

# Mass Measurement at Colliders

Rakhi Mahbubani  
CERN

Rencontres de Blois 2012

May 29th 2012

# Mass Measurement with MET at Colliders

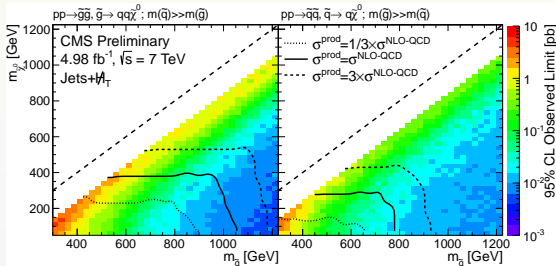
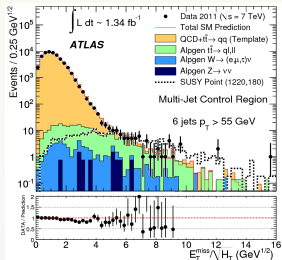
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# Parameters

## WHAT MET?

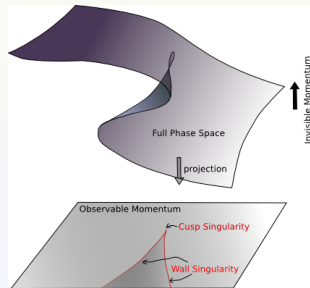
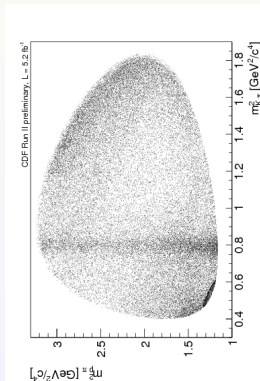
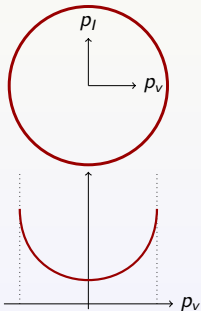


Natural theories with signatures involving large transverse momentum **not ruled out**. c.f. talks by Csaki, Weiler, ...

# Phase Space

$$\sigma(pp \rightarrow CD) = \sum_{a,b=q,g} \int f_a f_b \int_{\text{PS}} |M(ab \rightarrow CD)|^2$$

Phase space singularities = edges, endpoints, cusps, ...



Kim 0910.1149

# Mass Bound Variables

Barr et al 1105.2977

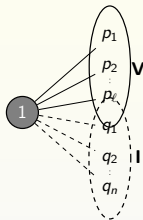
What is best bound for invariant mass of a group of  $N$  particles decaying to visibles + invisibles?

$$m_N(M_1, M_2, \dots, M_N) = \min_{q_T = p_T} [\max(M_1, M_2, \dots, M_N)] \leq \max(M_1, M_2, \dots, M_N)$$

$$M_a = \sum_{i=1}^{n_a} m_i$$

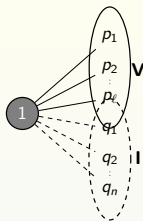
- Gives event-by-event lower bound on maximum parent mass
- Can saturate bound for correct input  $M$

# Transverse mass



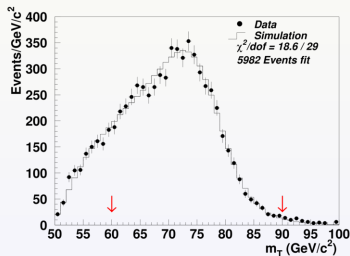
$$m_T(M) = m_V^2 + M^2 + 2 \left( \sqrt{p_T^2 + M^2} \sqrt{p_T^2 + m_V^2} - \vec{p}_T \cdot \vec{p}_T \right)$$

# Transverse mass



$$m_T(0) = m_V^2 + 2 \left( \sqrt{p_T^2} \sqrt{p_T^2 + m_V^2 + p_T^2} \right)$$

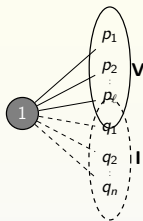
For massless invisibles, no upstream transverse momentum.



