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Multiplicity Dependence of Two-Particle Correlations in Proton-Proton Collisions

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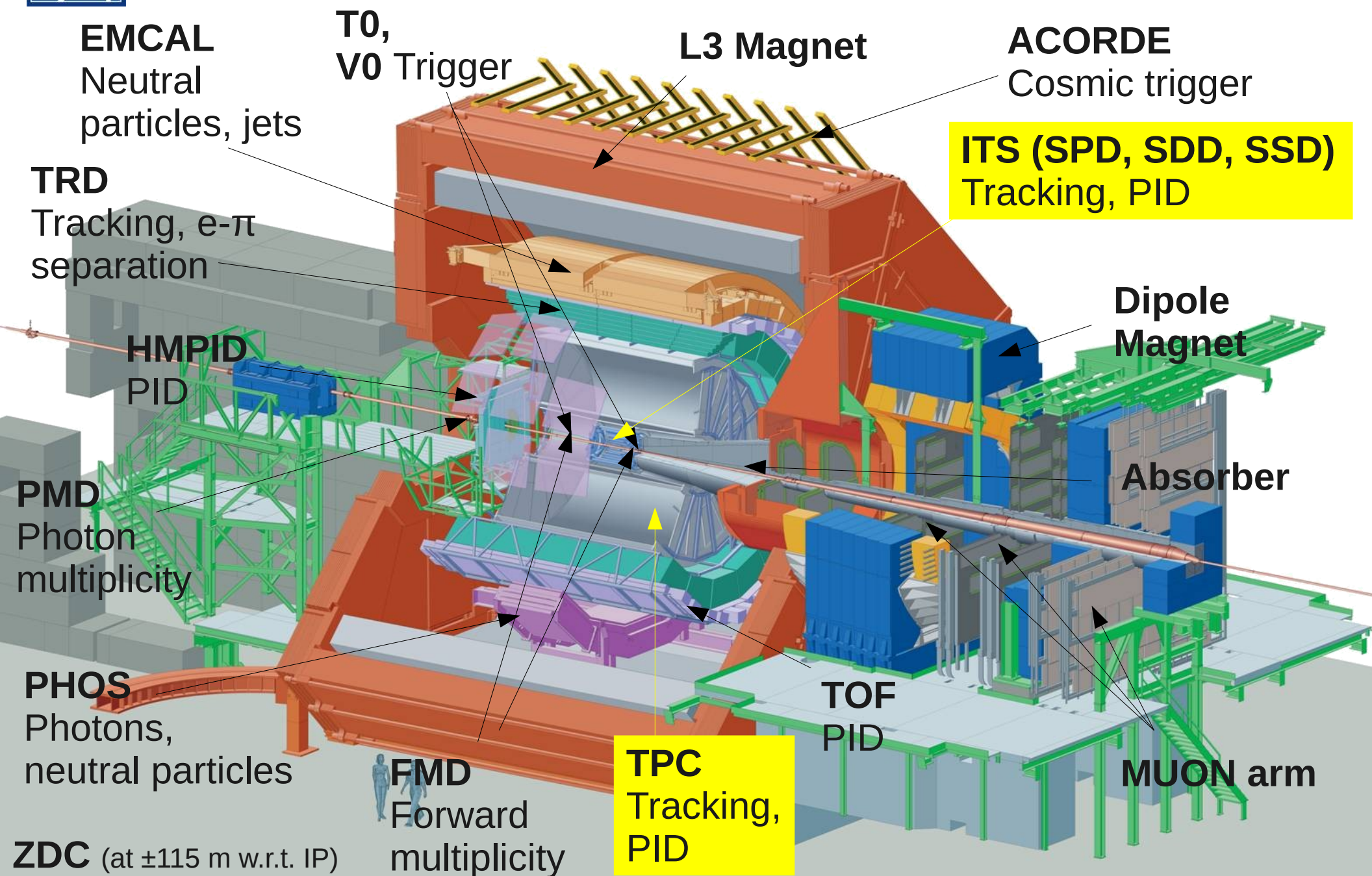
A Large Ion Collider Experiment



