



# The 3<sup>rd</sup> generation quarks in warped models : *LHC predictions from LEP/Tevatron anomalies*

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*with*

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PRD 2010 + arXiv:1105.3158

## Outline

I) Introduction: a warped model

II)  $A_{FB}^t$  and  $t\bar{t}$  cross section @ Tevatron

III)  $A_{FB}^b$  and EW precision tests @ LEP

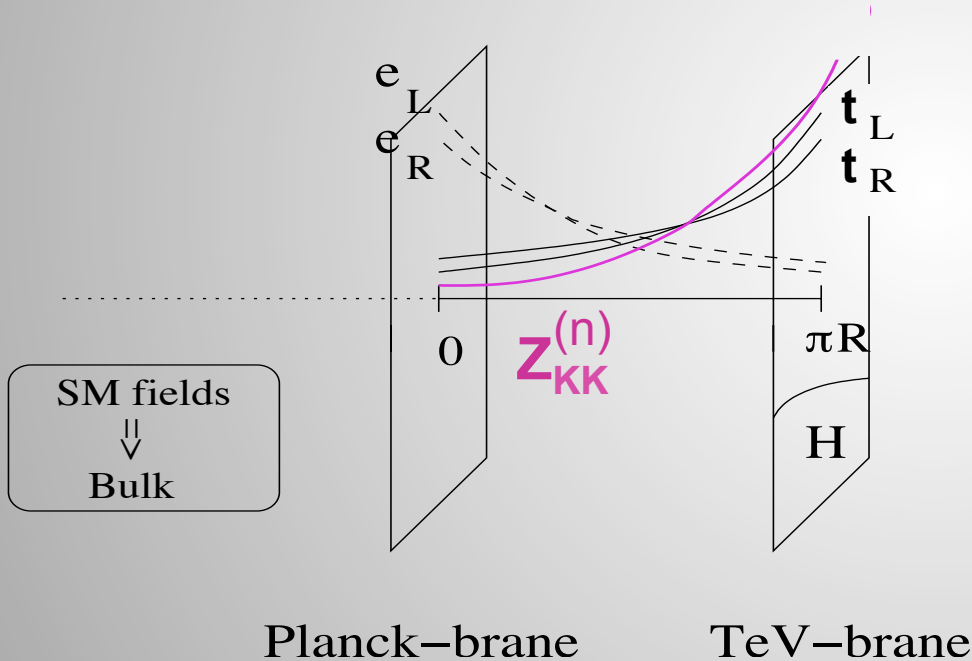
IV) Constraints and predictions @ LHC

V) Other scenarios for  $A_{FB}^t$  ?

VI) Conclusions

# 1) Introduction: a warped model

## The Randall-Sundrum (RS) scenario with bulk fields:



- RS addresses the gauge *hierarchy* :

$$M_{grav} \approx TeV \approx Q_{EW}$$

*Randall, Sundrum (1999)*

- RS generates the mass *hierarchies* :

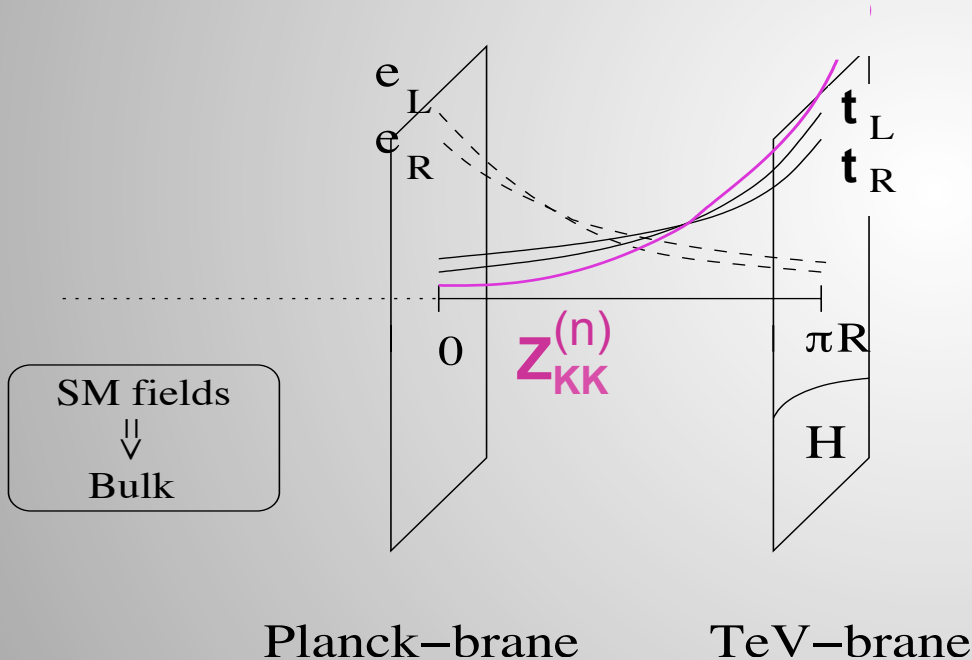
$$m_e \ll m_t$$

*Gherghetta, Pomarol (2000)*

...

# 1) Introduction: a warped model

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Gherghetta, Pomarol (2000)

...

➔ New Physics effects in the heavy fermion sector !

**+ attractive features of the RS scenario with bulk fields  
(= dual via AdS/CFT to composite Higgs & top models) :**

- WIMP candidates for the dark matter of universe:  
a LKP stable due to a possible KK-parity (*like in UED*)
- Unification of gauge couplings (*as in ADD*) at high-energies
- *Extra-Dimensions* =  
necessary ingredients for higher-energy string theories

## The EW precision constraints in warped models :

Bulk gauge bosons/fermions mix with their KK excitations

=> tree-level contributions to EW observables

**Ways out** to respect the constraints from EW precision data for  $M_{\text{KK}} \sim \text{TeV}$  :

## The EW precision constraints in warped models :

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**Ways out** to respect the constraints from EW precision data for  $M_{\text{KK}} \sim \text{TeV}$  :

~> **Gauge custodial symmetry in the bulk**

Agashe, Delgado,  
May, Sundrum (2003)

$$\begin{array}{ccc} O(4) & & SU(2)_L \times SU(2)_R \\ \Downarrow & \approx & \Downarrow \\ O(3) & & SU(2)_V \times P_{LR} \end{array}$$

~> **Brane-localized kinetic terms for fermions/gauge fields**

Carena et al. (2002) Aguilera et al. (2003)

~> **Modification of the AdS metric in the vicinity of the IR brane**

Cabrer, Gersdorff, Quiros (2010)

« *Minimal* » representations under  $SU(2)_L \times SU(2)_R \times U(1)_X$ :  $H=(2,2)_0$

$$\begin{pmatrix} t_{1L} & b'_L & q'_{-4/3L} \\ b_{1L} & q''_{-4/3L} & q'_{-7/3L} \end{pmatrix}_{-5/6} \quad (b_R \ q'_{-4/3R})_{-5/6} \quad \begin{pmatrix} q'_{5/3L} & t_{2L} \\ t'_L & b_{2L} \end{pmatrix}_{2/3} \quad (t_R)_{2/3}$$



“custodians”

$$SU(2)_R \longrightarrow U(1)_R$$

$$U(1)_R \times U(1)_X \longrightarrow U(1)_Y$$

$$\mathbf{W}_R^3 \quad \mathbf{B}_X \longrightarrow \mathbf{B}_Y \quad ( + \mathbf{Z}'^{KK} )$$



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$$W_R^3 \quad B_X \longrightarrow B_Y \quad (+ Z' \text{ KK})$$

$Z'$  charges ( $I_{3R}$  isospin) and coupling ( $g_{Z'} \sim 2$ )  $\Rightarrow$   $Zbb$  couplings addressing  $A_{FB}^b$

$t_R$  singlet: no custodian top partners  $\Rightarrow$  possible large  $g^{KK} t\bar{t}$  couplings favor  $A_{FB}^t$

## II) $A_{FB}^t$ and $t\bar{t}$ cross section @ Tevatron

### $A_{FB}^t$ at Tevatron

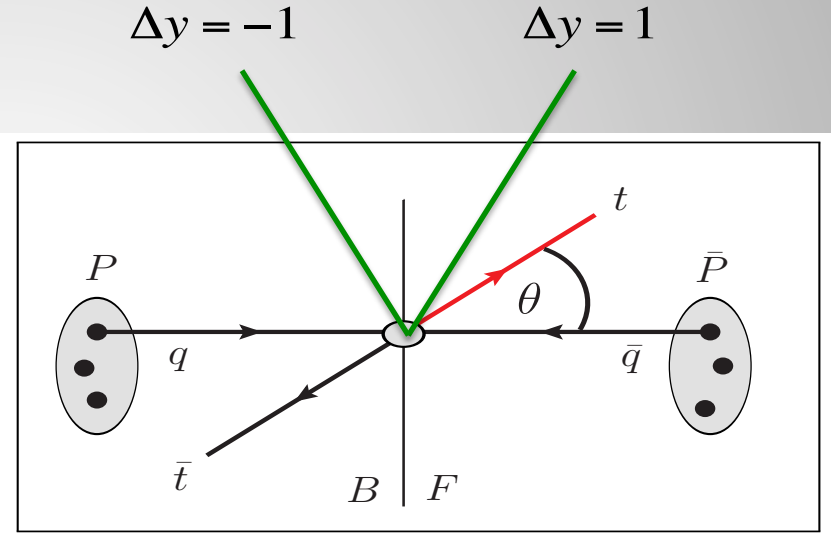
« What is the Forward-Backward asymmetry for the top quark ? »

$\neq 0$  with Parity-violating couplings

$$A_{FB}^t = \frac{\sigma^F - \sigma^B}{\sigma^F + \sigma^B} = \frac{\sigma[\cos \theta_t^* : 0 \rightarrow 1] - \sigma[\cos \theta_t^* : -1 \rightarrow 0]}{\sigma[\cos \theta_t^* : 0 \rightarrow 1] + \sigma[\cos \theta_t^* : -1 \rightarrow 0]} = \frac{\sigma[y_t > 0] - \sigma[y_t < 0]}{\sigma[y_t > 0] + \sigma[y_t < 0]}$$

(  $t\bar{t}$  rest frame )

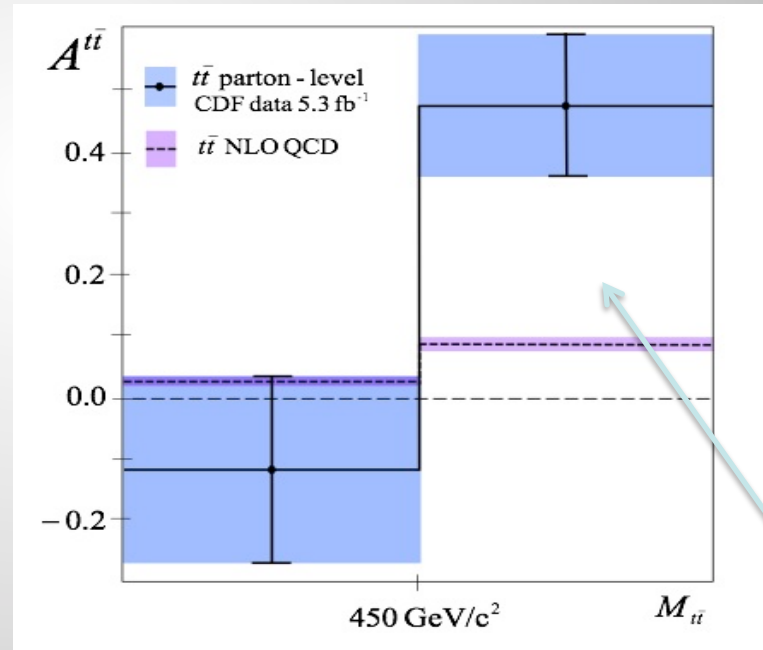
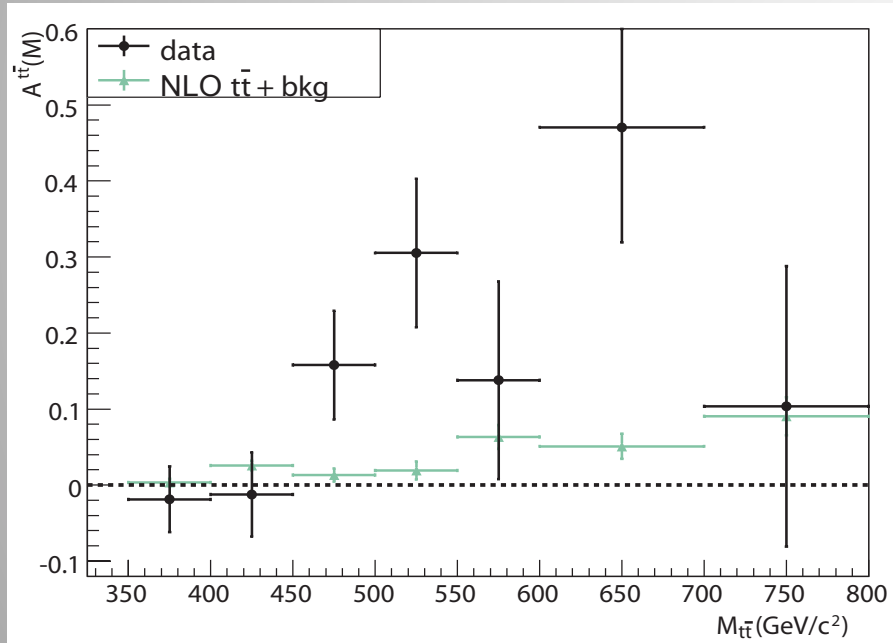
Rapidity :  $y_t = \frac{1}{2} \ln[(E + p_z)/(E - p_z)] = \Delta y/2$



the data we use cause: most recent, unfolded and the only ones on rapidity dependence