CDF 0708.3642

$W \rightarrow \ell \nu$

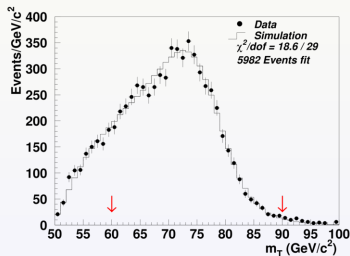
# Transverse mass



$$m_T(0) = m_V^2 + 2 \left( \sqrt{p_T^2} \sqrt{p_T^2 + m_V^2} + p_T^2 \right)$$

For massless invisibles, no upstream transverse momentum.

Name depends on context: cluster transverse mass,  $m_{T,\text{true}}$ ,  $\sqrt{s}_{\text{min}}$



CDF 0708.3642

$W \rightarrow \ell \nu$



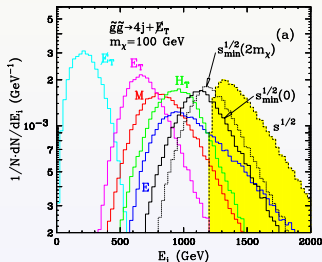
$$\sqrt{s}_{min}(0)$$

Konar, Kong & Matchev 0812.1042

Correlation between maximum of  $\sqrt{s}_{min}(0)$  distribution and sum of parent masses.

Independent of:

- process
- topology
- combinatorics



$$\sqrt{s}_{min}(0)$$

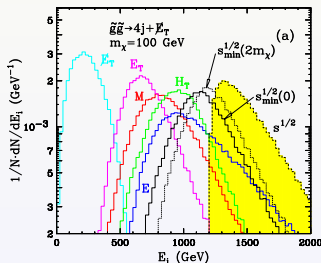
Konar, Kong & Matchev 0812.1042

Correlation between maximum of  $\sqrt{s}_{min}(0)$  distribution and sum of parent masses.

Independent of:

- process
- topology
- combinatorics

Caution: correlation dependent on  $M$  and number of invisibles



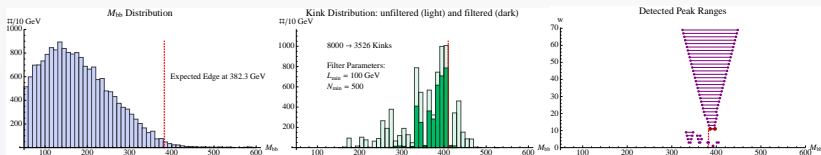
# Determining Endpoints

Curtin 1112.1095

Systematic way to automatically extract endpoint position.

Procedure:

- Fit linear kink distribution to random domains within distribution
- Obtain kink distribution (with filters)
- Detect peaks in kink distribution (bump-hunting) for intervals of varying width  $w$ . Real peaks are upside-down growing cones

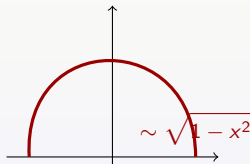
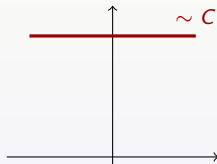
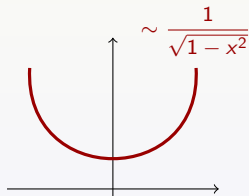
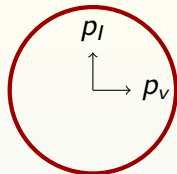


Code can be found at:

