

# Asymmetric WIMP dark matter and $DM/antiDM$ oscillations

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w M. Cirelli, P. Panci, G. Servant.

*24<sup>th</sup> Rencontre de Blois, 2012.*

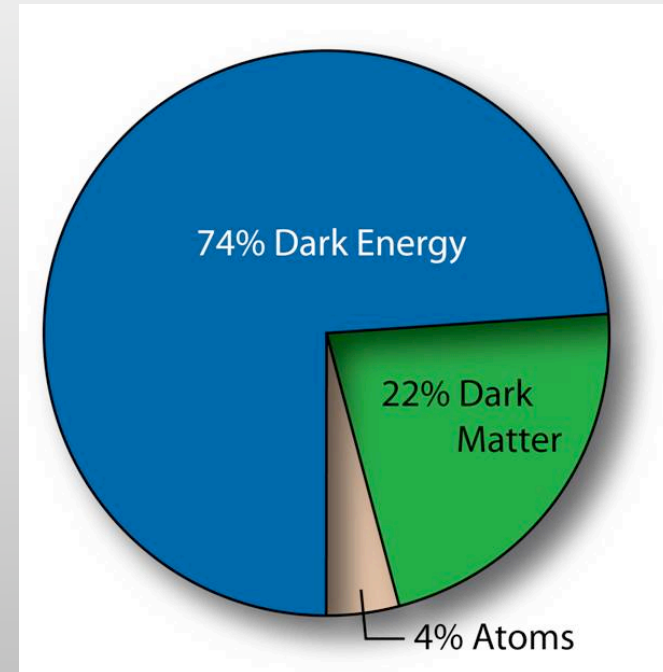
# Cosmic Pie

The energy content of the Universe:

$\Omega_{DM} \sim 22\%$  (CMB, rotational curves, X rays from clusters...)

$\Omega_b \sim 4\%$  (CMB, BBN, ...)

$\Omega_\Lambda \sim 74\%$  (CMB+SNIa observations)



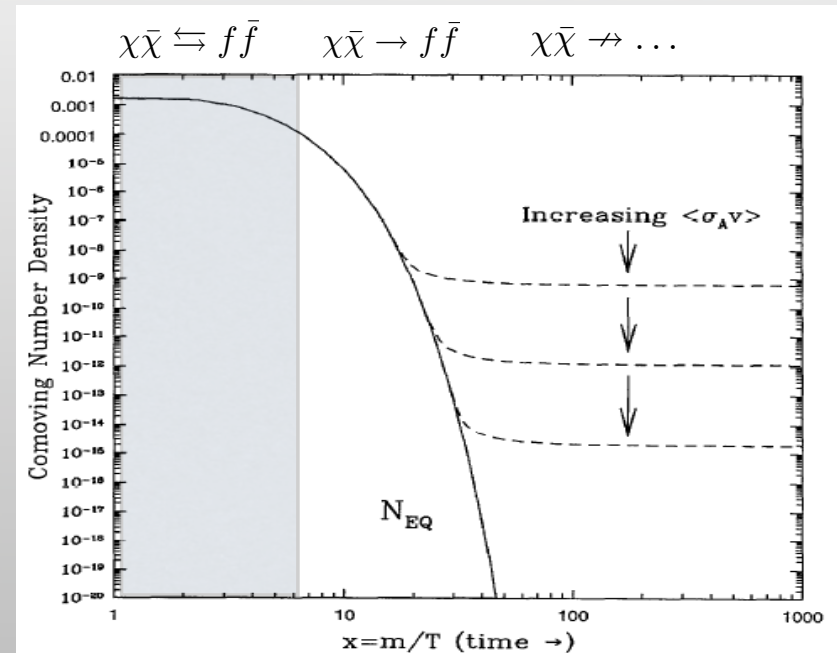
1) Most of the Universe is **unknown/Dark**.

👉 2)  $\Omega_{DM}$ ,  $\Omega_b$  (and  $\Omega_\Lambda$ ) are of a *comparable* magnitude.

# What determines $\Omega_{DM}$ and $\Omega_b$ ?

$\Omega_{DM} \leftrightarrow$  thermal decoupling (WIMPs):

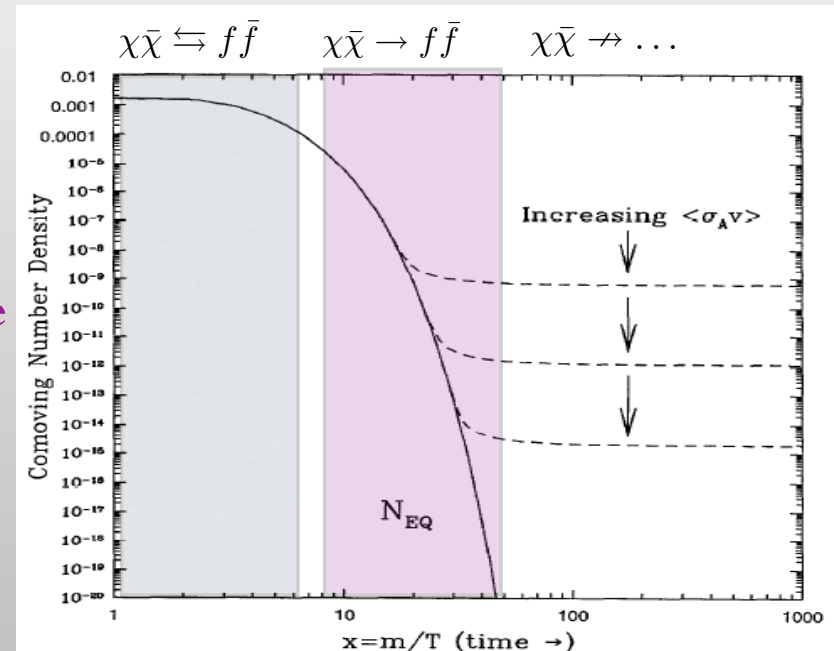
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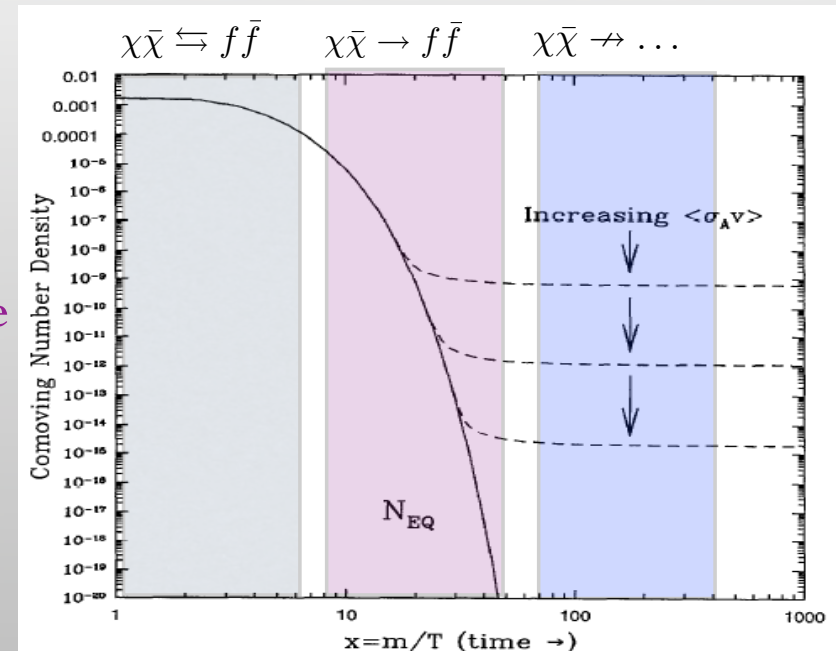
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- as the Universe expands
  - DM interaction rates drops below the expansion rate of the Universe,
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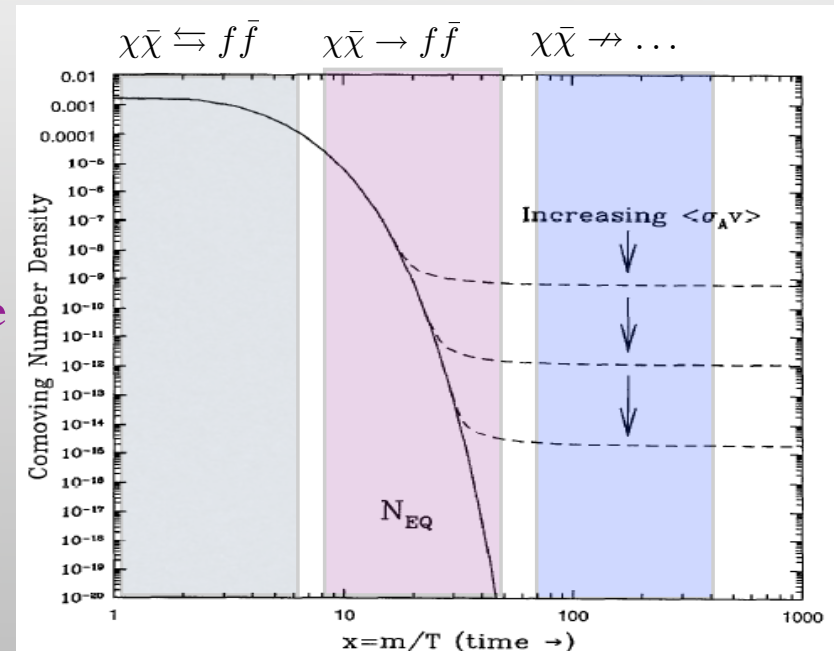
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- $\Omega_{DM}$  depends mainly on  $\langle\sigma v\rangle$ !  
(weak cross section → *WIMP miracle*)

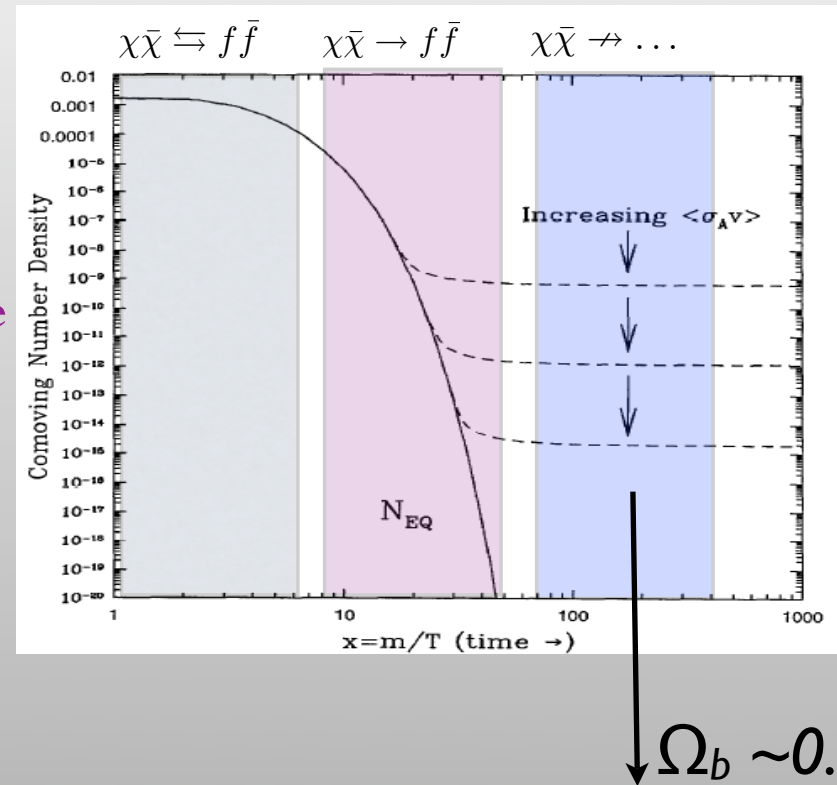


$$\langle\sigma_{\text{ann}}v\rangle \approx \frac{\alpha_w^2}{M^2} \approx \frac{\alpha_w^2}{\mathbf{1\ TeV^2}} \Rightarrow \Omega_X \sim \mathcal{O}(\text{few } 0.1)$$