01-2011 CDF in the lepton+jets channel with  $5.3\text{fb}^{-1}$  :

$A_{\text{FB}}^t = 0.158 \pm 0.075$  (+1.3 sigma from SM prediction)

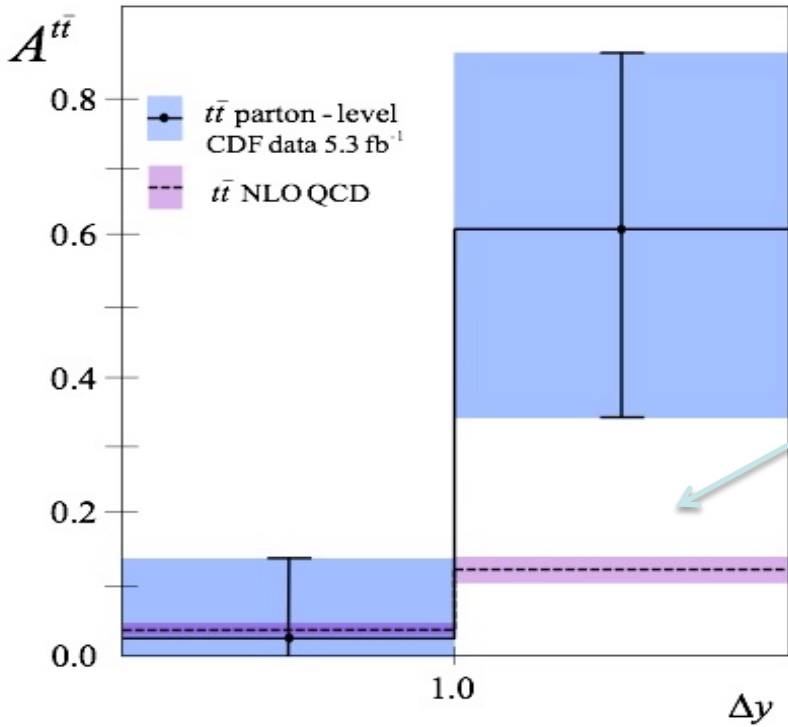


(  $t\bar{t}$  rest frame )

unfolding



+3.4 standard deviations from SM



+1.9 standard deviation from SM

(  $t\bar{t}$  rest frame, unfolded )

$$A_{\text{FB}}^{|\Delta y| < 1} = \frac{N(1 > \Delta y > 0) - N(-1 < \Delta y < 0)}{N(1 > \Delta y > 0) + N(-1 < \Delta y < 0)},$$

$$A_{\text{FB}}^{|\Delta y| > 1} = \frac{N(\Delta y > 1) - N(\Delta y < -1)}{N(\Delta y > 1) + N(\Delta y < -1)}$$

$$|\Delta y| < 3$$

## A<sup>t</sup><sub>FB</sub> in the considered warped model



+ interferences with SM  
(negligible EW gauge contrib.)

$A_{FB}^t$  non-vanishing (Parity violation)
 [

 $g_s Q(c_{t_L}) \neq g_s Q(c_{t_R})$   
 $g_s Q(c_{q_L}) \neq g_s Q(c_{q_R})$ 
]
⇒

*slightly closer to TeV-brane :*  
 $c_{u_L}, c_{d_L} \lesssim 0.5$ 
]
⇒

 $M_{KK} \sim 1.5 - 2 \text{ TeV}$ 
]
⇒

 $A_{FB}^t$  significant
 
]
⇒

 EW tests not so far treated in this setup

5D mass :  $c k$

## A<sup>t</sup><sub>FB</sub> in the considered warped model



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$A_{FB}^t$  significant  $\Rightarrow M_{KK} \sim 1.5 - 2 \text{ TeV}$

EW tests not so far treated in this setup

We will show that EW fits are OK for :

$c_{u/d_L} \sim 0.44, c_{u/d_R} \sim 0.8, c_{c/s_L} \sim 0.6, c_{c_R} \sim 0.6,$   
 $c_{s_R} \sim 0.49, c_{t/b_L} \sim 0.51, c_{b_R} \sim 0.53, c_{t_R} \sim -1.3$

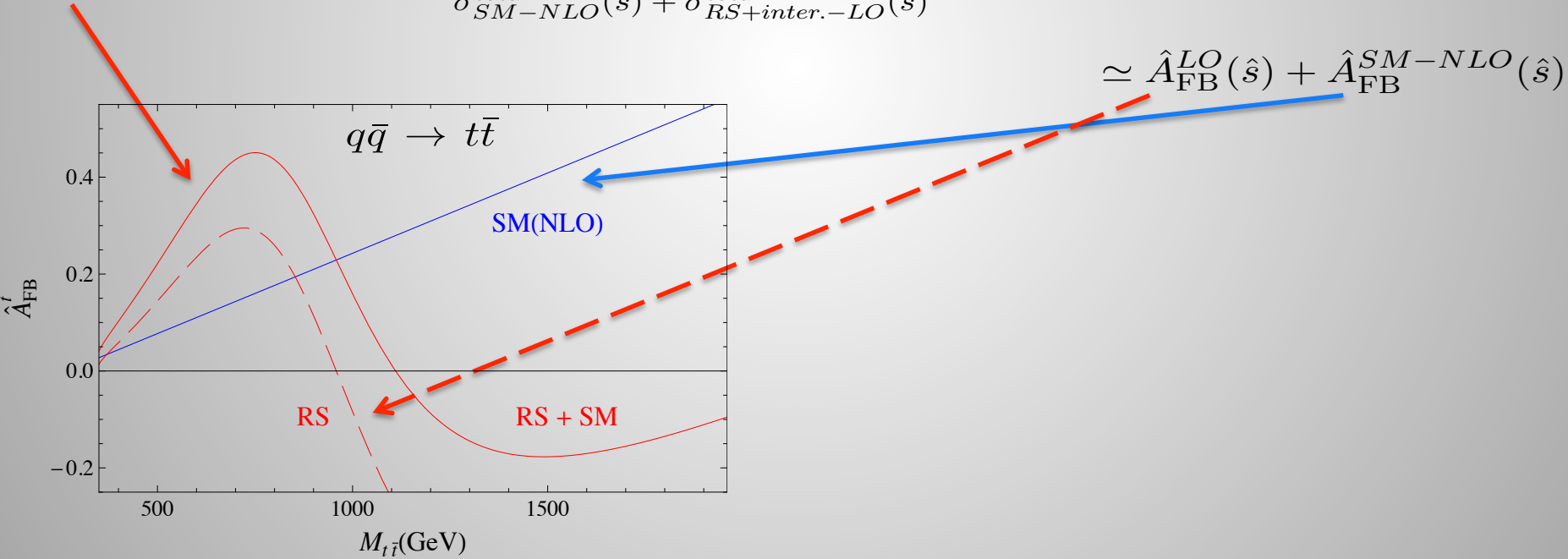
# Asymmetry at parton level (neglecting 2<sup>nd</sup>/3<sup>rd</sup> generation + gluon initial state)...

$$\hat{A}_{\text{FB}}^{LO}(\hat{s}) = a_q a_t \frac{4\pi\alpha_s^2(\mu_r) \beta_t^2 |\mathcal{D}|^2 [(\hat{s} - M_{KK}^2) + 2v_q v_t \hat{s}]}{9 \hat{\sigma}_{SM-LO}^{\text{total}}(\hat{s}) + \hat{\sigma}_{RS+inter.-LO}^{\text{total}}(\hat{s})}$$

$$\begin{cases} a_q = (Q(c_{qR}) - Q(c_{qL}))/2, \\ a_t = (Q(c_{tR}) - Q(c_{tL}))/2, \\ v_q = (Q(c_{qR}) + Q(c_{qL}))/2, \\ v_t = (Q(c_{tR}) + Q(c_{tL}))/2, \end{cases}$$

$$\hat{A}_{\text{FB}}^{NLO}(\hat{s}) = \frac{(\hat{\sigma}_{SM-NLO}^F(\hat{s}) + \hat{\sigma}_{RS+inter.-LO}^F(\hat{s})) - (\hat{\sigma}_{SM-NLO}^B(\hat{s}) + \hat{\sigma}_{RS+inter.-LO}^B(\hat{s}))}{\hat{\sigma}_{SM-NLO}^{\text{total}}(\hat{s}) + \hat{\sigma}_{RS+inter.-LO}^{\text{total}}(\hat{s})}$$

$$\simeq \hat{A}_{\text{FB}}^{LO}(\hat{s}) + \hat{A}_{\text{FB}}^{SM-NLO}(\hat{s})$$

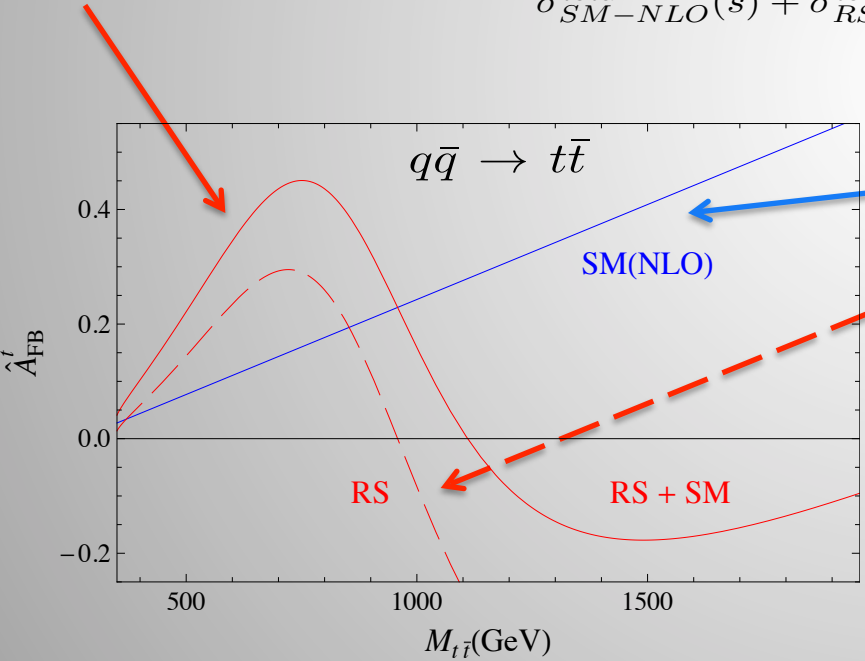


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$$\simeq \hat{A}_{\text{FB}}^{\text{LO}}(\hat{s}) + \hat{A}_{\text{FB}}^{\text{SM-NLO}}(\hat{s})$$

