/C at those energies
- The preferred rigidity dependence of  $D$  is  $\alpha = 0.6$  if C, O share the same spectral slope and closer to  $0.5$  if the C spectrum is smoother as suggested by CREAM
- The  $\gamma$ -ray profile along the GP observed by EGRET is reproduced either with a radially changing  $X_{co}$  or assuming a physically motivated  $D(r)$  profile

Future work: - adopt more detailed gas-models

- include energy losses to model electrons and IC emission

- apply to study dark matter annihilation product propagation

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