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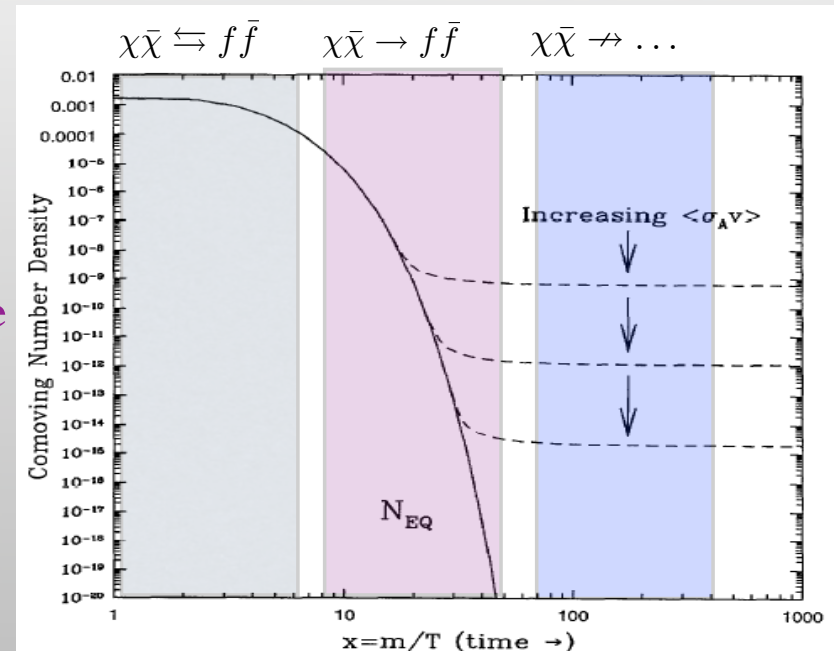
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→ DM interaction rates drops below the expansion rate of the Universe,  
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$\Omega_b \leftrightarrow$  primordial asymmetry;

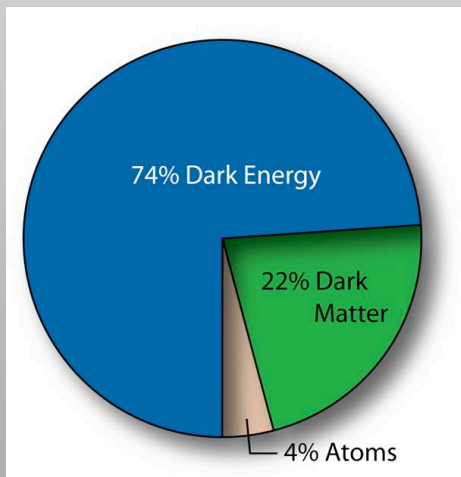
baryons freeze-out due to a lack of anti-baryons! (otherwise, due to the high cross section they would annihilate away).



# Motivation for Asymmetric DM models

$n_{DM} \leftrightarrow$  relic freeze-out  
 $n_b \leftrightarrow$  baryogenesis  
(lack of anti-baryons)

Two sectors, with mutually weak interactions and different time evolution, ...



$$\frac{\Omega_{DM}}{\Omega_b} \sim 5.86$$

Just a coincidence?  
Or signal of a link?

## General *idea* of ADM:

DM carries a **charge** and is 'asymmetric' (like the visible sector)  
+ there is a **connection** between  $\Delta B(X)$  and  $\Delta B(B,L)$  causing  $n_{DM} \sim n_b$ .



ADM models generally involve the *co-generation of an asymmetry* in both dark matter and baryonic sectors or *a transfer of asymmetries* between the two through higher-dimensional operators.

## General *features* of ADM:

1) ADM is naturally light.

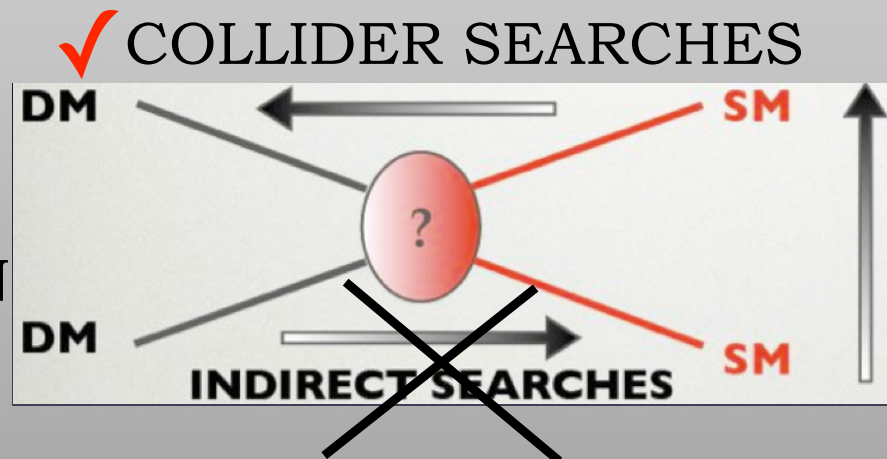
$$a (n_{DM} - n_{\overline{DM}}) = (n_B - n_{\overline{B}})$$

$$\rightarrow m_{DM} \sim 5a \text{ GeV!}$$

$$\left(\frac{\Omega_{DM}}{\Omega_B}\right) = \left(\frac{n_{DM}}{n_B}\right) \frac{m_{DM}}{m_B}$$

2) ADM does not self-annihilate: No standard indirect detection signatures.

✓ DIRECT  
DETECTION

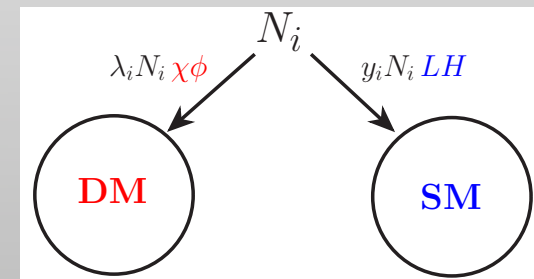


# Particle physics framework(s) - a brief overview of ideas

~100 papers on the ADM idea have been published since the 80ties.

## 1) *Co-generation* of asymmetry in dark and our sectors:

- Embed in EW baryogenesis via sphalerons/DM charged under the  $SU(2)$  (Nussinov, 1985, Barr, Chivukula&Farhi, 1990, Kaplan, 1992...).
- **Generalized GUT-baryogenesis or leptogenesis:** (Davoudiasl et. al, 1008.2399, Blennow et al., 1009.3159, Falkowski et. al, 1101.4936, ...) CP-violating decays of heavy states lead to a lepton number asymmetry in both the SM and hidden sectors.
- leptogenesis triggered by WIMP freeze-out (Cui, Randall, Shuve, 1112.2704; Chowdhury et al., 1110.5334).



(Falkowski et. al, 1101.4936:  
'Two sector leptogenesis')

# Particle physics framework(s) - a brief overview of ideas

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*2) Asymmetry transfer:* asymmetry generated in one sector and *transferred* to the other one:

- through (temperature dependent) mass mixing between X and L: (Cui, Randall, Shuve, 1106.4834.)
- through higher-dim operators (Kaplan et. al 0901.4117, Cohen&Zurek,0909.2035)

$$\mathcal{L}_{\text{asym}} = \frac{1}{M'^4_{ij}} \bar{X}^2 (L_i H)(L_j H) + \text{h.c.}, \quad \bar{X} \bar{X} \leftrightarrow \bar{\nu} \bar{\nu}$$

Asymmetry fixed after *transfer operators freeze-out* ( $T_D$ ).

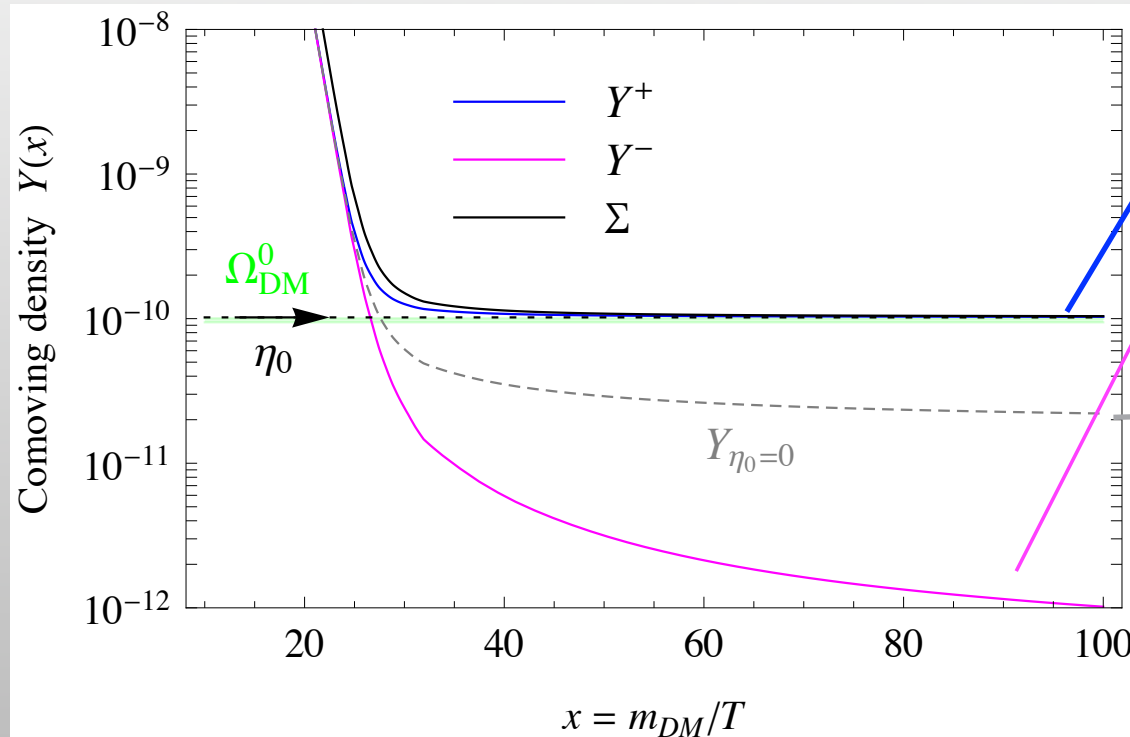
$$\frac{n_X}{n_b} \sim \frac{n_X^{eq}(T_D)}{n_b^{eq}(T_D)}$$

# DM/anti-DM oscillations?

The ADM story can change significantly in the presence of tiny *majorana mass term* which gives rise to **DM particle-antiparticle oscillations**.

Oscillating ADM provides a **generalization** of typical symmetric and asymmetric DM **freeze-out cosmologies**. (The asymmetric limit corresponds to oscillations slower than the lifetime of the Universe, while the symmetric limit corresponds to fast oscillations that turn on long before DM freeze-out.)

# DM/anti-DM oscillations: A different relic decoupling scenario



Asymmetric DM picture

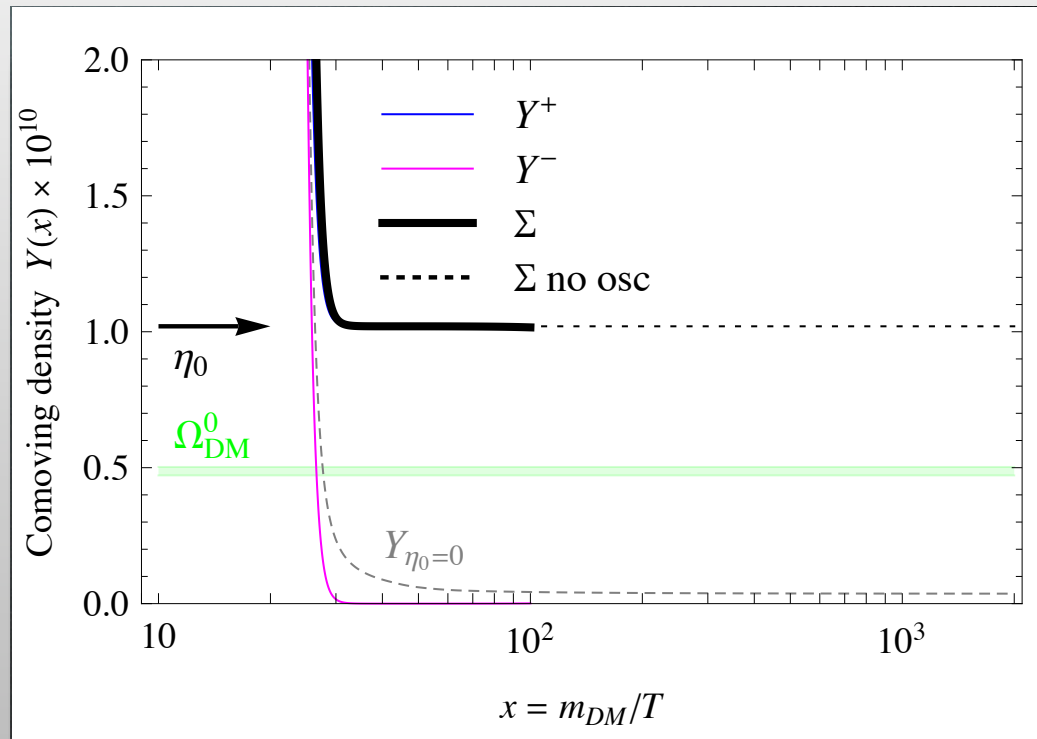
$$\Omega_{DM} \rightarrow \Omega_{DM}(\eta_0)$$