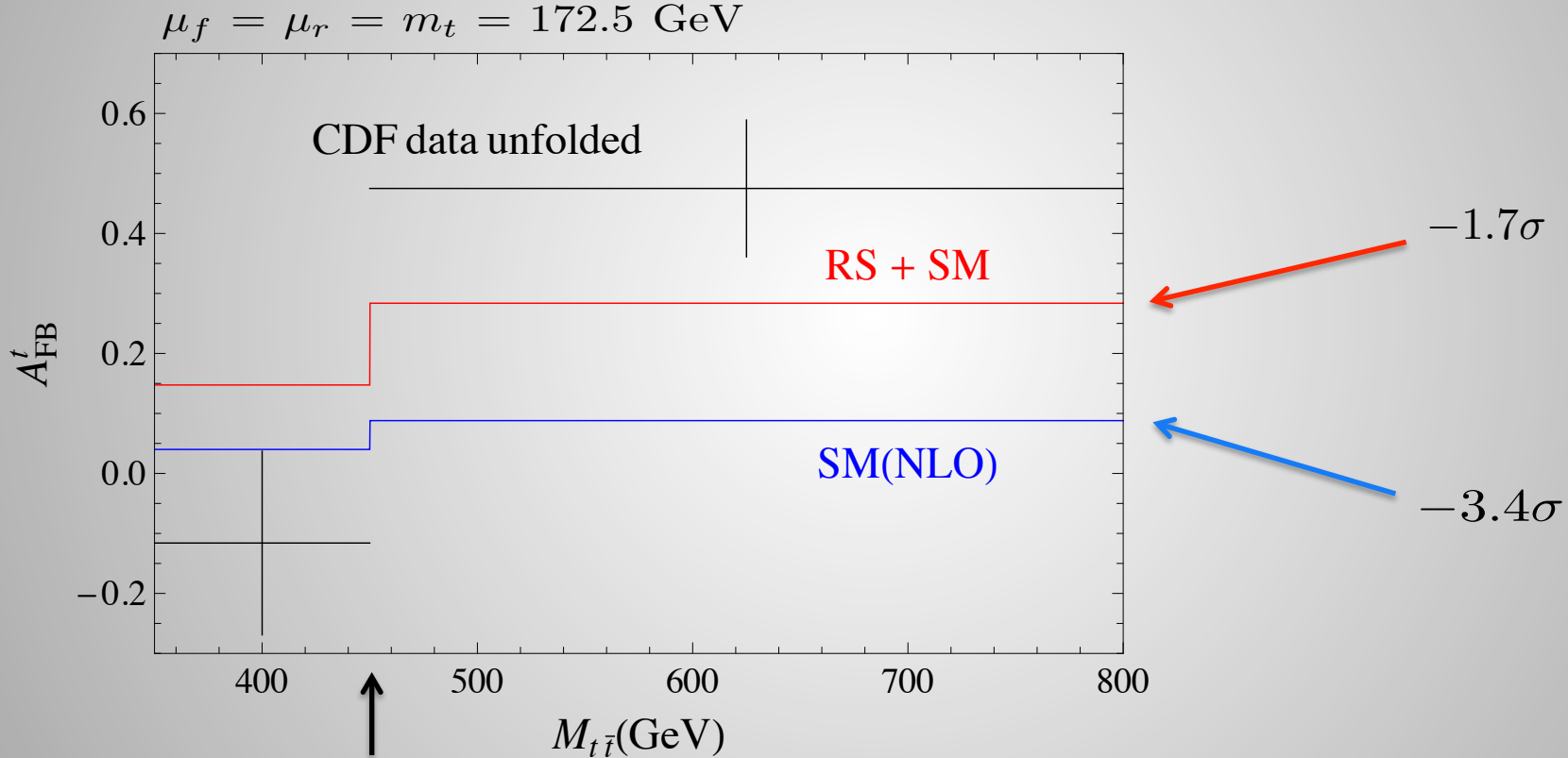
For our parameters such that:  
 $a_q a_t = -1.4 \quad v_q v_t = 0.7$

⇒ Positive  $A_{\text{FB}}^{\text{LO}}$  in RS at low  $M_{t\bar{t}}$   
 as wanted !



Full asymmetry after convolution with MSTW-2008...

(  $t\bar{t}$  rest frame )



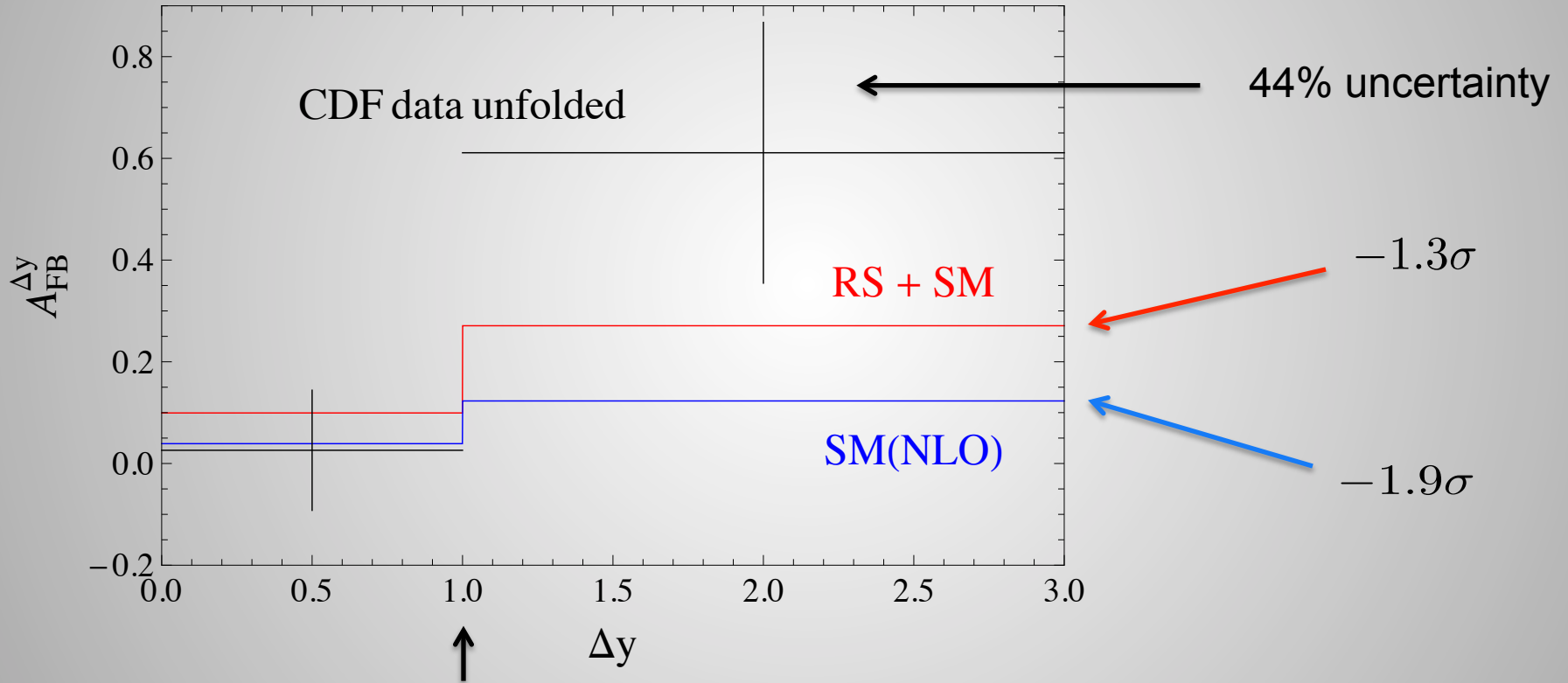
$M_{t\bar{t}} = 450 \text{ GeV}$

rest of the discrepancy : RS @ NLO ?

# Full asymmetry as a function of rapidity...

(  $t\bar{t}$  rest frame )

$$\mu_f = \mu_r = m_t = 172.5 \text{ GeV}$$

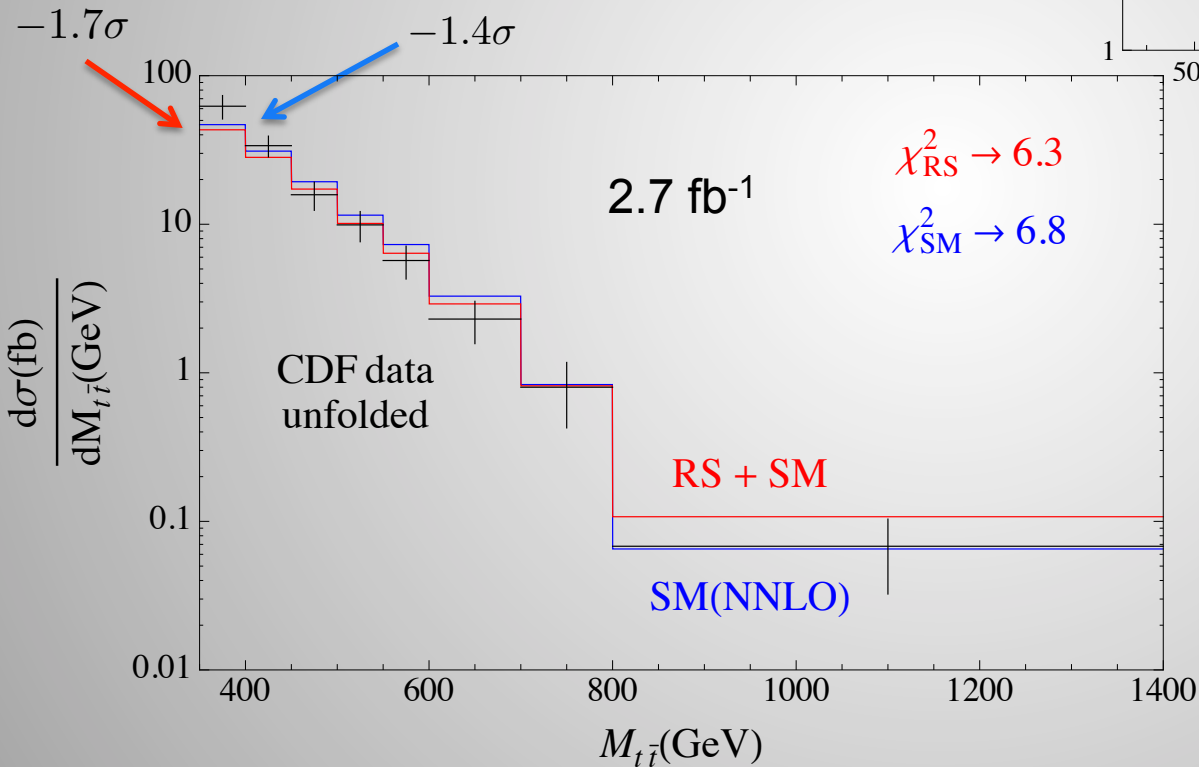
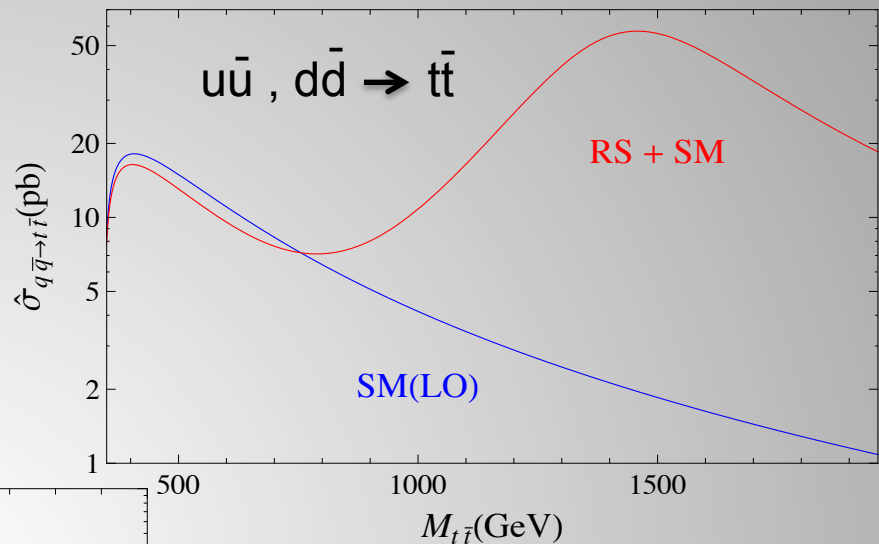


$\Delta y = 1$

additional positive test of the model

One must take care of the differential  $t\bar{t}$  production cross section in good agreement with the SM...

$$\frac{d\sigma_{SM-NNLO}}{dM_{t\bar{t}}} \left( 1 + \frac{d\sigma_{RS+inter.-LO}}{dM_{t\bar{t}}} / \frac{d\sigma_{SM.-LO}}{dM_{t\bar{t}}} \right)$$