- ALICE is designed to study heavy-ion (Pb-Pb) collisions and also proton-proton (pp) collisions
 - Several signals in heavy-ion collisions are measured relative to pp
 - ALICE also has a rich pp program
- ALICE special features for pp minimum bias physics
 - Low momentum sensitivity due to low material budget and low magnetic field
 - Excellent primary and secondary vertex resolution
 - Excellent Particle Identification (PID) capability
- ALICE can give important input to pp studies
 - Rare signals need good description of soft underlying event
 - Tuning of MC generators in low- p_T region
 - Study of high-multiplicity collisions



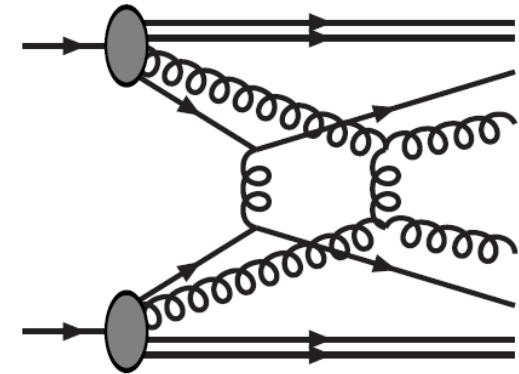
A Large Ion Collider Experiment



Analysis Motivation

- High-energy proton-proton collisions can be interpreted as collisions of two “bunches of partons”
- → when two protons collide, it is possible that multiple distinct pairs of partons collide with each other

→ Multiple parton interactions (MPI)



- MPIs presumably have impact on multiplicity distribution, jets, and the underlying event
- Is it possible to measure multiple parton interactions, e.g. the number and the corresponding particle yield?
 - Possible access to MPI via **jets** and **mini-jets**

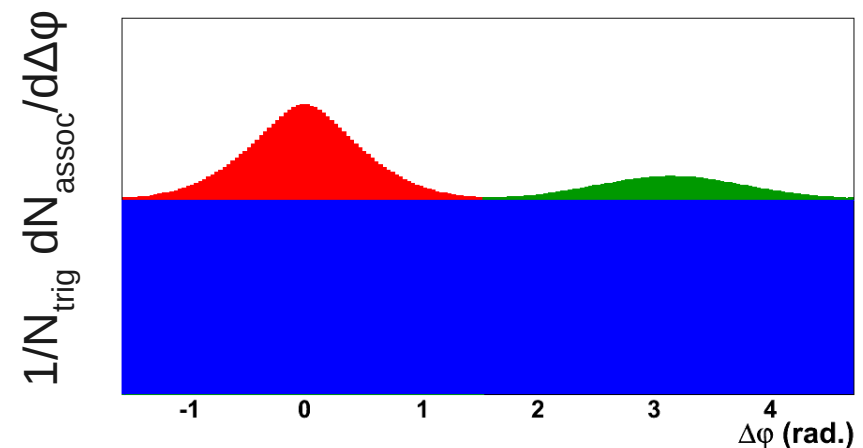
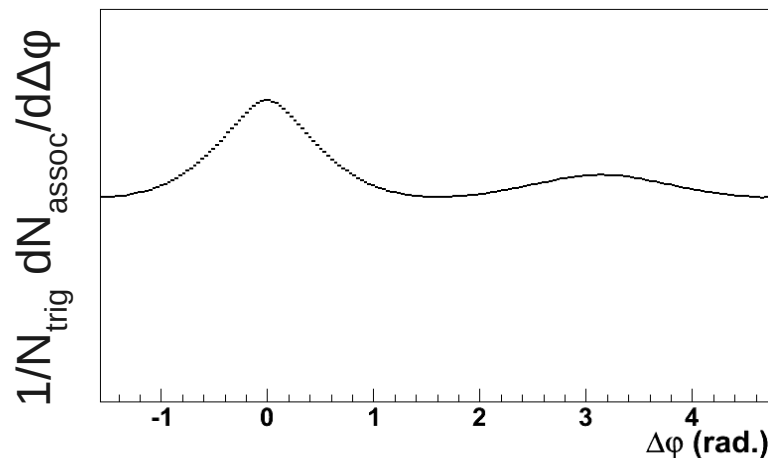
Motivation of Analysis Approach