Standard WIMP picture

$$\Omega_{DM} \rightarrow \Omega_{DM}(\langle \sigma v \rangle)$$

$\eta_0$ - primordial asymmetry.  
 $Y^+/Y^-$  DM particle/antiparticle.  
 $\Sigma = Y^+ + Y^-$

# DM/anti-DM oscillations: A different relic decoupling scenario



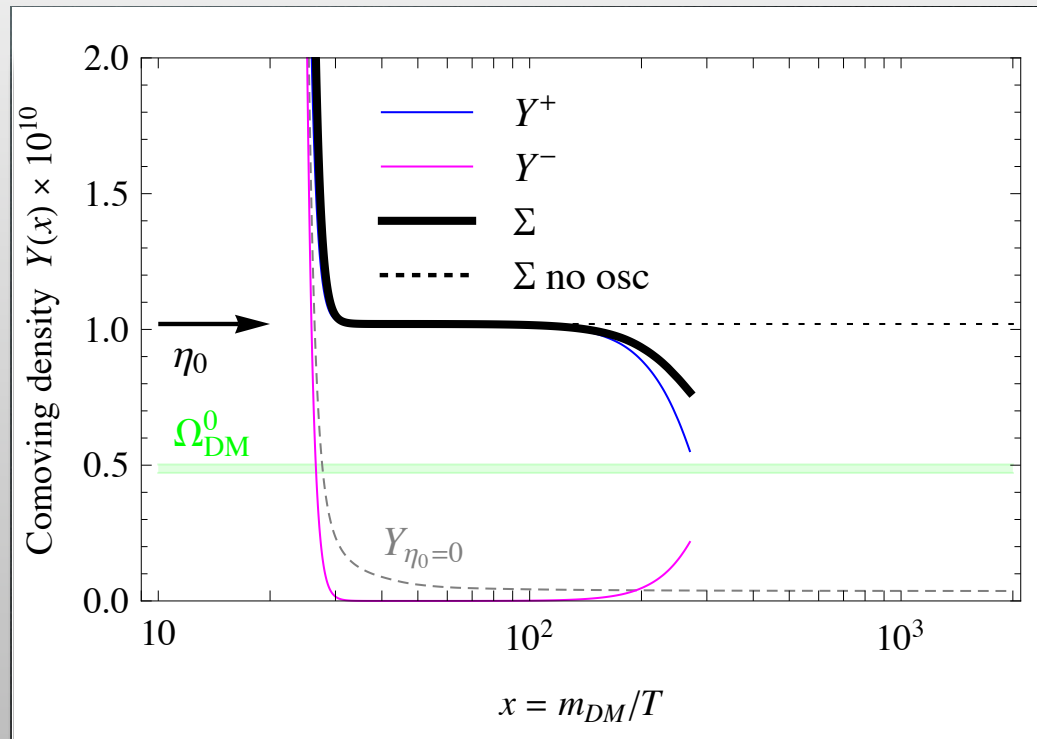
General features of ADM  
WIMP decoupling:

1. Asymmetric 'freeze-out'

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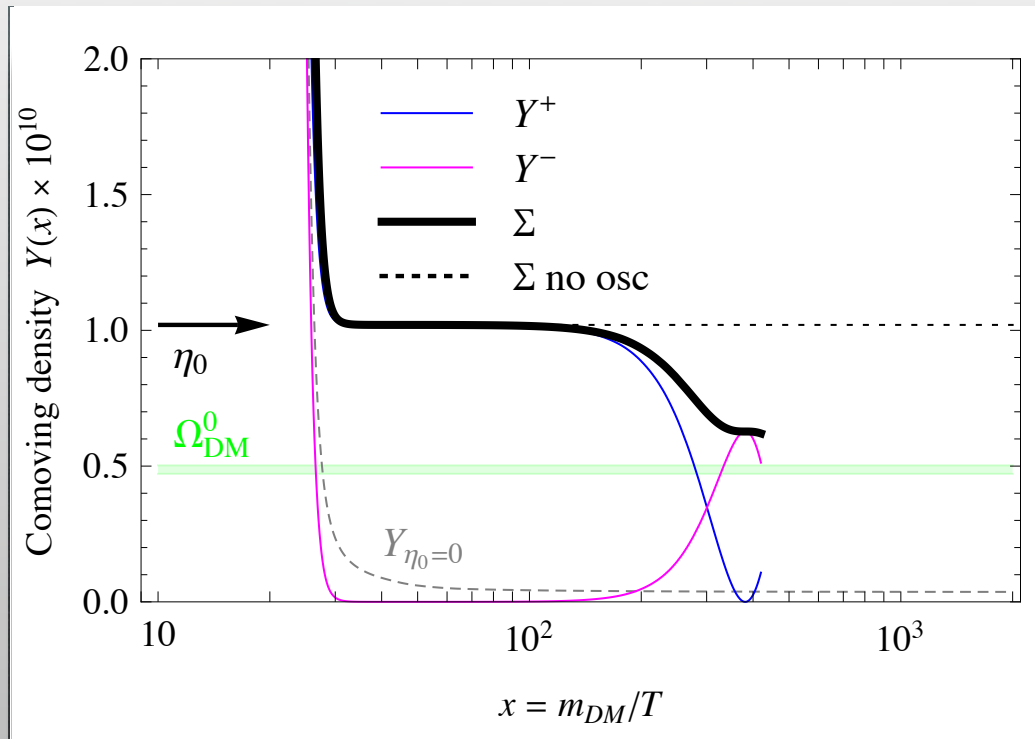


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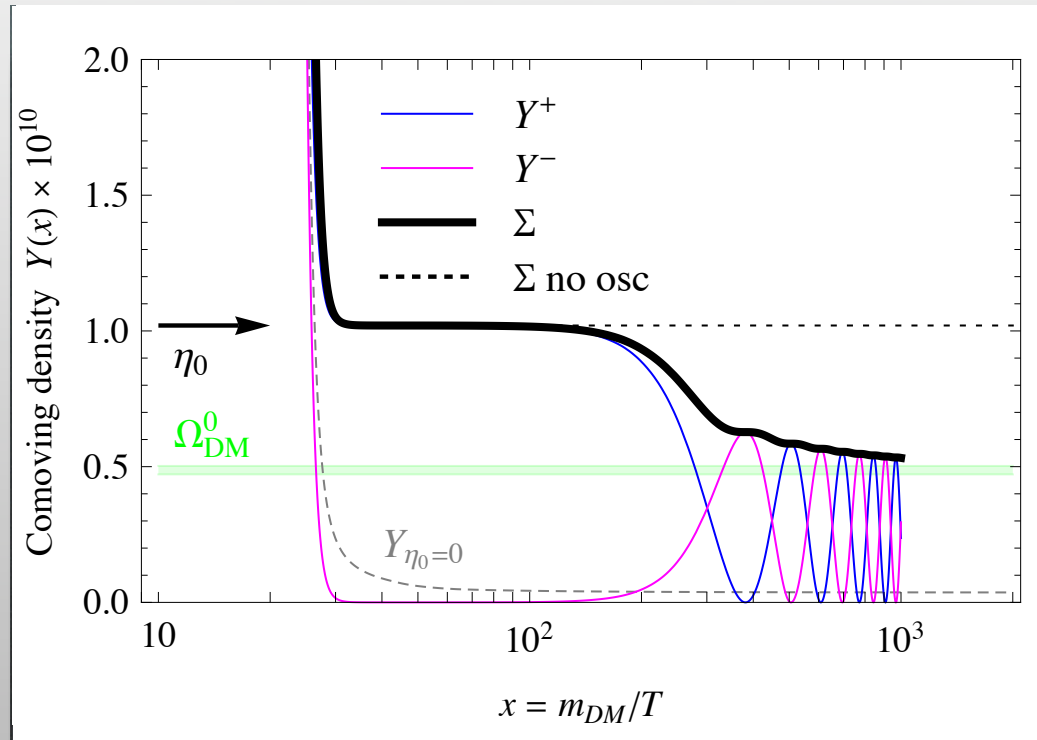


General features of ADM  
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3. **Annihilations recouple** and lower the total DM density.

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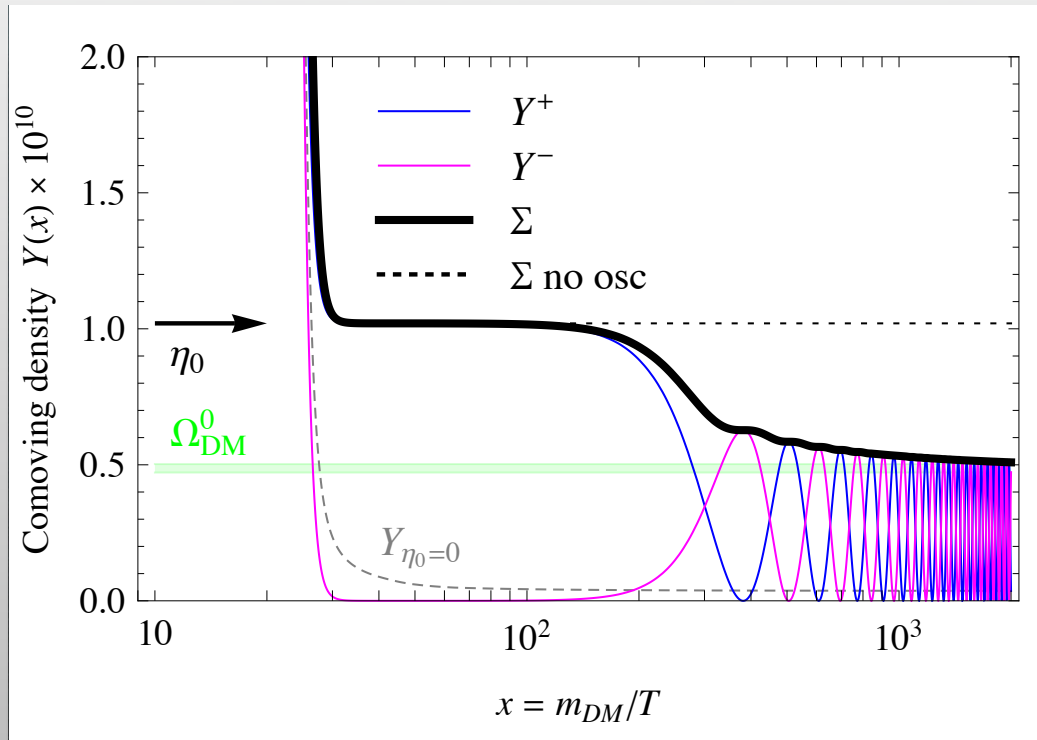


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4. **Process repeats** in a series of plateaux.

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General features of ADM  
WIMP decoupling:

1. Asymmetric 'freeze-out'
2. Oscillations repopulate  $Y^-$
3. Annihilations recouple and lower the total DM density.
4. Process repeats in a series of plateaux.
5. **Correct relic abundance** can be achieved and it now depends on:

$\eta_0$ - primordial asymmetry.  
 $Y^+/Y^-$  DM particle/antiparticle.  
 $\Sigma = Y^+ + Y^-$

$$\Omega_{DM} \rightarrow \Omega_{DM} (\langle \sigma v \rangle, \eta_0, m_{DM}, \delta m)$$

# DM/anti-DM oscillations: A different relic decoupling scenario

1. → Oscillations *fill a gap* between the standard freeze out prediction (where  $\Omega_{\text{DM}}$  depends only on the annihilation cross section  $\sigma$ ), and the ADM prediction where  $\Omega_{\text{DM}}$  depends only on the primordial DM asymmetry.
2. *Higher masses*  $>\sim 100$  GeV are therefore ‘naturally’ available in this framework
3. *Phenomenological bounds modified*: DM is symmetric today, so it self-annihilates! Traditional ADM bounds do not apply while standard WIMP bounds become relevant.

# DM/anti-DM oscillations: The formalism

We study a system of  $Y^+$  and  $Y^-$ , which possess *an initial asymmetry* ( $Y^+ > Y^-$ ) and is subject to *simultaneous*:

- i) oscillations  $Y^{+,-} \leftrightarrow Y^{-,+}$
- ii) annihilations  $Y^+ Y^- \leftrightarrow \text{SMSM}$  and
- iii) elastic scatterings  $Y^{+,-} \text{ SM} \leftrightarrow Y^{+,-} \text{ SM}$ .