In SM :

$$\chi_{SM}^2 / d.o.f. = 6.8 / 8$$


In RS :

$$\chi_{RS}^2 / d.o.f. = 6.3 / 8$$

$$m_t = 175 \text{ GeV}$$

$$\mu_f = \mu_r = m_t$$

# What about the **whole** integrated top quark **asymmetry** and **cross section** ?

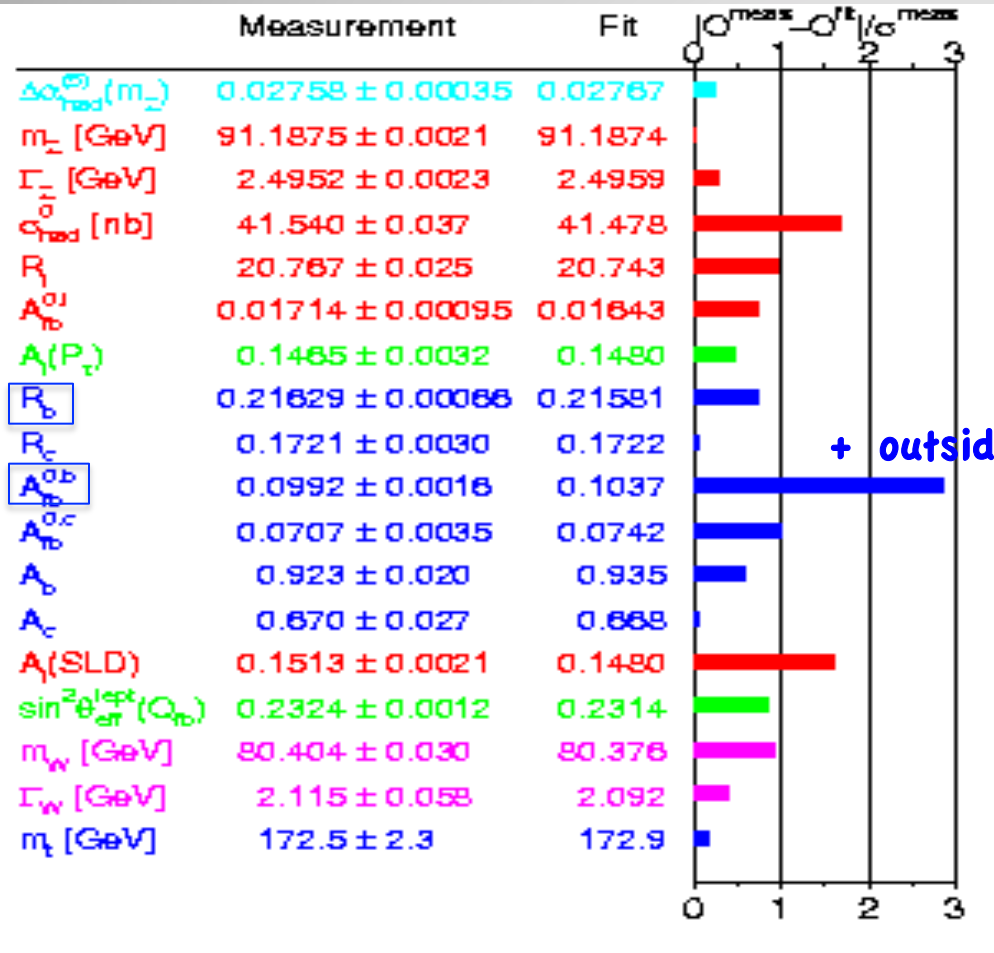
☺ **Tevatron data** [5] :  $0.158 \pm 0.075$  [5] CDF Collaboration  
SM [NLO] [5] :  $0.058 \pm 0.009 (-1.33\sigma)$  arXiv:1101.0034  
RS+SM :  $0.189 \pm 0.010 (+0.42\sigma)$   improves

☺ Theoretical (HATHOR):  $\sigma(p\bar{p} \rightarrow t\bar{t}) = 6.62 \pm 1 \text{ pb}$   
 $\mu_R = \mu_F = m_t = 172.5 \text{ GeV}$   
MSTW PDF NNLO

Experimental (Tevatron):  $7.50 \pm 0.48 \text{ pb}$  CDF Collaboration, Note 9913,  
Run II, October 2009.

 OK as heavy KK gluon with broad resonance

# III) $A_{FB}^b$ and EW precision tests @ LEP



$A_{FB}^b$  : a NP effect in the b sector ?

$$A_{FB}^b(p\hat{o}le) \equiv \frac{\int_0^{+1} \sigma_{\theta} d \cos \theta - \int_{-1}^0 \sigma_{\theta} d \cos \theta}{\sigma_0(e^+e^- \rightarrow \gamma / Z \rightarrow b\bar{b})}$$

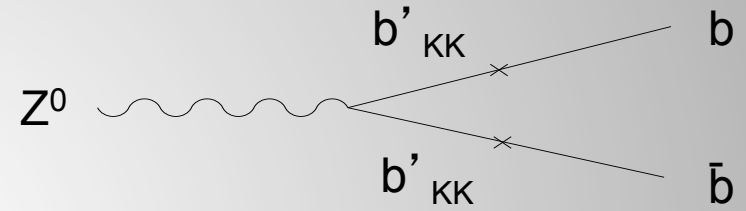
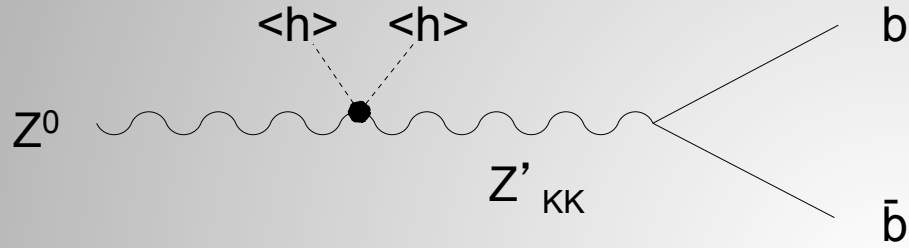
$$= \frac{3(Q_Z^{eL})^2 - (Q_Z^{eR})^2}{4(Q_Z^{eL})^2 + (Q_Z^{eR})^2} \frac{(Q_Z^{bL})^2 - (Q_Z^{bR})^2}{(Q_Z^{bL})^2 + (Q_Z^{bR})^2}$$

+ outside Z pôle !

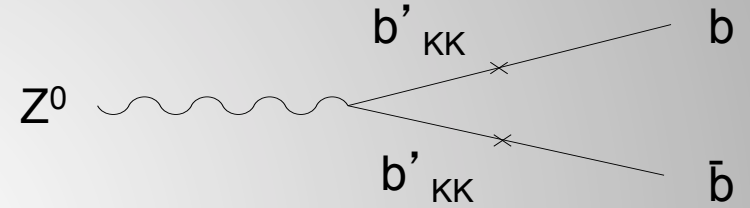
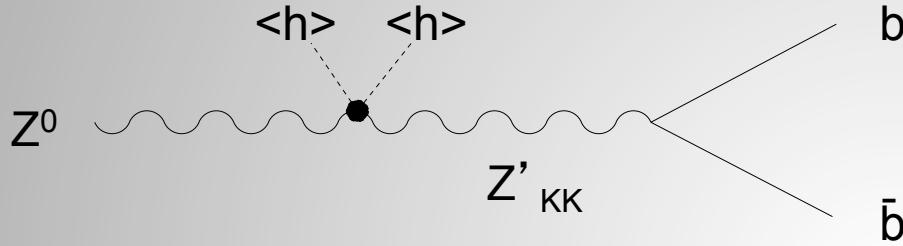
$$R_b \equiv \frac{\Gamma(Z \rightarrow b\bar{b})}{\Gamma(Z \rightarrow \text{hadrons})}$$

$$= \frac{(Q_Z^{bL})^2 + (Q_Z^{bR})^2}{\sum_{q \neq t} [(Q_Z^{qL})^2 + (Q_Z^{qR})^2]}$$

*Interpretation in a generic extra-dimensional model...*  
**(difficult in SUSY)**



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**(difficult in SUSY)**



$$\left| \delta Q_Z^{f_l} \right| \approx 1\%_{00} \ll \left| \delta Q_Z^{b_{L/R}} \right| \approx |-1.5/30\%|$$

$$m_{b'}(c_{t_R}) \ll m_{f'}(c_{\text{light}})$$

$$\text{Coupling } Z_{KK} f_l \bar{f}_l \ll \text{Coupling } Z_{KK} b \bar{b}$$

$$m_t(c_{t_R}) \uparrow \Rightarrow m_{b'}(c_{t_R}) \downarrow$$



**'natural' conditions within the RS model**

# Summary of the EW observables...

Observable	SM	RS
$A_{FB}^b(m_Z)$	$2.7\sigma$	$1.2\sigma$
$R_b$	$0.8\sigma$	$1.2\sigma$
$A_{FB}^c(m_Z)$	$0.9\sigma$	$0.9\sigma$
$R_c$	$0.0\sigma$	$0.5\sigma$
$A_{FB}^s(m_Z)$	$0.6\sigma$	$0.2\sigma$
$\Gamma_{\text{had}}(Z)$	$1.3\sigma$	$1.0\sigma$
$\Gamma_{\text{tot}}(W)$	$0.2\sigma$	$0.2\sigma$
$\langle Q_{FB} \rangle$	$1.1\sigma$	$0.1\sigma$
$C_{1u} + C_{1d}$	$0.2\sigma$	$0.8\sigma$
$C_{1u} - C_{1d}$	$1.1\sigma$	$0.1\sigma$
$\chi^2/d.o.f.$	25.3/17	19.8/17

no more  $A_{FB}^b$  anomaly  
at the  $Z^0$  pole

still fits well

whole fit improved


+ Zuu/Zdd OK from  
Tevatron Run I & II  
& HERA (H1,ZEUS)



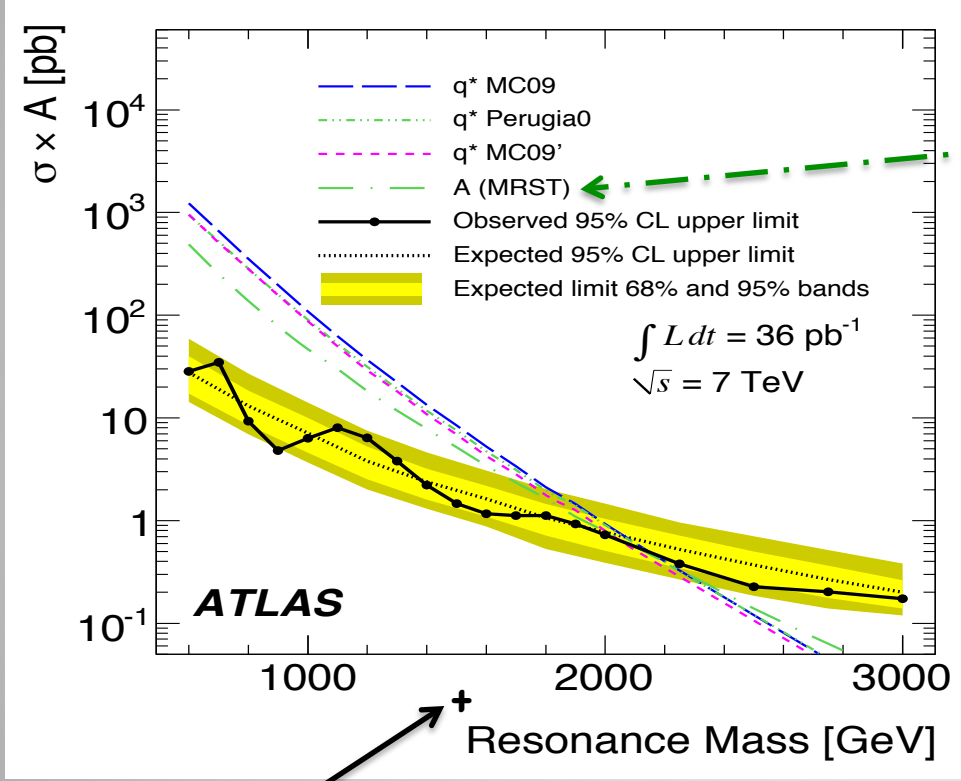
## IV) Constraints and predictions @ LHC