<http://insti.physics.sunysb.edu/~curtin/edgefinder/>

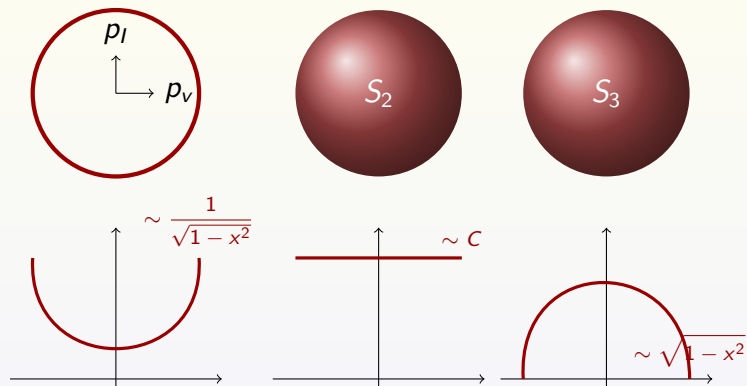
# Counting Invisibles

Giudice, Gripaio, RM 1108.1180



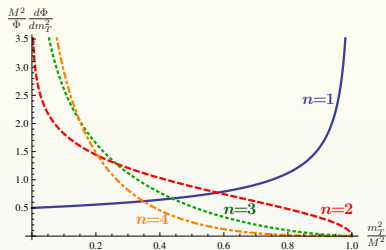
# Counting Invisibles

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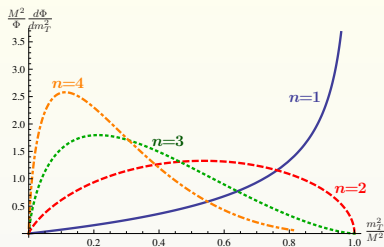


Study near-endpoint behaviour to extract number of invisibles

# Single Production



$M \rightarrow W + nX$

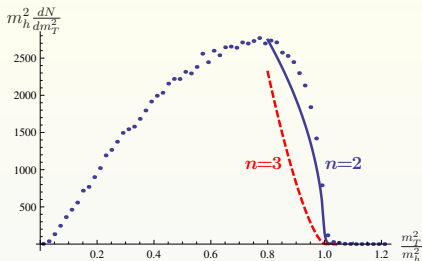
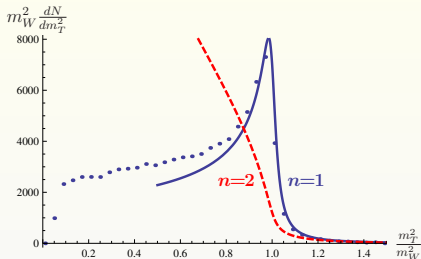


$M \rightarrow 2W + nX$

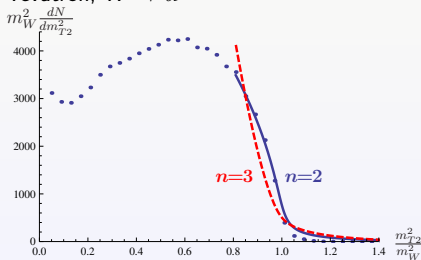
$$\frac{d\Phi}{dm_T^2} \propto \left(1 - \frac{m_T^2}{M^2}\right)^{n-1}$$

- Large difference between  $n = 1$  and  $n > 1$
- Distinguishing between different  $n \geq 2$  more difficult
- Near-universal behaviour

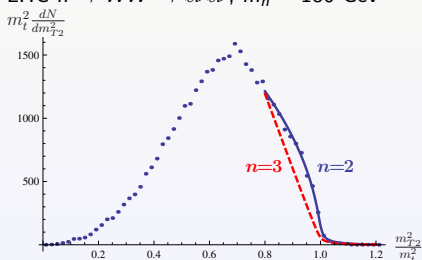
# Standard Model Examples



Tevatron,  $W \rightarrow l\nu$



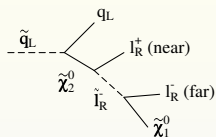
LHC  $h \rightarrow WW \rightarrow l\nu l\nu$ ,  $m_h = 180$  GeV



LHC  $h \rightarrow WW \rightarrow l\nu l\nu$ ,  $m_h = 180$  GeV

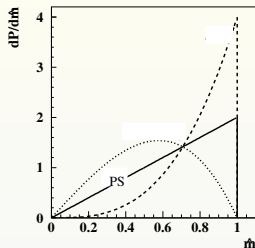
LHC  $t\bar{t} \rightarrow b\bar{b}WW \rightarrow b\bar{b}l\nu l\nu$

# SUSY Example



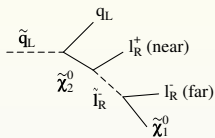
Barr hep-ph/0405052

	$\tilde{u}_L$	$\chi_2^0$	$\tilde{e}_R^-$	$\chi_1^0$
mass (GeV)	631	231	153	116





# SUSY Example



$m_X / \text{GeV}$	$R$ -squared ( $m_{T2}^2$ )			$R$ -squared ( $m_{V1}^2$ )	
	$n = 2$	$n = 3$	$n = 4$	$k = 1$	$k = 2$
0	0.947	0.992	0.899	0.992	0.855
100	0.998	0.889	0.822	0.993	0.921
450	0.859	0.991	0.870	0.987	0.911

Barr hep-ph/0405052