It is an interplay between a coherent process such as oscillations with incoherent processes such as annihilations and scatterings.

‘*Density matrix formalism*’ (originally developed for  $\nu$  oscillations in the Early Universe) provides a framework to account for quantum coherence between particle and antiparticle states (Dolgov, 1981; Sigl&Raffelt, 1993; Dolgov et al., hep-ph/0202122v2, ...)

# DM/anti-DM oscillations: The formalism

$$\mathcal{Y}(x) = \begin{pmatrix} Y^+(x) & Y^{+-}(x) \\ Y^{-+}(x) & Y^-(x) \end{pmatrix}$$

$Y$ : co-moving DM abundance;  
**diagonal elements** are *physical states*.  
 off diagonal elements are their superposition.

$$Y_0^\pm \equiv Y^\pm(x_0) = Y_{\text{eq}}(x_0) e^{\pm\xi_0}$$

$$\mathcal{Y}'(x) = -\frac{i}{x H(x)} \left[ \mathcal{H}, \mathcal{Y}(x) \right]$$

mass hamiltonian acts as source of oscillations

$$-\frac{s(x)}{x H(x)} \left( \frac{1}{2} \left\{ \mathcal{Y}(x), \Gamma_a \bar{\mathcal{Y}}(x) \Gamma_a^\dagger \right\} - \Gamma_a \Gamma_a^\dagger \mathcal{Y}_{\text{eq}}^2 \right)$$

$Y^+ \leftrightarrow Y^-$   
**annihilations**  
 $Y^+ Y^- \leftrightarrow \text{SMSM}$

$$-\frac{1}{x H(x)} \left\{ \Gamma_s(x), \mathcal{Y}(x) \right\}$$

**elastic scatterings**  
 $Y \text{ SM} \leftrightarrow Y \text{ SM}$

$$\mathcal{H} = \begin{pmatrix} m & \delta m \\ \delta m & m \end{pmatrix}$$

and we take  $\Gamma_a \sim \langle \sigma_{aV} \rangle I$ ,  $\Gamma_s \sim \sigma_s I$ .

# DM/anti-DM oscillations:

## Results:

Parameters of the system:  $m_{\text{DM}}$ ,  $\sigma_0$ ,  $\delta m$ ,  $\eta_0$ ,  $\xi$ .

$\delta m$ : oscillation parameter: tiny! typically  $10^{-14} \rightarrow 10^{-2}$  eV

If  $\delta m$  *too large*: oscillations occur too early, system is symmetric.

If  $\delta m$  *too small*: oscillations occur too late, system is totally asymmetric.

$\eta_0$ : primordial DM asymmetry: free, but naturally  $\sim \eta_b$

$\xi$ : strength of scattering on normal matter wrt naive  $\sim G_F$  expectations.

Direct detection experiments impose  $\xi < 10^{-2}$



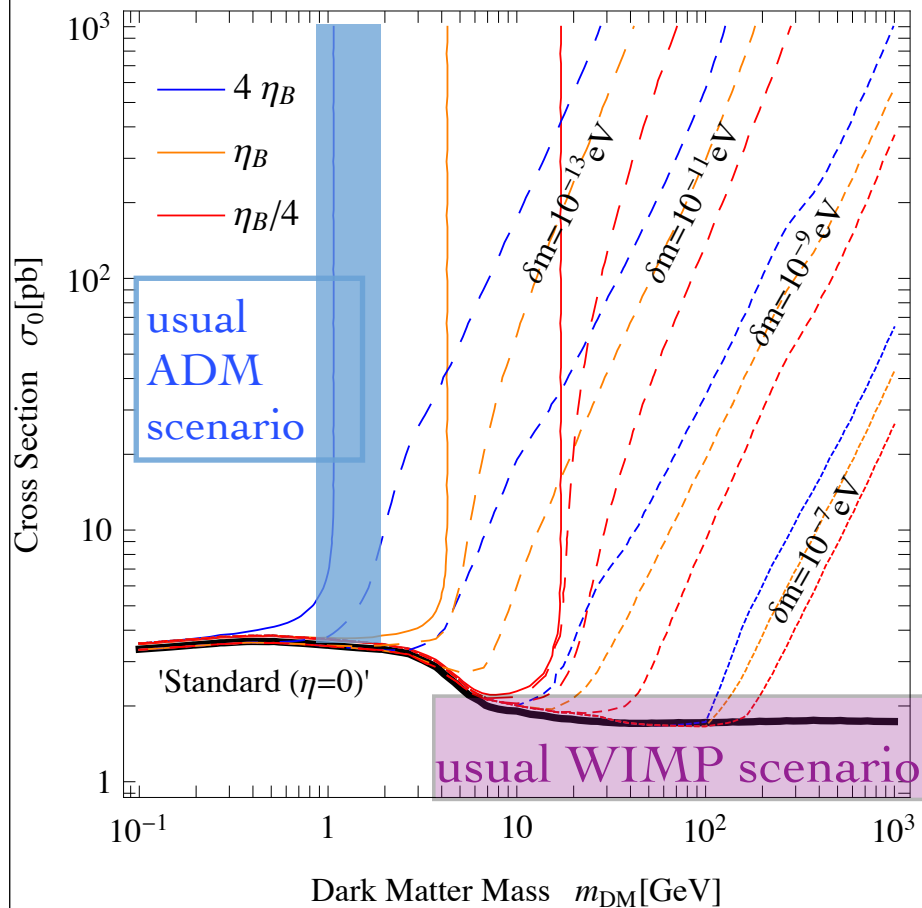
# DM/anti-DM oscillations:

Results:  $\sigma_0$  vs  $m_{\text{DM}}$  plane.

w isolines of correct  $\Omega_{\text{DM}}$ , for different values of  $\delta m$  and  $\eta_0$ .

ann+osc

$\xi = 0$



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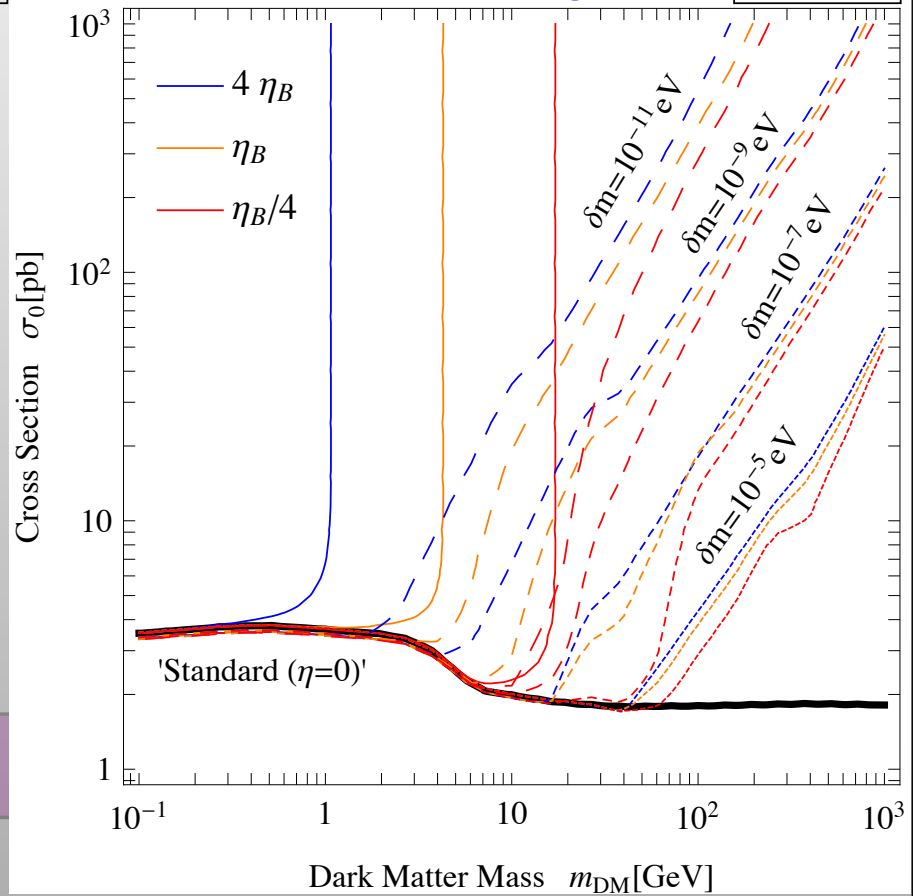
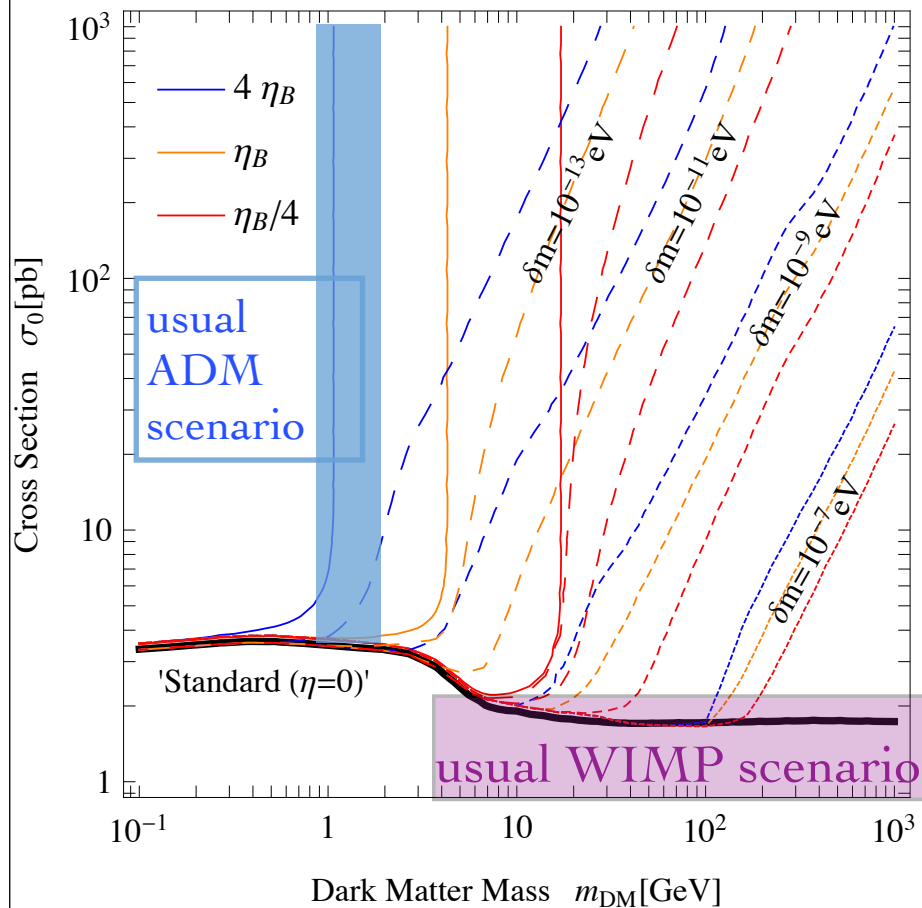
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ann+osc

$\xi = 0$

ann+osc+ el scatterings

$\xi = 10^{-2}$



# DM/anti-DM oscillations:

Results: Parameter space with phenomenological constraints.

Oscillations symmetrize dark sector → constraints on WIMP annihilations apply.

→ Energy injected from DM annihilation during **recombination** ( $z \sim 1100$ ), results in an increased amount of free electrons, which survive to lower redshifts and affect the **CMB** anisotropies. [Galli et al., PRD (2011)]

→ **Present** time annihilations (*producing gamma rays*)

Fermi-LAT observation (non-detection) of **dwarf spheroidal Galaxies**. [Fermi-LAT collaboration, PRL (2011)]

HESS observation of the **Galactic Center** halo region. Due to the high energies covered by ACTs these limits are specially relevant for heavy  $> \sim 1 \text{ TeV}$  DM.