### Comparison of the $t\bar{t}$ cross section $\sigma_{t\bar{t}}$

in RS+SM	NNLO (HATHOR)	$\mu_F = \mu_R = m_t = 173 \text{ GeV}$	$\sqrt{s} = 7 \text{ TeV}$ $\mathcal{L} = 35 \text{ pb}^{-1}$
$\sigma(pp \rightarrow t\bar{t})$ SM	at $-0.86\sigma$ at $-0.81\sigma$	from the ATLAS measurement, $180 \pm 18.5 \text{ pb}$	
$\sigma(pp \rightarrow t\bar{t})$ SM	at $+0.36\sigma$ at $+0.31\sigma$	from the CMS measurement, $158 \pm 19 \text{ pb}$	

 OK as major contribution from the gg initial state

# Constraints from dijets



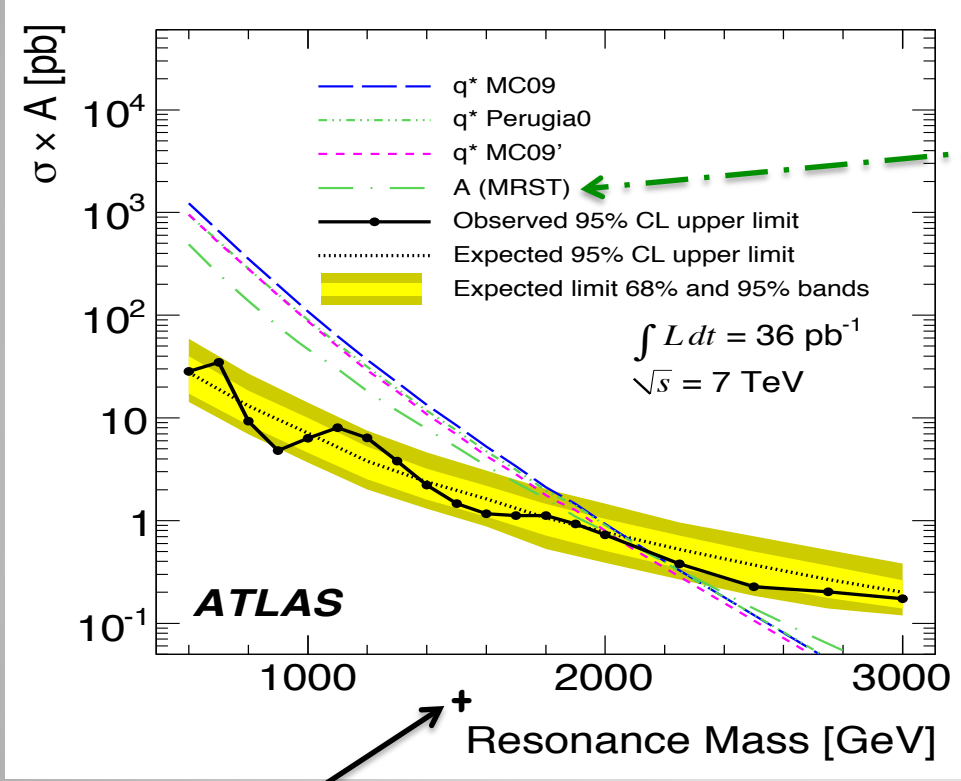
Axiguon -  $SU(3)_L \times SU(3)_R$

*Frampton et al. (1987)*  
*Bagger et al. (1987)*

- ★ now including the width effect between  $0.7 M_{KK}$  and  $1.3 M_{KK}$
- ★ we have also checked the angular distribution constraints

we've computed the ratio  $RS/Axiguon$   
 $\Rightarrow KK$  gluon exchange @ 0.023 pb

# Constraints from dijets



Axigluon -  $SU(3)_L \times SU(3)_R$

*Frampton et al. (1987)*  
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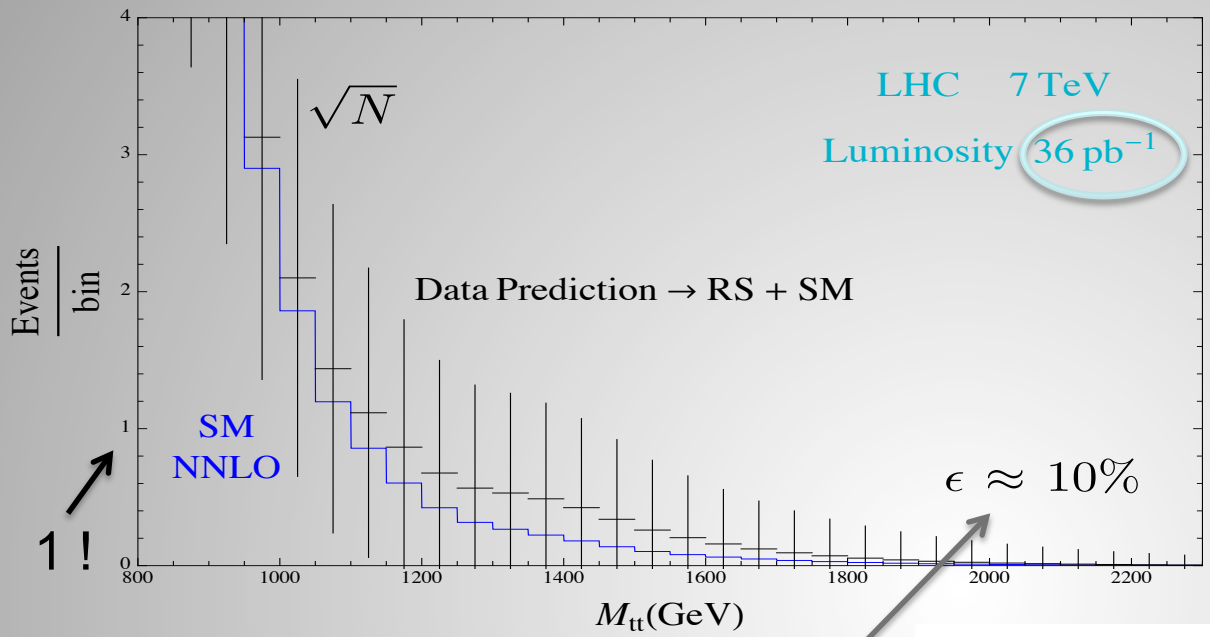
Coupling  $g^{(1)tt} > g^{(1)qq}$



RS addresses  $A_{FB}^t$   
 + passes dijet bounds

we've computed the ratio RS/Axigluon  
 => KK gluon exchange @ 0.023 pb

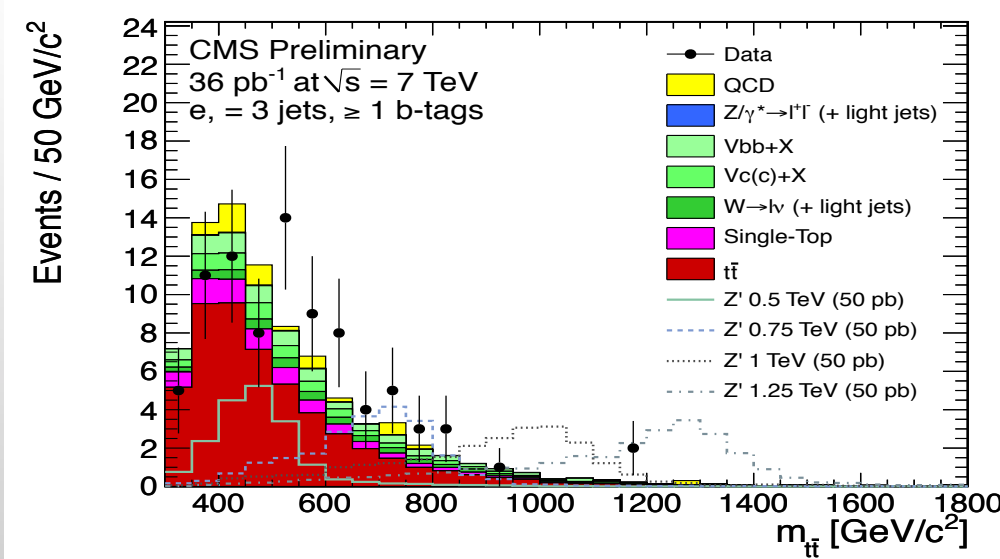
**Predictions on the  $M_{tt}$  distribution at LHC**



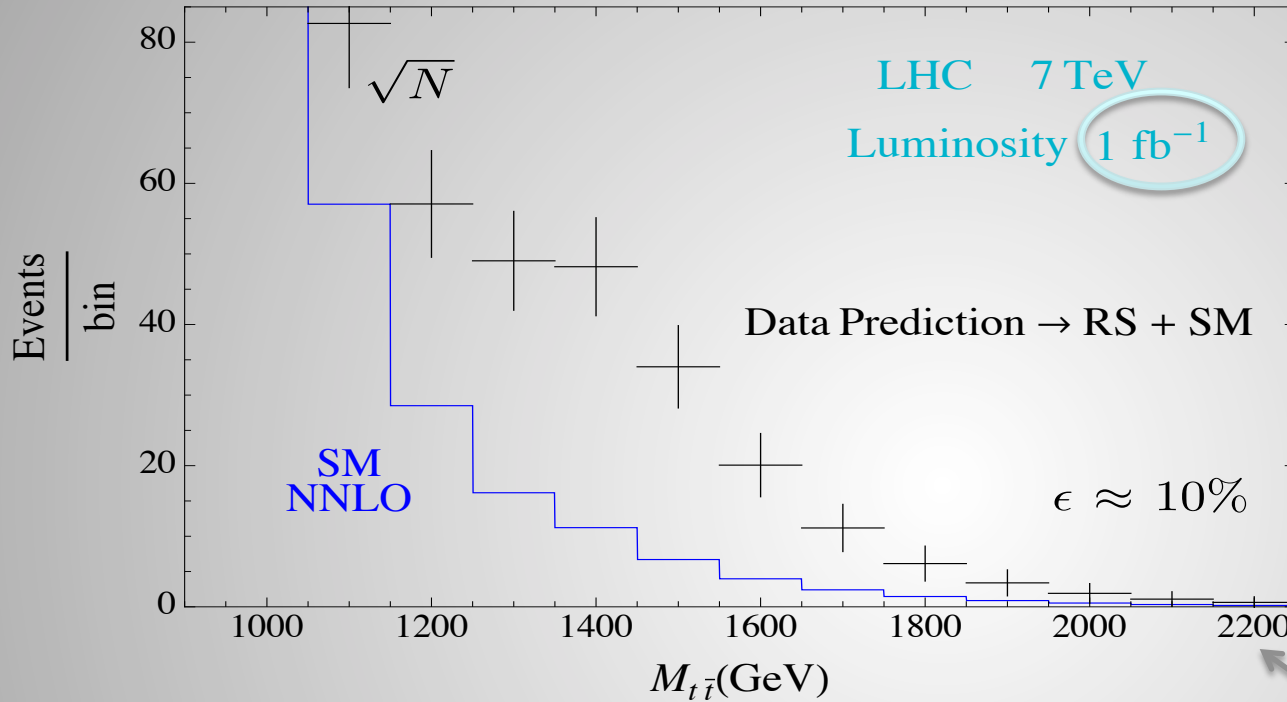
compatible

$t\bar{t}$  reconstruction efficiency taken

$$\mu_f = \mu_r = m_t = 173 \text{ GeV}$$



What does the RS model predicts at the expected luminosity of  $1 \text{ fb}^{-1}$  ?