[ H.E.S.S. Collaboration, arXiv:1103.3266]

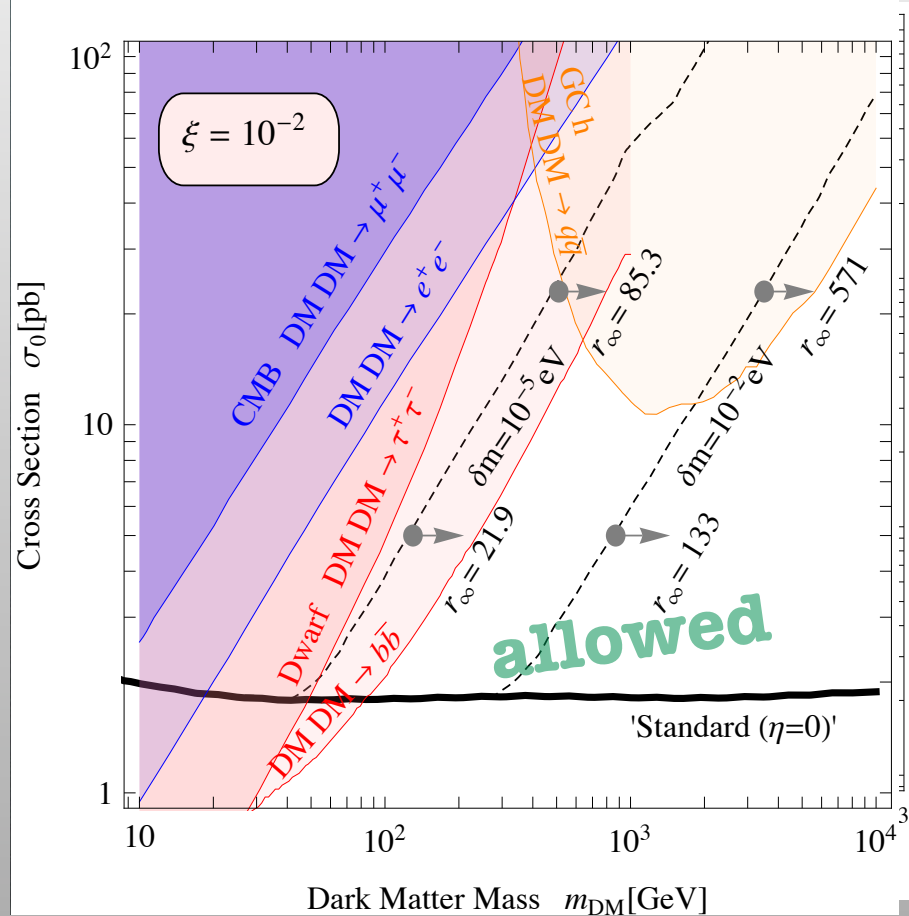
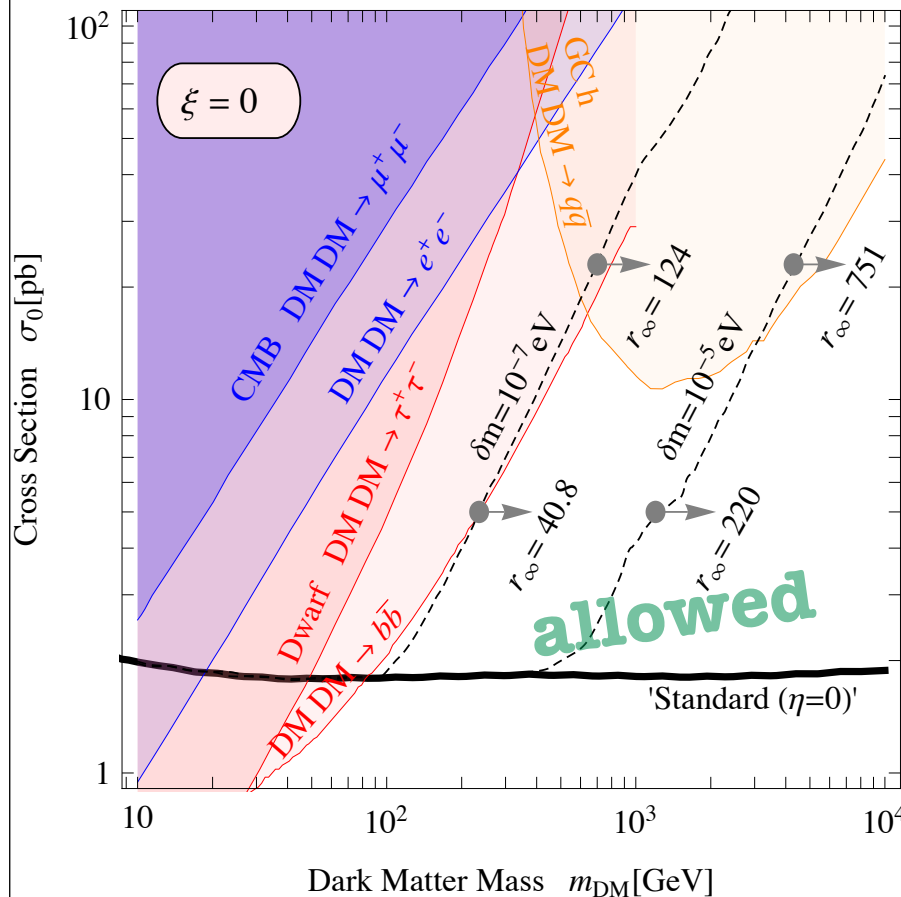
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ann+osc

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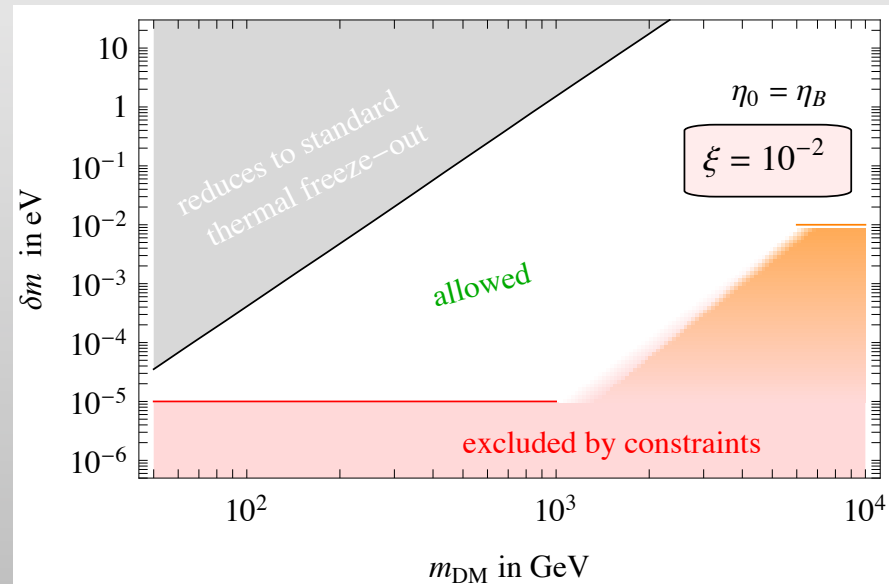
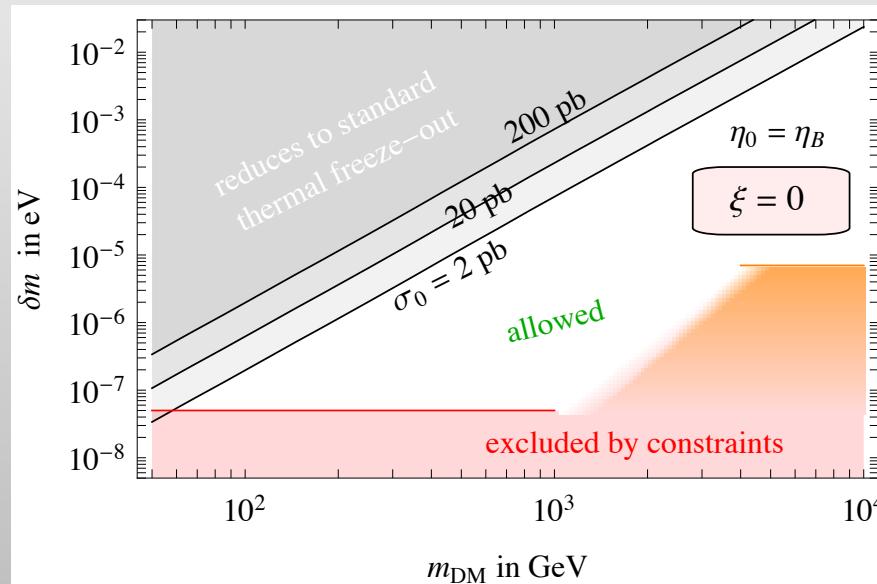
# DM/anti-DM oscillations:

## Results: $\delta m$ vs $m_{\text{DM}}$ plane.

As oscillations symmetrize dark sector, usual WIMP constraints apply.

ann+osc

ann+osc+ el scatterings



Note: a natural value in the fermionic case is obtained from the dimension-5 operator:

$$\frac{XXH^\dagger H}{\Lambda}$$

taking  $\Lambda \sim M_{\text{Pl}}$ ,  $\langle H \rangle \rightarrow \delta m \sim 10^{-6} \text{ eV}$ .

# Comparing

Tulin, Yu, Zurek, 1202.0283

✓ full formalism from first principles:

- non-equilibrium QFT

✓ extends to include

- flavor sensitive interactions
- precise effects of scatterings

- only specific examples

This work, 1110.3809

- full matrix formalism

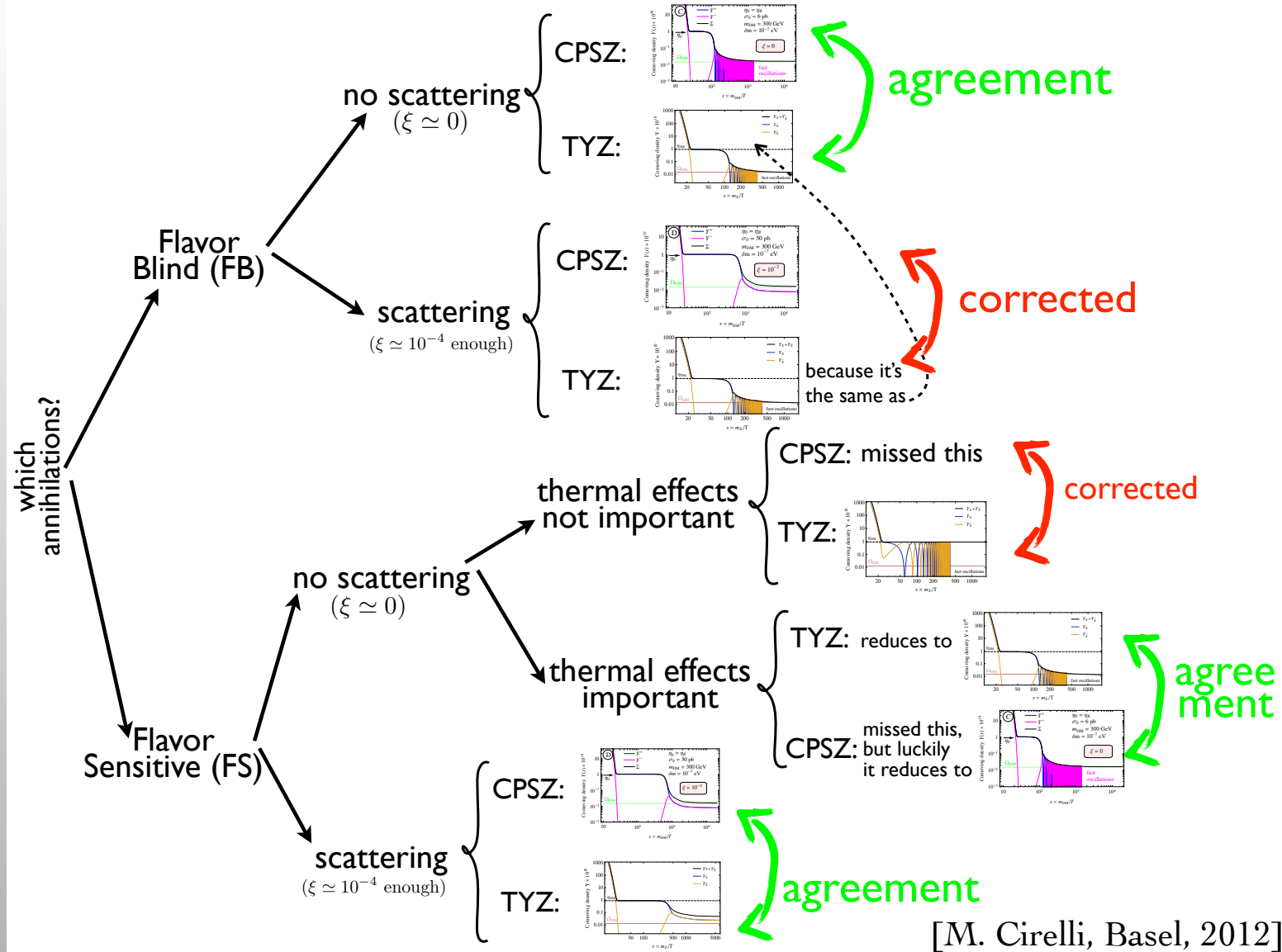
- scattering on plasma

✓ scans parameter space

## Quantitatively:

results unchanged for some particle physics cases

some new cases appear (next page)



FB/FS refers to a transformation property of a L under C.

If DM/fermions coupled through contact interaction: flavor blind (scalar, pseudo scalar, axial vector)/sensitive (vector and tensor).

# Summary

- Scenarios with DM anti-DM oscillations *preserve the attractive feature of ADM*, that relates the DM primordial asymmetry and the baryon asymmetry and at the same time *preserve also the appeal of weak scale DM mass and cross-sections*.
- We *suggest a formalism* needed to treat the system of particles that oscillate coherently but at the same time suffer coherence-breaking elastic scatterings on the plasma and annihilations among themselves.
- We have applied such formalism to *explore the phenomenologically available space*, by varying the parameters of  $m_{\text{DM}}$ ,  $\sigma_0$ ,  $\eta_0$ ,  $\delta m$ , for two discrete choices of the parameter  $\xi$  that sets the strength of the elastic scatterings on the plasma.
- Work on particular particle physics cases in progress.



Extra slides

## General features of ADM:

## Phenomenological probes/constraints:

Stars can *accumulate* far more ADM particles than usual WIMPs, which can *alter their dynamics*.

- ADM captured in *neutron stars* can become *self-gravitating*, forming a *black hole* that will eventually destroy the host stars. *Observation of old pulsars in globular clusters* then sets the limit on DM capture rate (elastic cross section) competitive w.r.t. direct detection experiments. (McDermott et al., 1103.5472)

(Panci, Cirelli, Servant,  
Zaharijas, I I 10.3809)

## DM/anti-DM oscillations?

A small  $\chi^+/\chi^-$  mass splitting induces  $\chi^+ \leftrightarrow \chi^-$  oscillations.

$$- \mathcal{L}_{mass} = \frac{1}{2} \overline{\left( (X_L)^c \quad X_R \right)} \begin{pmatrix} \Delta & m \\ m & \Delta \end{pmatrix} \begin{pmatrix} X_L \\ (X_R)^c \end{pmatrix} + h.c. \quad \text{fermionic DM}$$

$$\mathcal{L}_{mass} = \frac{1}{2} (\varphi, \varphi^*)^* \begin{pmatrix} m^2 & \Delta^2/2 \\ \Delta^2/2 & m^2 \end{pmatrix} \begin{pmatrix} \varphi \\ \varphi^* \end{pmatrix} \quad \text{scalar DM}$$

$$\mathcal{H} = \begin{pmatrix} m & \delta m \\ \delta m & m \end{pmatrix} \quad \text{where} \quad \delta m = \begin{cases} \Delta & \text{if fermionic DM} \\ \Delta^2/(4M) & \text{if bosonic DM} \end{cases}$$

$\Delta$  is a term which violates a global  $U(1)_{DM}$  and its non-zero value is responsible for the oscillations between  $Y^+$  and  $Y^-$ .

Natural to assume: 'Majorana' mass  $\Delta \ll$  'Dirac' mass  $m$ .

# DM/anti-DM oscillations: $\delta m$

In our study,  $\delta m$  is a free parameter that can range orders of magnitude.  
*Could the Majorana masses of neutrinos and dark matter have a common origin?*

(Cohen&Zurek, 0909.2035, Falkowski, 1101.4936),

extra *hidden scalar*  $\varphi$  links *right handed N* and **DM** (leptogenesis framework)

$$\mathcal{L} \supset -m_\chi \chi \tilde{\chi} + \frac{1}{2} M_{N_1} N_1^2 + \lambda N_1 \chi \langle \phi \rangle + y N_1 L \langle h \rangle + h.c.$$

$$\mathcal{L} \supset -m_\chi \chi \tilde{\chi} - \frac{\mu_\chi}{2} \chi^2 - \frac{m_\nu}{2} \nu^2 - \mu_{\chi\nu} \chi \nu + h.c.$$

$$\mu_\chi = \lambda^2 \frac{v_\phi^2}{M_{N_1}}, \quad m_\nu = y^2 \frac{v_{EW}^2}{M_{N_1}}, \quad \mu_{\chi\nu} = \left( \frac{\lambda}{y} \frac{v_\phi}{v_{EW}} \right) m_\nu.$$

if  $\varphi$  acquires a vev, it generates a Majorana mass for DM but also induces a mixing between DM and neutrinos that can lead to DM decay depending on the choice of parameters.

- Note: a natural value in the fermionic case is obtained from the dimension-5 operator:

$$\frac{X X H^\dagger H}{\Lambda}$$

taking  $\Lambda \sim M_p$ ,  $\langle H \rangle \rightarrow \delta m \sim 10^{-6} \text{ eV}$ .

## Formalism: Consider *only* DM annihilations

The density matrix equation reads:

$$\mathcal{Y}'(x) = -\frac{s(x)}{x H(x)} \left( \frac{1}{2} \left\{ \mathcal{Y}(x), \Gamma_a \bar{\mathcal{Y}}(x) \Gamma_a^\dagger \right\} - \Gamma_a \Gamma_a^\dagger \mathcal{Y}_{\text{eq}}^2 \right).$$

annihilations

$$\Gamma_a \Gamma_a^\dagger = \langle \sigma v \rangle \mathbb{I} \quad \bar{\mathcal{Y}} = \text{CP}^{-1} \cdot \mathcal{Y} \cdot \text{CP}$$

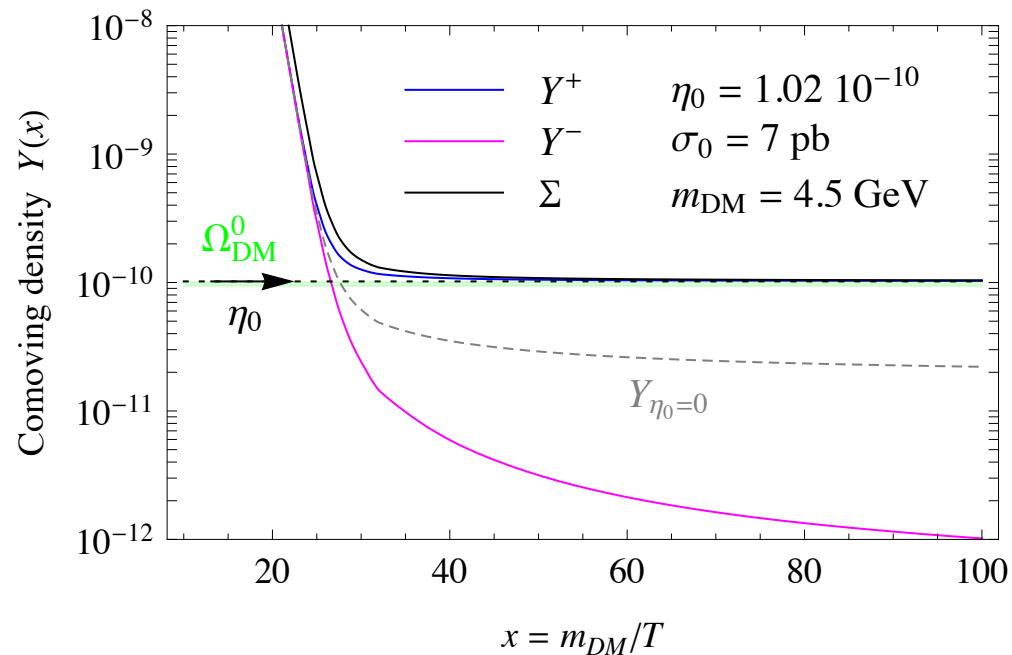
In this case the matrix form reduces to the usual Boltzmann eqn:

$$Y^{\pm'}(x) = -\frac{\langle \sigma v \rangle s(x)}{x H(x)} \left[ Y^+(x) Y^-(x) - Y_{\text{eq}}^2(x) \right].$$

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## Formalism: Consider *only* oscillations

The density matrix equation reads:

$$\mathcal{Y}'(x) = -\frac{i}{x H(x)} [\mathcal{H}, \mathcal{Y}(x)].$$

mass hamiltonian acts as source of oscillations

$$\mathcal{H} = \begin{pmatrix} m_{\text{DM}} & \delta m \\ \delta m & m_{\text{DM}} \end{pmatrix}.$$

And is equivalent to a simple set of two equations:

$$\begin{cases} \Sigma'(x) = 0, \\ \Delta'(x) = -2 \frac{\Gamma_{\text{osc}}(x)}{x H(x)} \Delta(x). \end{cases}$$

$\Sigma$ - the total number of particles  
 $\Delta$  - the difference

$$\Gamma_{\text{osc}} \rightarrow \delta m \tan(\delta m / H(x))$$

## Formalism: Consider *only* oscillations

And is equivalent to a simple set of two equations:

$$\begin{cases} \Sigma'(x) = 0, \\ \Delta'(x) = -2 \frac{\Gamma_{\text{osc}}(x)}{x H(x)} \Delta(x). \end{cases}$$

Solutions are simple oscillations:

- $\Sigma$  stays constant,
  - $\Delta$  oscillates,
- $$\Delta = \Delta_0 \text{Cos}(\delta m / 2H(x))$$

$$\Gamma_{\text{osc}} \rightarrow \delta m \tan(\delta m / H(x))$$

oscillation period:  $H \sim l/2t$ ;  $t_{\text{osc}} \sim 2\pi/\delta m$ .



## Formalism: *Oscillations + elastic scatterings*

Now we can study an effect of *decoherence* of scattering on DM oscillations

$$\mathcal{Y}'(x) = -\frac{i}{x H(x)} \left[ \mathcal{H}, \mathcal{Y}(x) \right] - \frac{1}{H(x)} \left\{ \Gamma_s(x), \mathcal{Y}(x) \right\}.$$

$$\mathcal{H} = \begin{pmatrix} m_{\text{DM}} & \delta m \\ \delta m & m_{\text{DM}} \end{pmatrix}. \quad \Gamma_s = \begin{pmatrix} \gamma_s & 0 \\ 0 & \gamma_s \end{pmatrix}$$

mass hamiltonian acts as  
source of oscillations

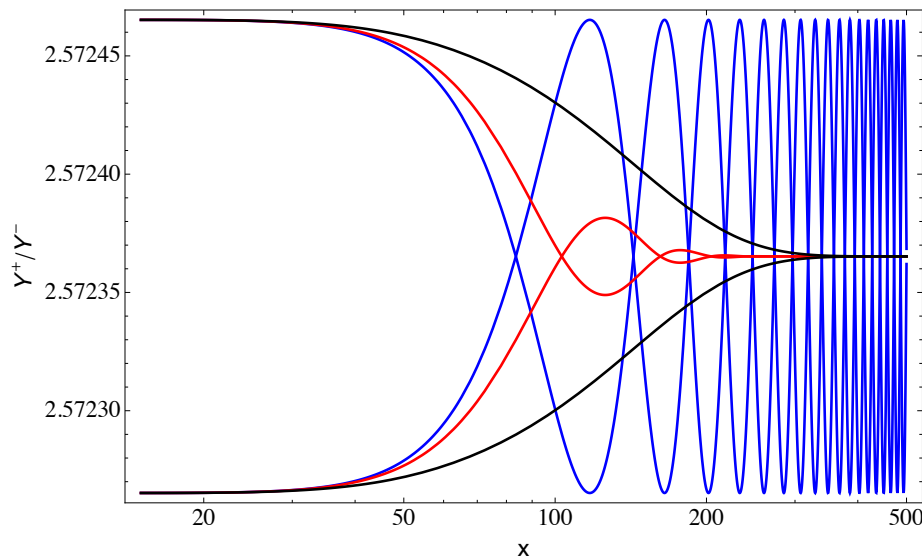
elastic scatterings described  
by a diagonal matrix.

# Formalism: *Oscillations + elastic scatterings*

Now we can study an effect of *decoherence* of scattering on DM oscillations

$$\mathcal{Y}'(x) = -\frac{i}{x H(x)} \left[ \mathcal{H}, \mathcal{Y}(x) \right] - \frac{1}{H(x)} \left\{ \Gamma_s(x), \mathcal{Y}(x) \right\}.$$

numerical solution of DMeq:



*Scatterings delay and damp oscillations!*

The same holds for *annihilations*.