..a KK gluon resonance

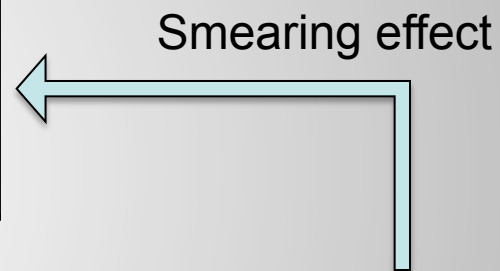
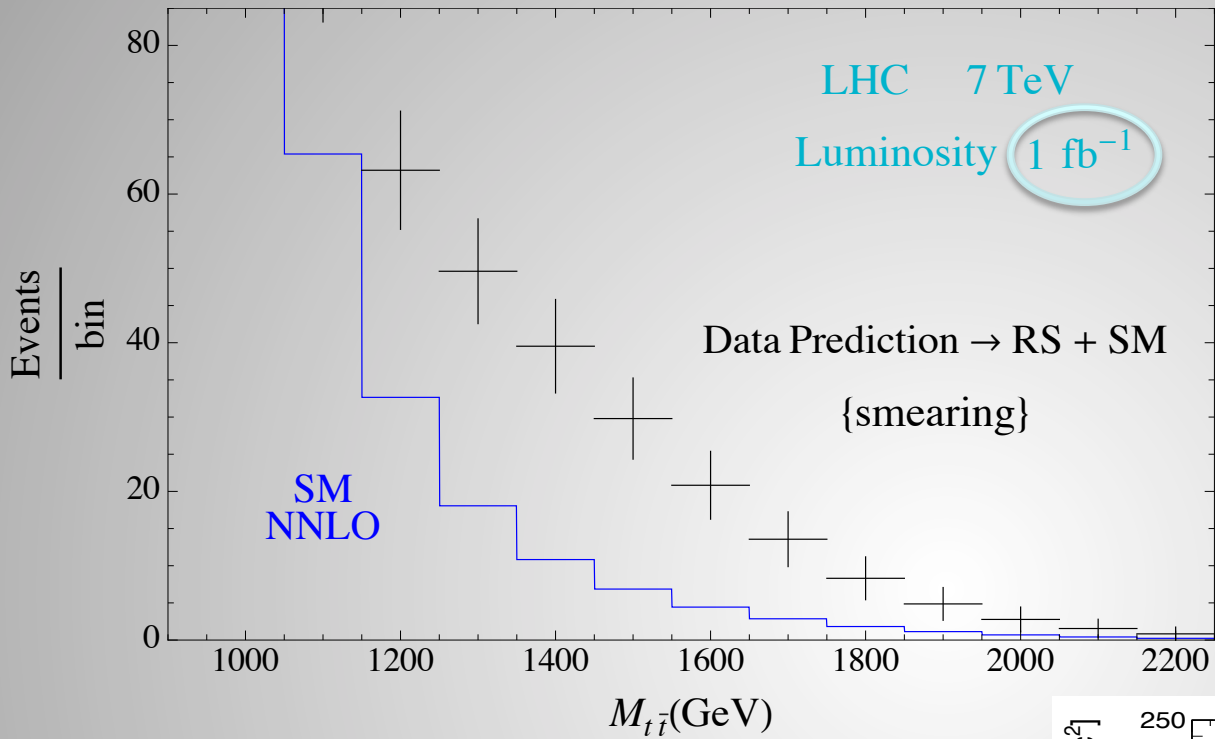
$$\Gamma_{g^{(1)}} \simeq 40\% M_{KK}$$

assuming 100 GeV bin resolutions

integration of the cross section e.g. over  $[1050, 1750]$  GeV

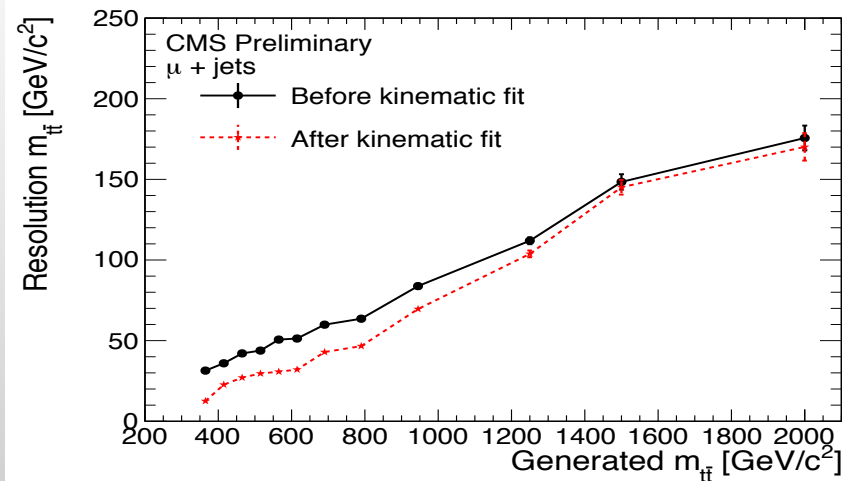
$$\text{Signal} / \sqrt{\text{Background}} \simeq 13.9$$

**An excess should be clearly visible.**



$$\text{Signal} / \sqrt{\text{Background}} \cong 12.7$$

**A great excess even simulating the  $M_{t\bar{t}}$  experimental resolution:**



# V) Other scenarios for $A_{FB}^t$ ?

Aguilar-S. et al. (2011)  
Delaunay et al. (2011)  
Degrande et al. (2011)

➔ Messages from the effective operator approach...  
(trying to fit  $A_{FB}^t$  and  $\sigma_{t\bar{t}}$  )

Extra scalar field – color octet [t-channel] : impossible

‘ ‘ – color triplet [t-channel] : possible (diquark FC couplings)

Shu et al. (2010), ...

‘ ‘ – color singlet [s- & t-channel] : difficult

Giudice et al. (2011)

Extra vector boson – color octet [s-channel] : possible (Axigluon/KK gluon)

‘ ‘ – color singlet [s- & t-channel] :

tensions as no  $Z', W'$  interferences with the SM contributions (QCD@LO)

Possibility: t-chan. exchange of a non-abelian  $Z'$  (with  $Z'_R t_R$  couplings)

Jung et al. (2011)

## VI) Conclusions

- ☀ The ‘warped paradigm’, with theoretical motivations, predicts deviations from SM in the 3<sup>rd</sup> generation sector =>  $A_{FB}^b, A_{FB}^t = \text{early indications ?}$
- ☀ We suggest a geometrical RS realization addressing both  $A_{FB}^b$  and  $A_{FB}^t$ .
- ☀ The several constraints on the parameter space render this RS scenario quite **predictive on the effects in the  $t\bar{t}$  invariant mass distribution @ LHC.**
- ☀ One must wait for more data (Tevatron, LHC) in order to discriminate between the main  $A_{FB}^t$  interpretations: Z/W’, KK gluon, Axigluon, stop...
- ☀ This RS model addressing  $A_{FB}^b, A_{FB}^t$  predicts a **KK gluon resonance**  
 $\neq$   
Other RS models usually with light **custodians copiously producible**  
( ‘no-lose signal’ theorem in warped pheno. @ LHC )



Back up

Some useful formula's...

$$\cos \theta_t^* = \sqrt{1 + \frac{4m_t^2}{\hat{s} - 4m_t^2}} \tanh y_t$$

$$\frac{1}{\mathcal{D}} = \hat{s} - M_{KK}^2 + i \frac{\hat{s}}{M_{KK}^2} \sum_q \Gamma_{KK}^{g(1) \rightarrow q\bar{q}} M_{KK} \frac{\beta_q [v_q^2 (3 - \beta_q^2)]/2 + a_q^2 \beta_q^2}{v_q^2 + a_q^2}$$

$$\beta_t = \sqrt{1 - 4m_t^2/\hat{s}}$$

$$\sqrt{\hat{s}_0} \simeq \frac{M_{KK}}{(1 + \Gamma_{KK}^2/M_{KK}^2)^{1/4}}$$

$$\frac{d\hat{\sigma}_{RS-LO}}{d \cos \theta_t^*}(\hat{s}) = \frac{\pi \alpha_s^2(\mu_r) \beta_t}{9\hat{s}} \times$$

$$\hat{s}^2 |\mathcal{D}|^2 \left[ 8v_q v_t a_q a_t \beta_t \cos \theta^* + (a_q^2 + v_q^2) (v_t^2 (2 - \beta_t^2 \sin^2 \theta^*) + a_t^2 \beta_t^2 (1 + \cos^2 \theta^*)) \right]$$

$$\frac{d\hat{\sigma}_{inter.-LO}}{d \cos \theta_t^*}(\hat{s}) = \frac{\pi \alpha_s^2(\mu_r) \beta_t}{9\hat{s}} 4\hat{s} \text{Re}(\mathcal{D}) \left[ v_q v_t \left( 1 - \frac{1}{2} \beta_t^2 \sin^2 \theta^* \right) + a_q a_t \beta_t \cos \theta^* \right]$$

$$\left( \frac{d\hat{\sigma}_{SM-LO}}{d \cos \theta_t^*}(\hat{s}) \Big|_{q\bar{q}} = \frac{\pi \alpha_s^2(\mu_r) \beta_t}{9\hat{s}} \left\{ 2 - \beta_t^2 \sin^2 \theta^* \right\} \right)$$

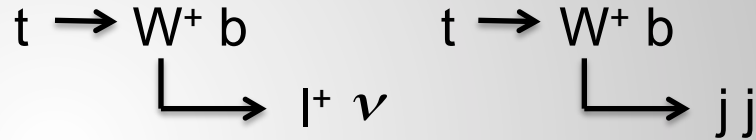
« How is  $A_{\text{FB}}^t$  measured at Tevatron in lepton+jet channels ? »

$$\Delta y = y_t - y_{\bar{t}} \quad y_t = (y_t - y_{\bar{t}})/2$$

$$\Delta y = q(y_l - y_h) = q\Delta y_{lh}$$



in the laboratory frame

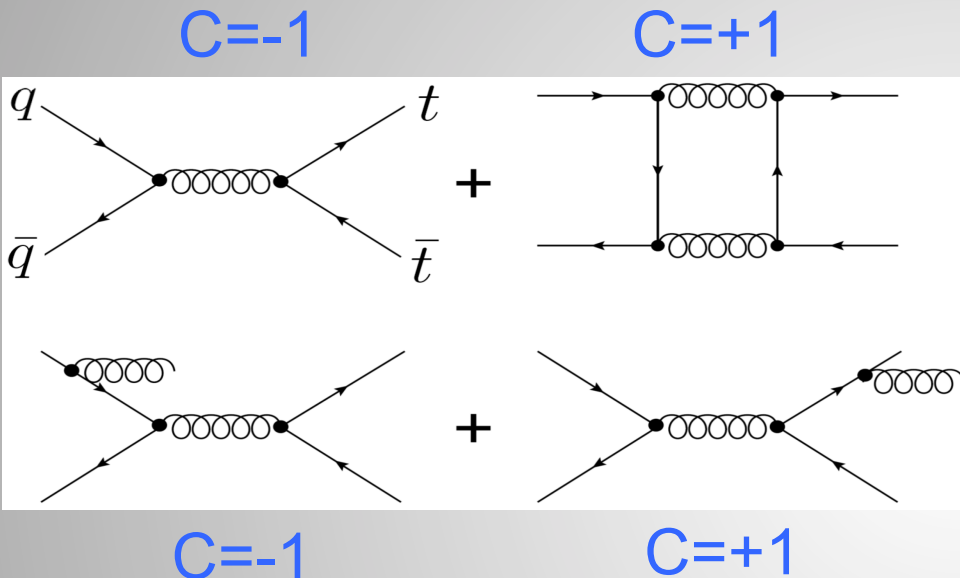


$$A_{\text{FB}}^t = \frac{N(\Delta y > 0) - N(\Delta y < 0)}{N(\Delta y > 0) + N(\Delta y < 0)} = \frac{N(q\Delta y_{lh} > 0) - N(q\Delta y_{lh} < 0)}{N(q\Delta y_{lh} > 0) + N(q\Delta y_{lh} < 0)}$$

Other asymmetries...

$$A_{\text{FB}}^{p\bar{p}} = \frac{\sigma[y_t^{p\bar{p}} > 0] - \sigma[y_t^{p\bar{p}} < 0]}{\sigma[y_t^{p\bar{p}} > 0] + \sigma[y_t^{p\bar{p}} < 0]} \quad A_C^t = \frac{\sigma_t[y_t > 0] - \sigma_{\bar{t}}[y_t > 0]}{\sigma_t[y_t > 0] + \sigma_{\bar{t}}[y_t > 0]} \quad A_C^t = A_{\text{FB}}^t \Rightarrow CP$$

## Standard Model (QCD) contribution to $A_{FB}^t$



$$A_{FB}^{SM} = \frac{\sigma_{SM-NLO}^F - \sigma_{SM-NLO}^B}{\sigma_{SM-NLO}^F + \sigma_{SM-NLO}^B}$$

(vanishing at LO)

MCFM for SM ( $m_t=172.5\text{GeV}$ , PDF=CTEQ) @ NLO :  $A_{FB}^t = 0.058 \pm 0.009$


Ahrens et al. (2010) obtain ( $m_t=173.1\text{GeV}$ , PDF=MSTW) :

@ NLO :  $A_{FB}^t = 0.067^{+0.006}_{-0.004}$       @ NNLO-approx :  $A_{FB}^t = 0.064^{+0.009}_{-0.007}$   $0.2 < \mu_f / \text{TeV} < 0.8$

=>  $A_{FB}^t [M_{tt} > 450\text{GeV}]$  anomaly probably not fully explained by QCD errors  $\sim 0.01$

## Measurements of $A_{FB}^t$ at Tevatron

*now 5.1fb<sup>-1</sup>: see F.Badaud's talk*

**07-2010** D0 in the lepton+jets channel with **(0.9fb<sup>-1</sup> then) 4.3fb<sup>-1</sup>**   
(*ttbar frame, not unfolded = no subtracting bckgrd & effic. + no ttbar level*) :  
 $A_{FB}^t = 0.08 \pm 0.04 \pm 0.01$  (**+1.7 sigma** from SM prediction)

**03-2009** CDF in the lepton+jets channel with **(1.9fb<sup>-1</sup> then) 3.1fb<sup>-1</sup>**  
(*lab frame, unfolded*) :  
 $A_{FB}^t = 0.193 \pm 0.065 \pm 0.024$  (**+2.1 sigma** from SM prediction)

**01-2011** CDF in the dilepton channel with **5.1fb<sup>-1</sup>**  
(*lab frame, unfolded*) :  
 $A_{FB}^t = 0.42 \pm 0.15 \pm 0.05$  (+2.3 sigma from SM prediction)  
(large error => +1.7 sigma from lept.+jets channel)

(*lab frame, not unfolded*) :  
 $A_{FB}^t (M_{tt} < 450 \text{ GeV}) = 0.104 \pm 0.066$  (+1.6 sigma from SM prediction)  
 $A_{FB}^t (M_{tt} > 450 \text{ GeV}) = 0.212 \pm 0.096$  (**+2.6 sigma** from SM prediction)

The way to compute it...

$$A_{\text{FB}}^t = \frac{(\sigma_{SM}^F + \sigma_{RS}^F + \sigma_{inter.}^F) - (\sigma_{SM}^B + \sigma_{RS}^B + \sigma_{inter.}^B)}{(\sigma_{SM}^F + \sigma_{RS}^F + \sigma_{inter.}^F) + (\sigma_{SM}^B + \sigma_{RS}^B + \sigma_{inter.}^B)}$$

$$\Leftrightarrow A_{\text{FB}}^t = A_{\text{FB}}^{RS} \times R + A_{\text{FB}}^{SM} \times (1 - R)$$

Cao et al. (2010)

with

$$A_{\text{FB}}^{RS} = \frac{(\sigma_{RS-LO}^F + \sigma_{inter.-LO}^F) - (\sigma_{RS-LO}^B + \sigma_{inter.-LO}^B)}{(\sigma_{RS-LO}^F + \sigma_{inter.-LO}^F) + (\sigma_{RS-LO}^B + \sigma_{inter.-LO}^B)}$$

$$R = \frac{\sigma_{RS-LO}^{\text{total}} + \sigma_{inter.-LO}^{\text{total}}}{\sigma_{SM-LO}^{\text{total}} + \sigma_{RS-LO}^{\text{total}} + \sigma_{inter.-LO}^{\text{total}}}$$

ex:  $\sigma_{RS-LO}^F = \sigma_{RS-LO}[\cos \theta_t^* : 0 \rightarrow 1] =$

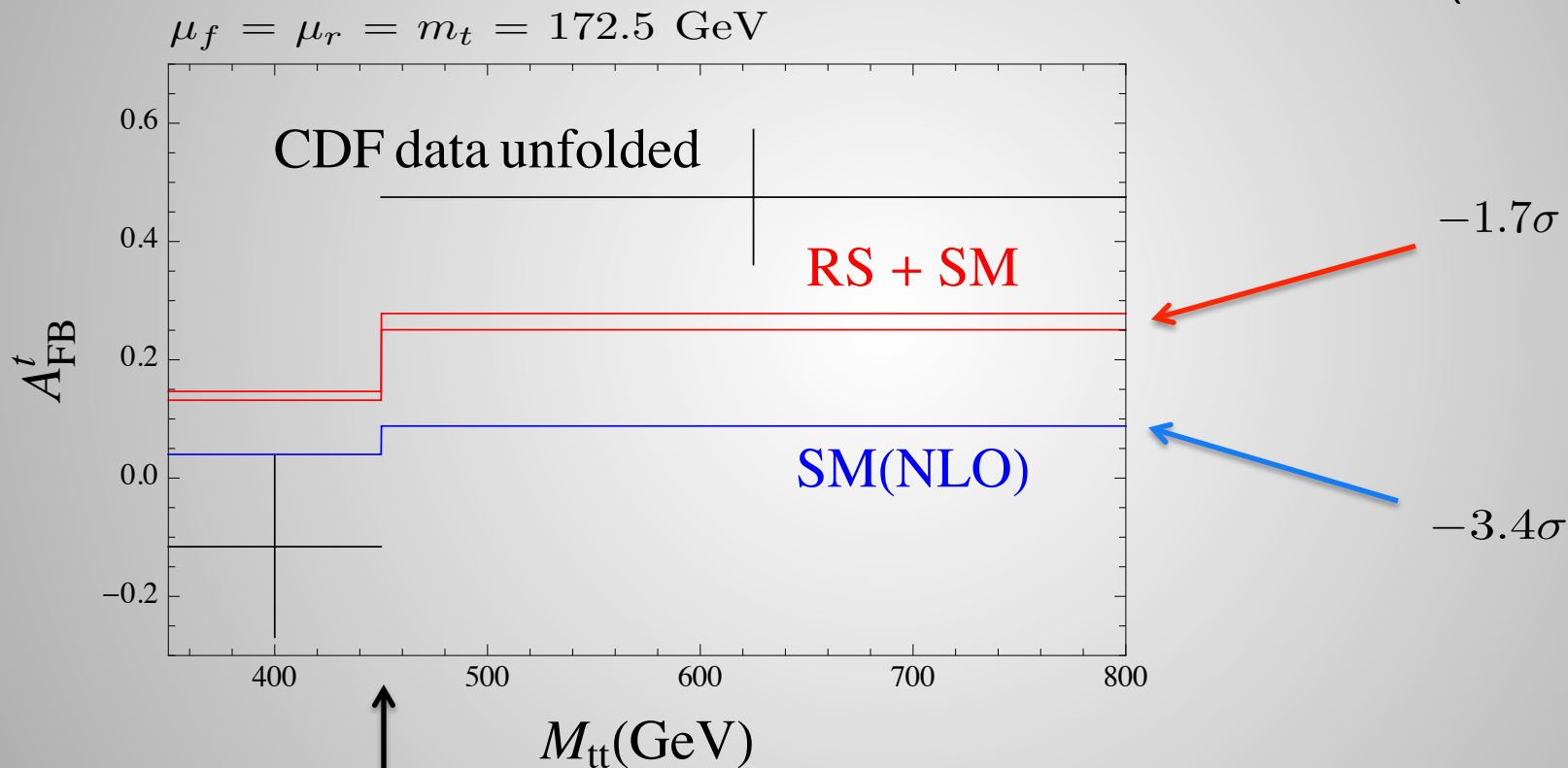
$$\sum_{ij} \int_{\tau_{min}}^{\tau_{max}} d\tau \left[ \int_0^1 d \cos \theta_t^* \left( \frac{d\hat{\sigma}_{RS-LO}}{d \cos \theta_t^*}(\tau s) \right)_{ij} \right] \left\{ \int_{\tau}^1 \frac{dx}{x} f_i(x, \mu_f) f_j\left(\frac{\tau}{x}, \mu_f\right) \right\}$$

$$\tau_{min/max} = \hat{s}_{min/max}/s$$

MSTW-2008-NLO

Looking at the effect of MSTW uncertainties [*@ 90% C.L.*]...

(*ttbar* frame)



$M_{\text{tt}} = 450 \text{ GeV}$

no significant dependence as well on  $\mu_f, \mu_r$  and  $m_t$



$$1/(t - M_{KK}^2) \quad -t \leq M_{KK}^2 \quad t = -M_{jj}^2/2 \quad M_{jj} = \sqrt{2}M_{KK} \sim 2 \text{ TeV}$$

$$\cos \theta^* = 0$$

KK gluon produces less than 10% deviation

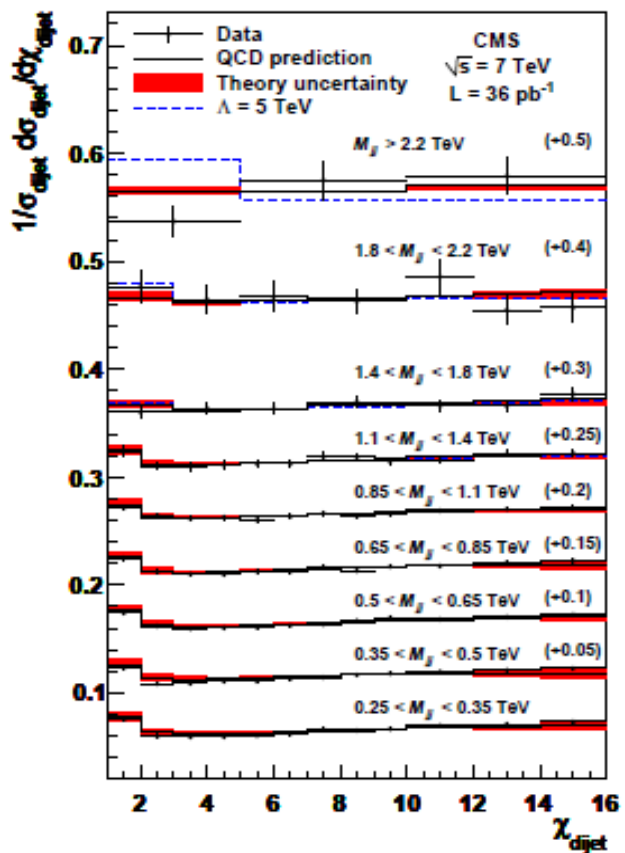
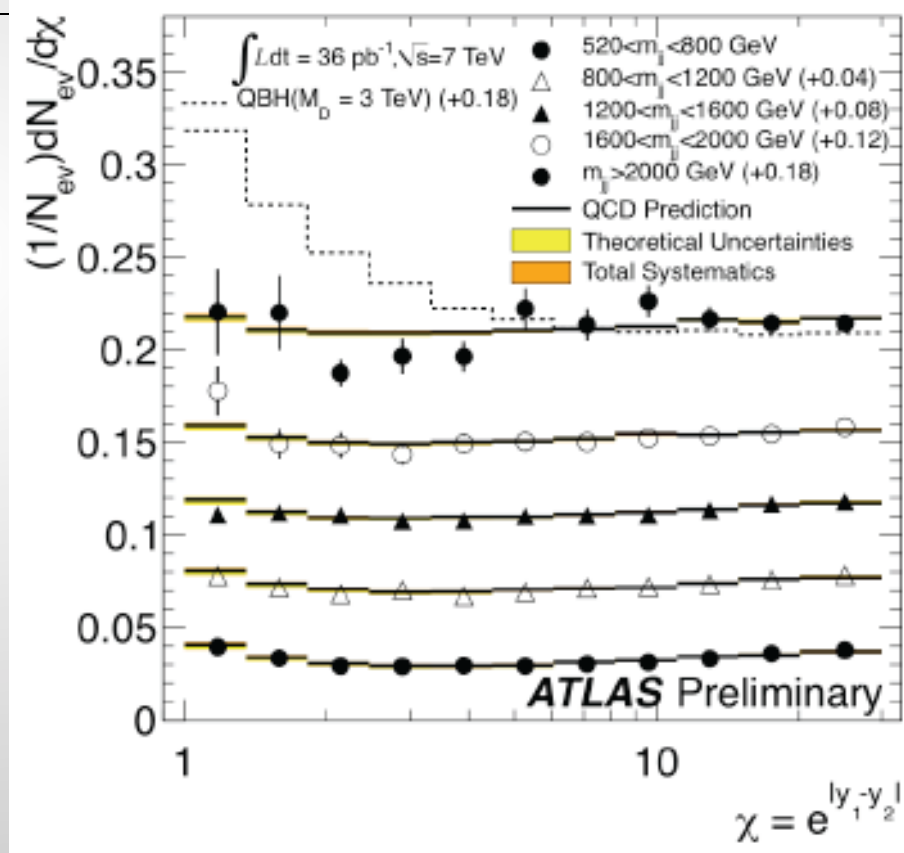
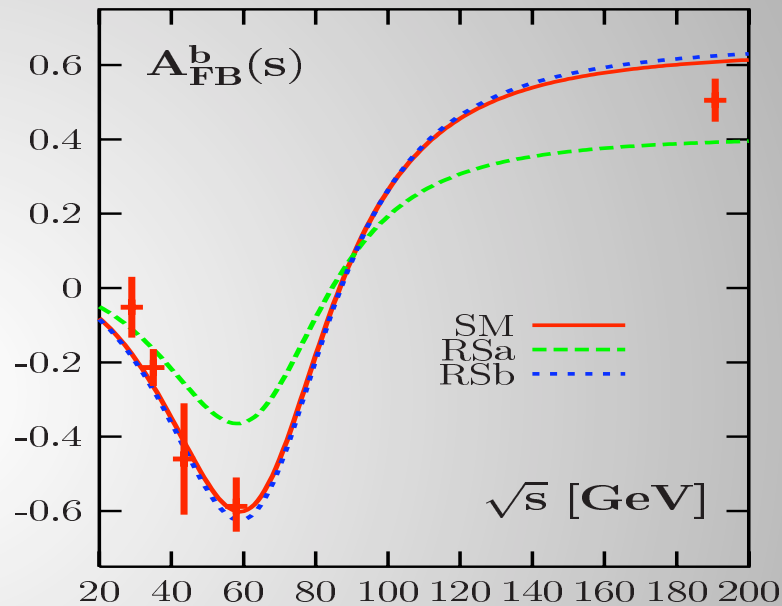
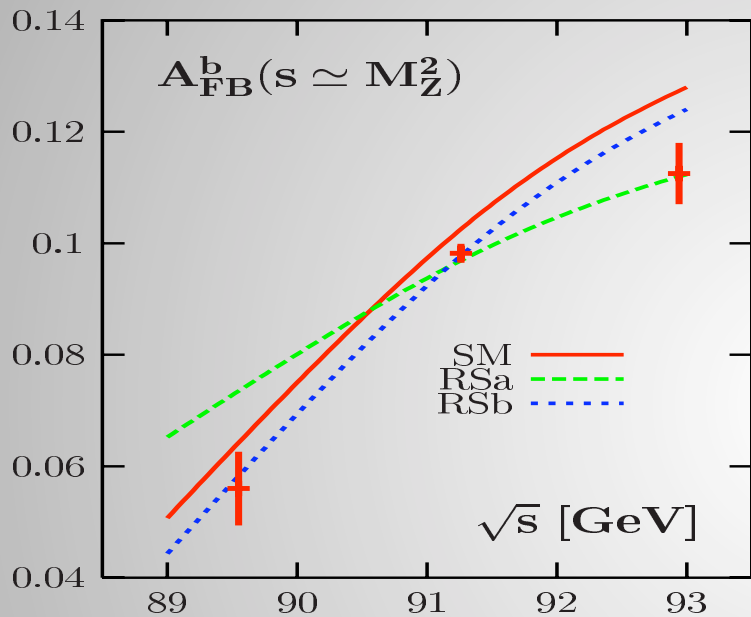