$\Gamma = 0$  oscillations only

$\Gamma = \delta m$

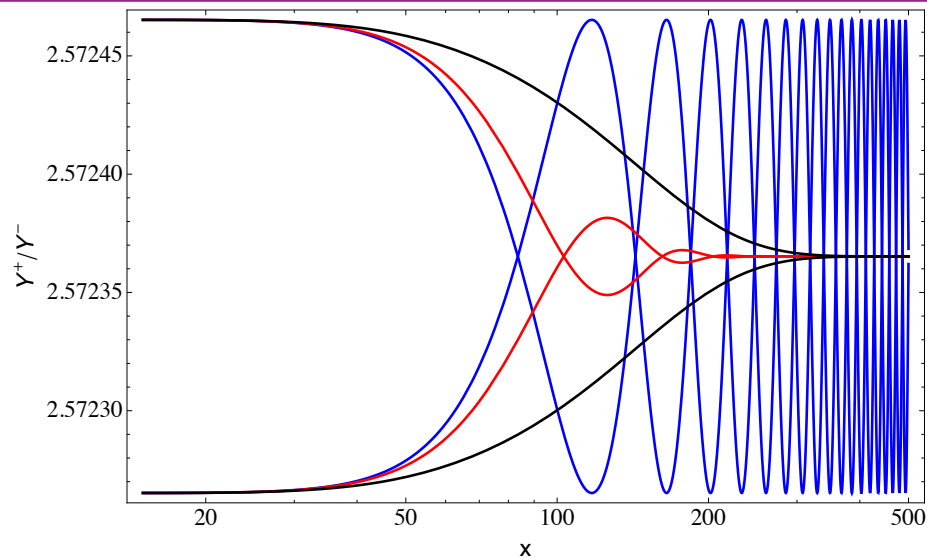
$\Gamma = 5\delta m$

## Formalism: *Oscillations + elastic scatterings*

$$\begin{cases} \Sigma'(x) = 0, \\ \Delta'(x) = -2 \frac{\Gamma_{\text{osc}}(x)}{x H(x)} \Delta(x). \end{cases}$$

If scattering rates are  $\gg \delta m$ , the solution is **damped oscillator**, with a decay time  $\delta m^2/\Upsilon!$

$$\Gamma_{\text{osc}} \rightarrow 2 \delta m^2 / \gamma_s$$



$\Gamma = 0$  oscillations only

$\Gamma = \delta m$

$\Gamma = 5\delta m$

## Formalism: *Full Boltzmann equation*

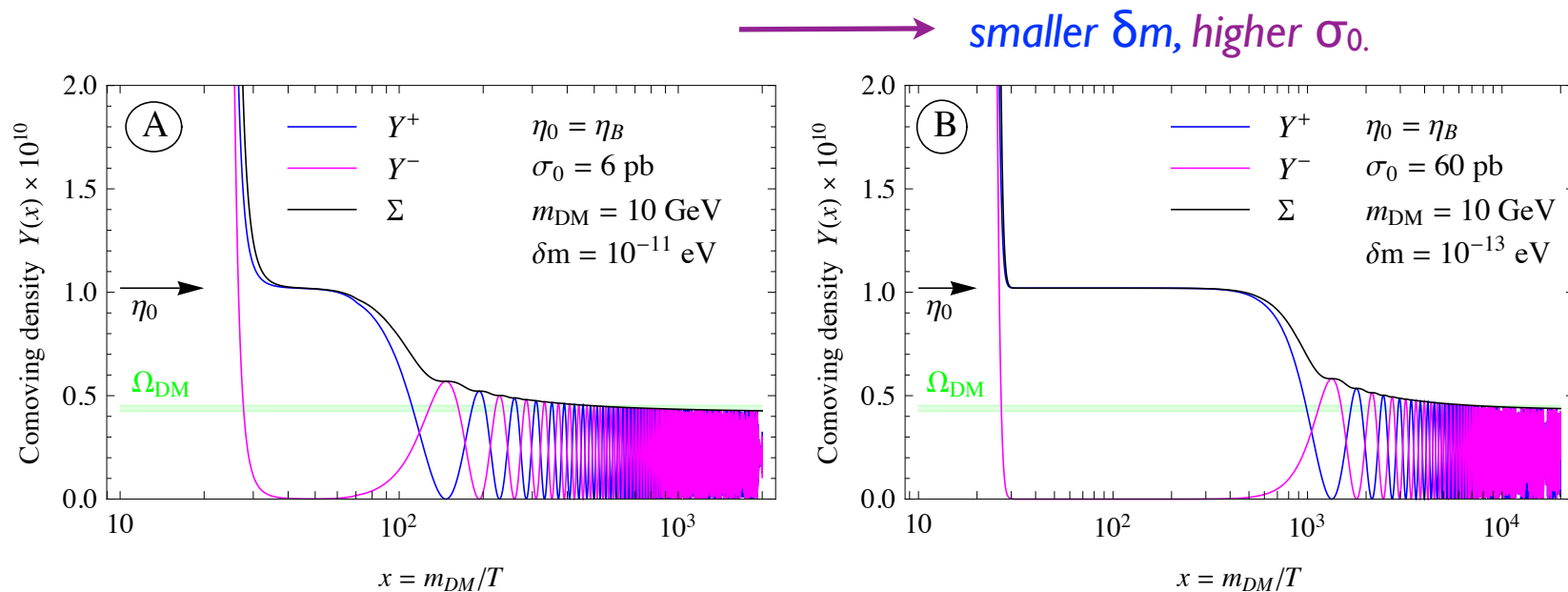
Rephrased in terms of 4 new variables, rather than density matrices.

$$\left\{ \begin{array}{l} \Sigma'(x) = -2 \frac{\langle \sigma v \rangle s(x)}{x H(x)} \left[ \frac{1}{4} \left( \Sigma^2(x) - \Delta^2(x) - \Xi^2(x) - \Pi^2(x) \right) - Y_{\text{eq}}^2(x) \right], \\ \Delta'(x) = \frac{2i \delta m}{x H(x)} \Xi(x), \\ \Xi'(x) = \frac{2i \delta m}{x H(x)} \Delta(x) - \frac{i \Delta V}{x H(x)} \Pi(x) - \frac{\gamma_s}{x H(x)} \Xi(x) - \frac{\langle \sigma v \rangle s(x)}{x H(x)} \Xi(x) \Sigma(x), \\ \Pi'(x) = -\frac{i \Delta V}{x H(x)} \Xi(x) - \frac{\gamma_s}{x H(x)} \Pi(x). \end{array} \right.$$

$$\Pi(x) = Y^{+-}(x) + Y^{-+}(x)$$

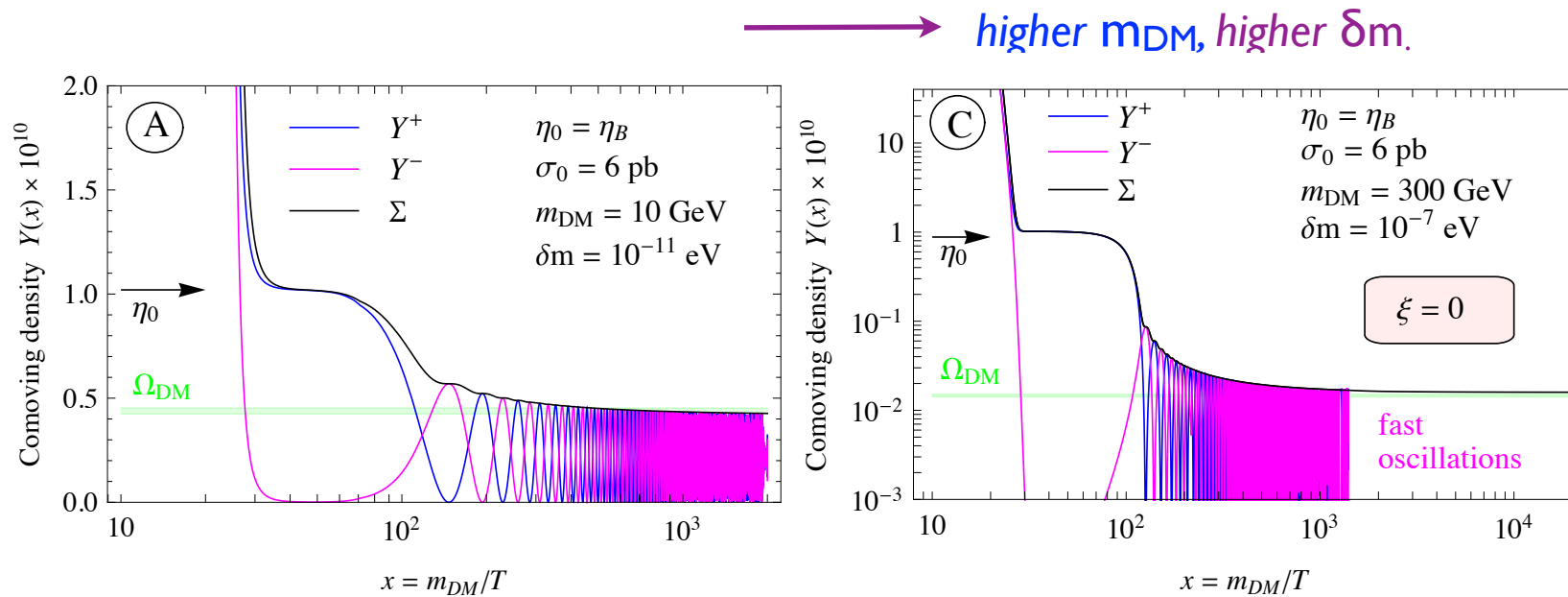
$$\Xi(x) = Y^{+-}(x) - Y^{-+}(x)$$

# Results: Interplay among parameters: varying $\delta m$



To the right: a much *smaller*  $\delta m$ : the co-moving population of DM therefore sits for a *longer* time on the plateau determined by the initial asymmetry  $\eta_0$ . **Higher value of  $\sigma_0 = 60 \text{ pb}$**  is now needed to reach the correct relic abundance.

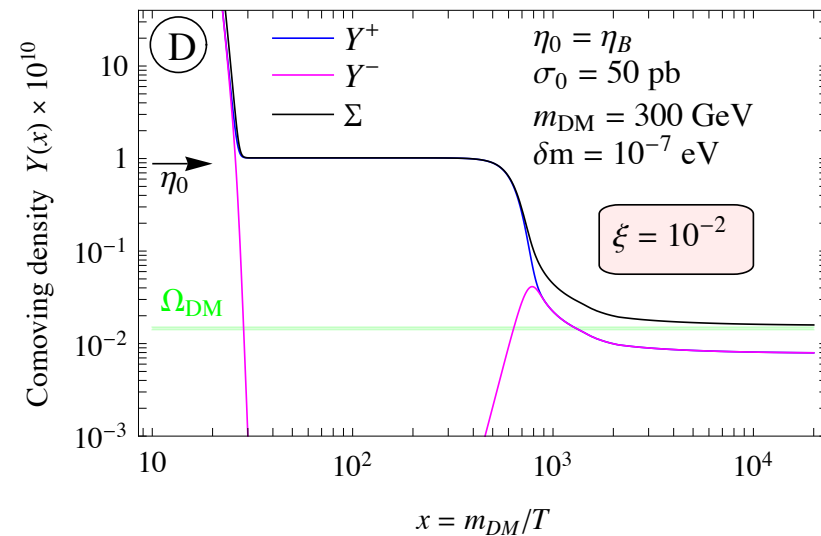
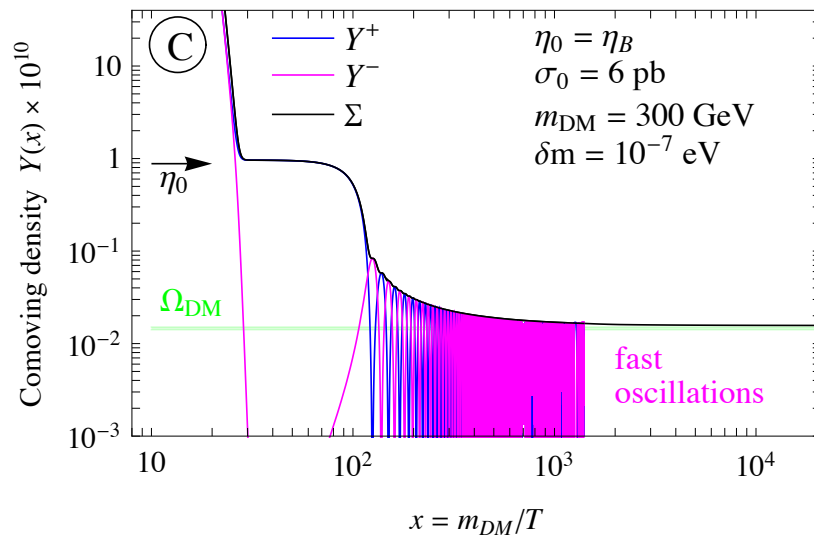
# Results: Interplay among parameters: varying $m_{DM}$



To the right: a higher, roughly **weak-scale value of the DM mass**. The correct relic abundance is achieved by starting oscillations earlier (to deplete  $Y$  more efficiently!), i.e. by choosing a **larger  $\delta m$** .

# Results: Interplay among parameters: adding $\xi$ .

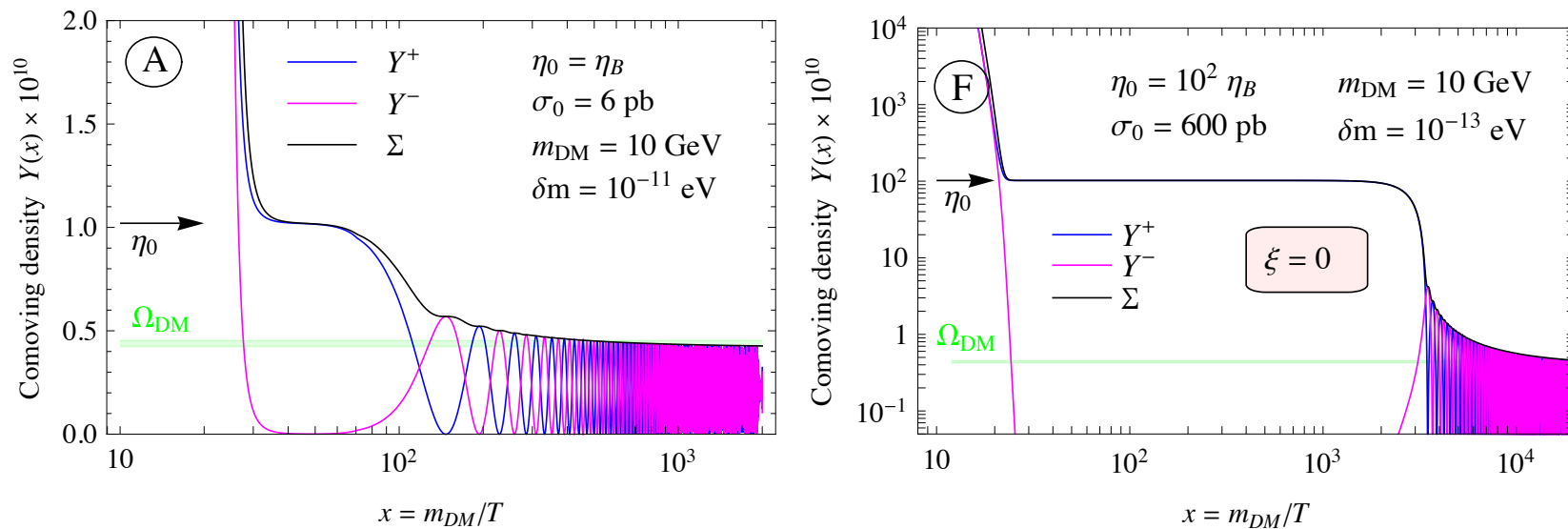
→ added  $\xi$ , higher  $\sigma_0$ .



To the right: *elastic scatterings included* ( $\xi = 10^{-2}$ ) - the effect of *incoherent scatterings* that delay and damp the oscillations. A *larger cross section* is needed to keep the annihilations active at late times and thus reach the right abundance.

# Results: Interplay among parameters: adding $\eta_0$ .

→  $\eta_0 \gg \eta_B$ , higher  $\sigma_0$ .



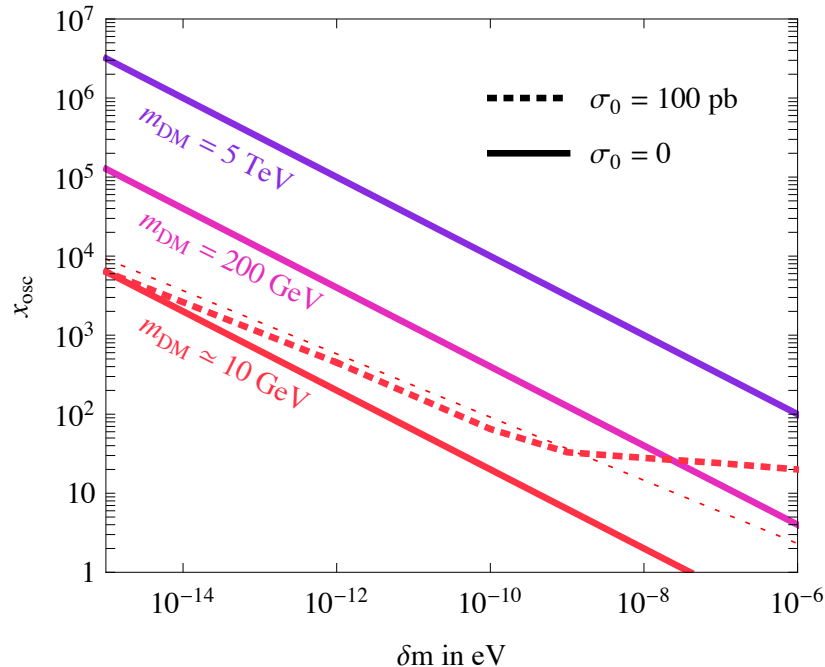
In case F a **very large initial asymmetry** is assumed. Having adopted a relatively small  $\delta m$ , oscillations start late but **still efficient depletion** is reached. Much higher asymmetry wrt  $\eta_B$  in the dark sector possible.



# Overview of general features:

1. annihilation cross sections *higher* than usual  $\sigma_0$  are needed to reach the correct abundance!

2. oscillations start *later* than a simple guess  $\sim 1/\delta m$ , due to decoherence effects.

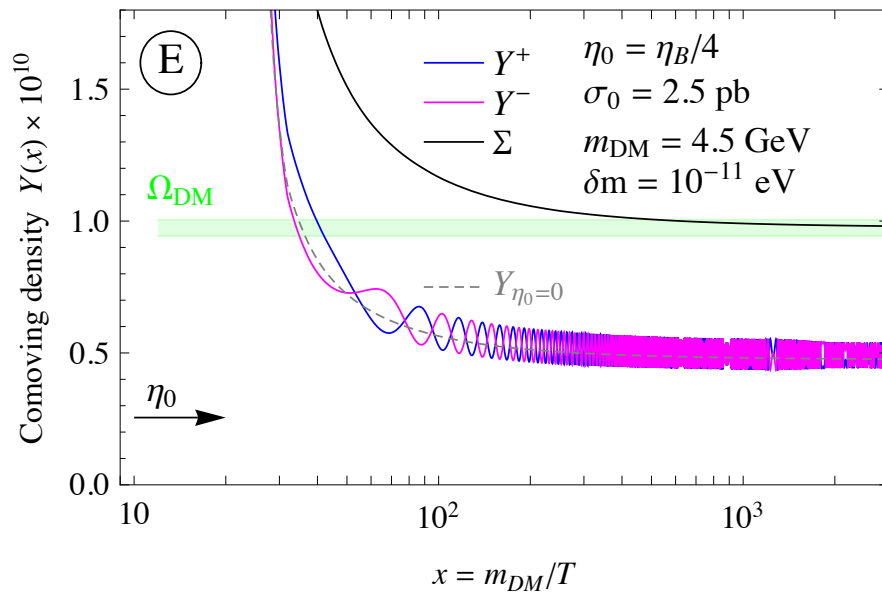


$$x_{\text{osc}} \simeq H/\delta m$$

$$x_{\text{osc,ann}} \simeq \left( \frac{H_m \gamma_a}{2 \delta m^2} \right)^{1/2} \simeq \left( \frac{H_m \sigma_0 s_m \eta_0 / 2}{\delta m^2} \right)^{1/5}$$

# Overview of general features:

3. oscillations can modify DM thermal history only for sufficiently small  $\delta m < \delta m_{\text{max}}$ .



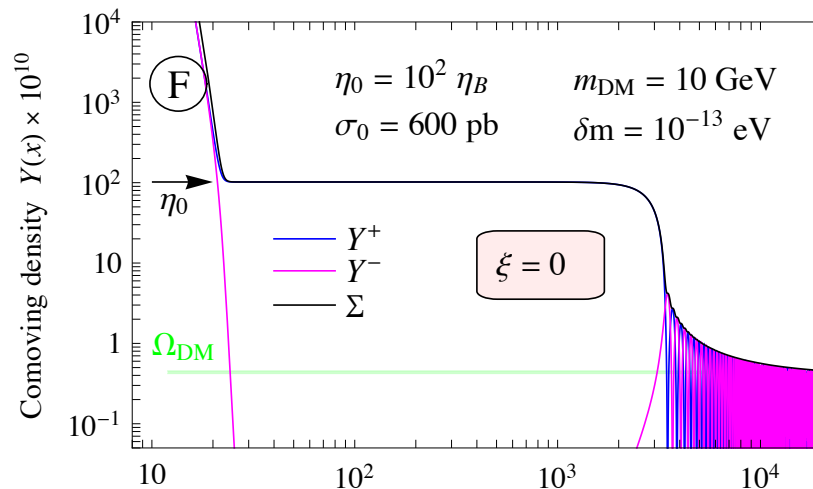
For too large  $\delta m$  oscillations start too early and symmetrize the dark sector → *usual WIMP scenario!*

# Phenomenological constraints:

In these scenarios DM consists of equal portions of DM and anti-DM and can **self-annihilate** at late epochs.

*Usual WIMP (+ novel) indirect detection signatures.*

i) **BBN**: if oscillations start after the end of BBN, i.e. if  $t_{\text{osc}} > t_{\text{BBN}}$ , as annihilations recouple, a large amount of energy is injected into the plasma. The set-up is similar to the one of late-decaying heavy DM progenitor states. However, other constraints stronger and imply  $t_{\text{osc}} < \sim 0.1$  sec...



# Phenomenological constraints:

In these scenarios DM consists of equal portions of DM and anti-DM and can **self-annihilate** at late epochs.

*Usual WIMP (+ novel) indirect detection signatures.*

i) **CMB**: energy injected from DM annihilation during recombination ( $z \sim 1100$ ), results in an increased amount of free electrons, which survive to lower redshifts and affect the CMB anisotropies.

Limits on  $\sigma_0$  set using **WMAP-7** data and **ATACAMA** telescope data, for DM annihilation channels to  $e^+e^-$  and  $\mu^+\mu^-$ .

[Galli et al., Phys.Rev.D84 (2011)]

## Phenomenological constraints:

In these scenarios DM consists of equal portions of DM and anti-DM and can self-annihilate at late epochs, as in usual WIMP scenarios.

iii) **Present time annihilations:** *Fermi-LAT observation (non-detection) of dwarf spheroidal Galaxies*. Stringent upper limits are derived by applying a joint likelihood analysis to 10 satellite galaxies with 2 years of FERMI-LAT data, and taking into account the uncertainty in the dark matter distribution in the satellites.

[Fermi-LAT collaboration, [arXiv:1108.3546v2](https://arxiv.org/abs/1108.3546v2)]

The limits are particularly strong for hadronic annihilation channels ( $q\bar{q}$ ) and  $\tau^+\tau^-$ . These limits are somewhat weaker for  $e^+e^-$  and  $\mu^+\mu^-$ , as diffusion of leptons out of these systems is poorly constrained.

## Phenomenological constraints:

In these scenarios DM consists of equal portions of DM and anti-DM and can self-annihilate at late epochs, as in usual WIMP scenarios.

iii) **Present time annihilations:** *HESS observation of the Galactic Center halo region.*

Due to the high energies covered by ACTs these limits are specially relevant for heavy  $> \sim 1 \text{ TeV}$  DM.

This refers to a  $q\bar{q}$  annihilation channel and assumes that the DM distribution in the Galaxy follows a **cuspy** profile ( $\sim$ NFW). *These constraint are lifted in case of a **cored profile!***

[ H.E.S.S. Collaboration, arXiv:1103.3266]

# Comparing

Buckley+Profumo, 1109.2164v1

- simplified Boltzmann formalism, with constant oscillation rate:
  - no oscillations
  - no accounting for decoherence
- no scatterings on plasma
  - no accounting for decoherence
- not concerned w obtaining correct  $\Omega_{\text{DM}} h^2$

This work, 1110.3809

- ✓ full matrix formalism
  - oscillations
  - accounting for decoherence
- ✓ scatterings on plasma
  - accounting for decoherence
- ✓ requires correct  $\Omega_{\text{DM}} h^2$

Quantitatively:

- evolution is almost always very different
- final abundances differ (a few to more than one order of magnitude)