Figure 1: Normalized dijet angular distributions in several  $M_{jj}$  ranges, shifted vertically by the additive amounts given in parentheses in the figure for clarity. The data points include statistical and systematic uncertainties. The results are compared with the predictions of pQCD at NLO (solid histogram) and with the predictions including a contact interaction term of compositeness scale  $\Lambda = 5 \text{ TeV}$  (dashed histogram). The shaded band shows the effect on the NLO pQCD predictions due to  $\mu_r$  and  $\mu_f$  scale variations and PDF uncertainties, as well as the uncertainties from the non-perturbative corrections added in quadrature.



$$\chi = e^{\frac{|y_1 - y_2|}{2}}$$

## Global $A_{\text{FB}}^b$ fit @ and off the Z pôle :



SM :  $\chi^2 = 24$     RSa :  $\chi^2 = 20$     RSb :  $\chi^2 = 14$

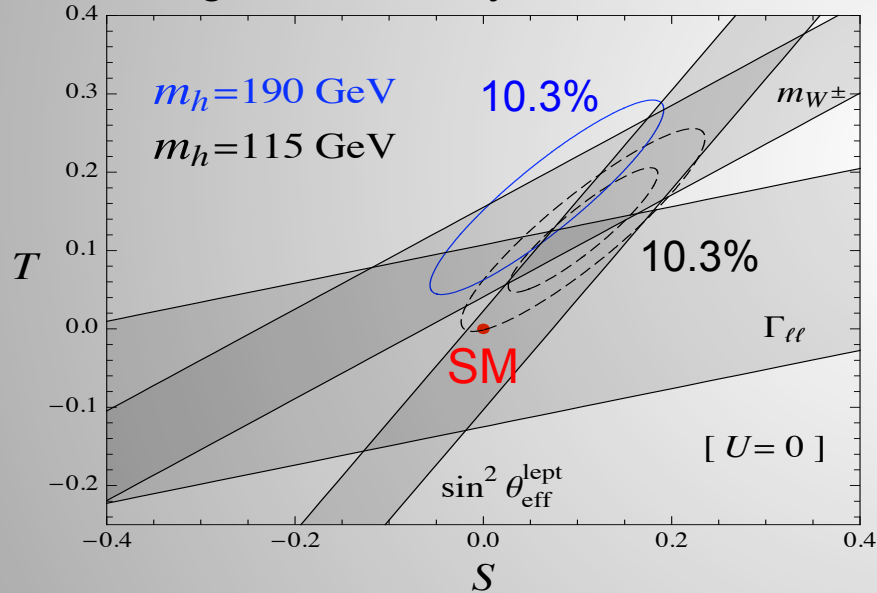
$b_R$  under  $SU(2)_L \times SU(2)_R \times U(1)_X$  :

$$\begin{cases} Q_X = (B - L)/2 \Rightarrow I_R^3 = -1/2 & \text{RSa} \\ Q_X = -5/6 \Rightarrow I_R^3 = +1/2 & \text{RSb} \end{cases}$$

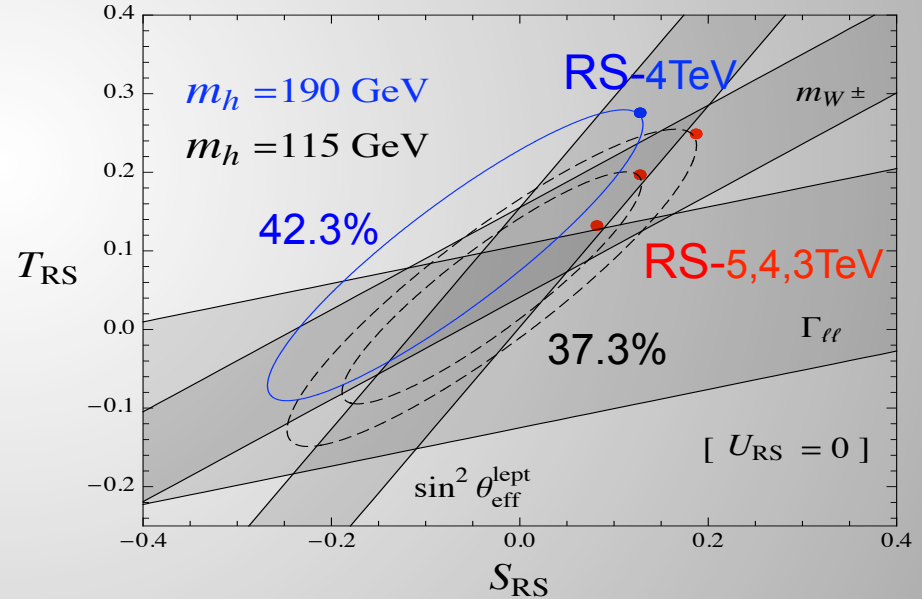
## Improved goodness-of-fit

EW observables are expressed in terms of oblique parameters encoding the New Physics...

$$S_{\text{RS}} \simeq 2\pi \left( \frac{2.4v}{M_{KK}} \right)^2 \quad T_{\text{RS}} \simeq k\pi^2 R_c \frac{\tilde{g}^2}{8e^2} \frac{\tilde{M}^2}{k^2} \left( \frac{2.4v}{M_{KK}} \right)^2$$



p-value 10.3%  $\Leftrightarrow \chi^2/11 = 1.56$

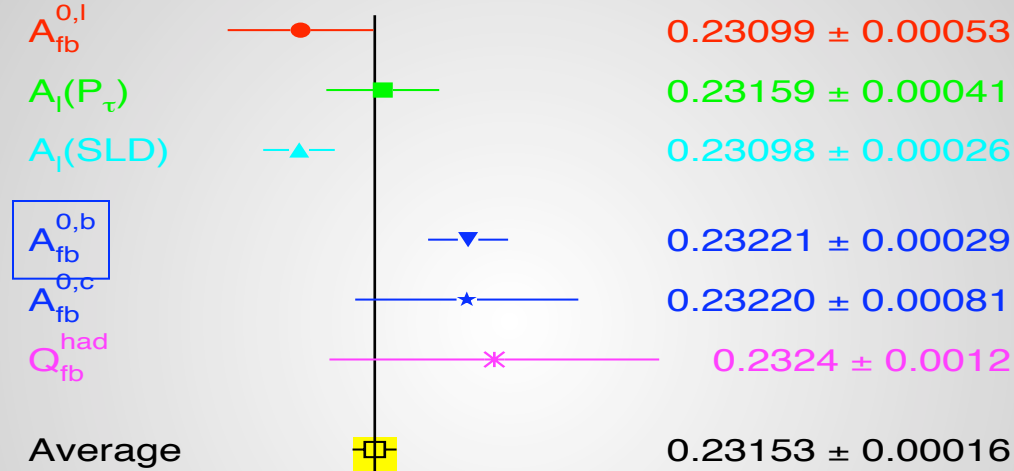


p-value 37.3%  $\Leftrightarrow \chi^2/10 = 1.08$

# Better quality of fit in RS than in SM cause..

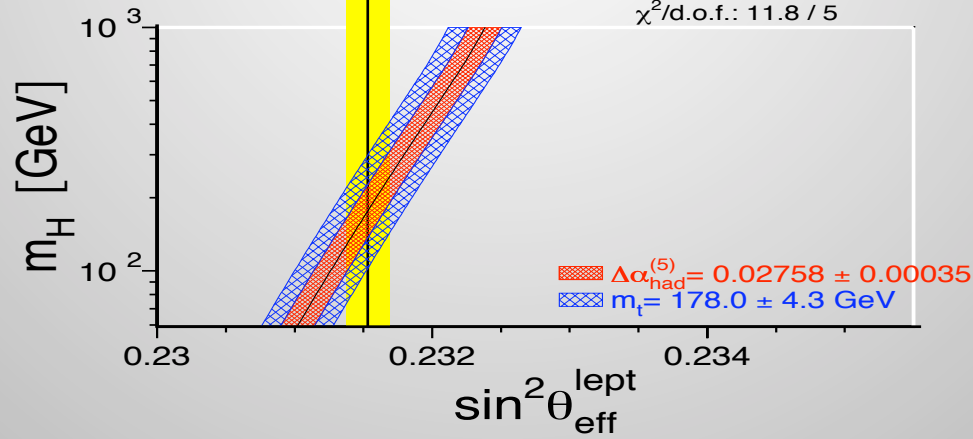
1) positive contribution  $T_{RS}$  (*custodial symmetry breaking*)

2) SM fit degraded by the  $\sin^2 \theta_W$  measurement derived *directly* from  $A_{FB}^b$  :



$\chi^2/d.o.f.: 11.8 / 5$

SM →



*AdS / CFT correspondance (98') :*

WARPED H-DIM. SCENARIOS / STRONGLY COUPLED MODELS

<b>5D holographic version</b>	<b>RS with bulk fields</b>	<b>gauge-Higgs unification</b>	<b>Higgsless models</b>
<b>4D dual interpretation</b>	<b>composite Higgs boson</b>	<b>composite Higgs pseudo-Goldstone boson of a global symmetry</b>  <i>(as for little Higgs with T parity)</i>	<b>technicolor models</b>