- Investigate properties of jets and low energetic “mini-jets” and their contribution to the event multiplicity
 - “Mini-Jets” are particles from “hard scattering”, which have too low energy in comparison to the underlying event, and which therefore can not be reconstructed event-by-event
 - But, there is a possibility to access mini-jet properties via two particle correlations averaged over many events
- Different correlation approaches:
 1. Correlation with one leading particle, particles with highest transverse momentum
 - Bias to hard momentum scale (increase of $p_{T,max}$ with $N_{charged}$)
 2. Triggered, inclusive correlations between all tracks with $p_T > p_{T,trig}$ and $p_T > p_{T,assoc}$ using $p_{T,trig} > p_{T,assoc}$
 - Attention: possible bias due to unwanted combinatorics of correlated trigger particles
- Both methods have drawbacks for mini-jet measurements

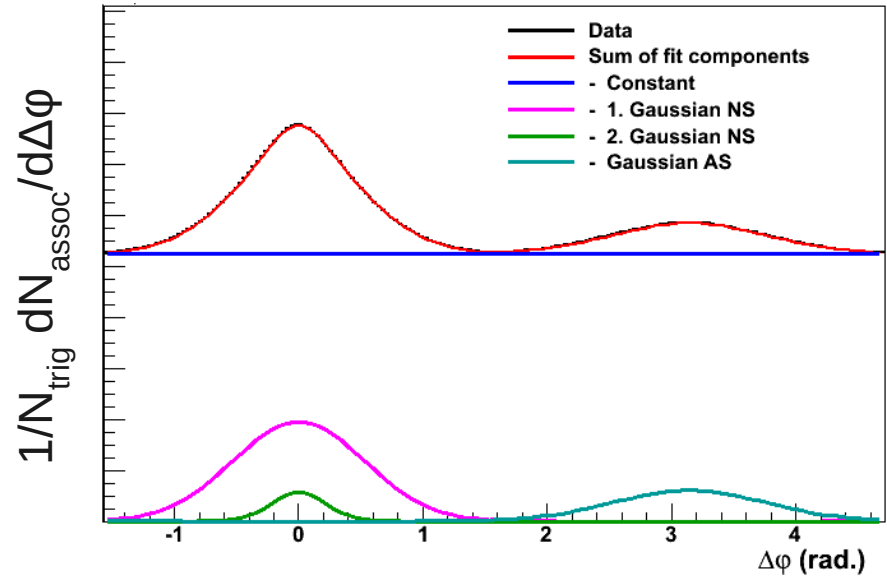
- Associated per-trigger yield as function of azimuthal angle φ and multiplicity N_{charged}
- Several trigger-particle per event
- $p_{T,\text{trig}} > 0.7$ GeV/c or higher
- $p_{T,\text{assoc}} > 0.4$ (0.7) GeV/c or higher

$$\frac{d^2 N}{d \Delta \varphi d N_{ch}} (\Delta \varphi, N_{ch}) = \frac{1}{N_{\text{trig}}} \frac{d^2 N_{\text{assoc}}}{d \Delta \varphi d N_{ch}}$$

- Associated per-trigger yield can be computed for different
 - $N_{ch}, p_{T,\text{trig}}, p_{T,\text{assoc}}$
- Comparison of single correlation properties instead of comparison of the complete distribution
 - e.g. per-trigger yield in combinatorial background, per-trigger “near side” yield, per-trigger “away side” yield



$$f(\Delta\varphi) = C + A_1 e^{-\frac{\Delta\varphi^2}{2\sigma_1^2}} + A_1 e^{-\frac{(\Delta\varphi-2\pi)^2}{2\sigma_1^2}} + A_2 e^{-\frac{\Delta\varphi^2}{2\sigma_2^2}} + A_2 e^{-\frac{(\Delta\varphi-2\pi)^2}{2\sigma_2^2}} + A_3 e^{-\frac{(\Delta\varphi-\pi)^2}{2\sigma_3^2}} + A_3 e^{-\frac{(\Delta\varphi+\pi)^2}{2\sigma_3^2}}$$



- The fit function is a combination of a constant and periodically continuing Gaussian functions
- Data and fit are in good agreement with each other
- Extract correlation observables from fit and derive final observable

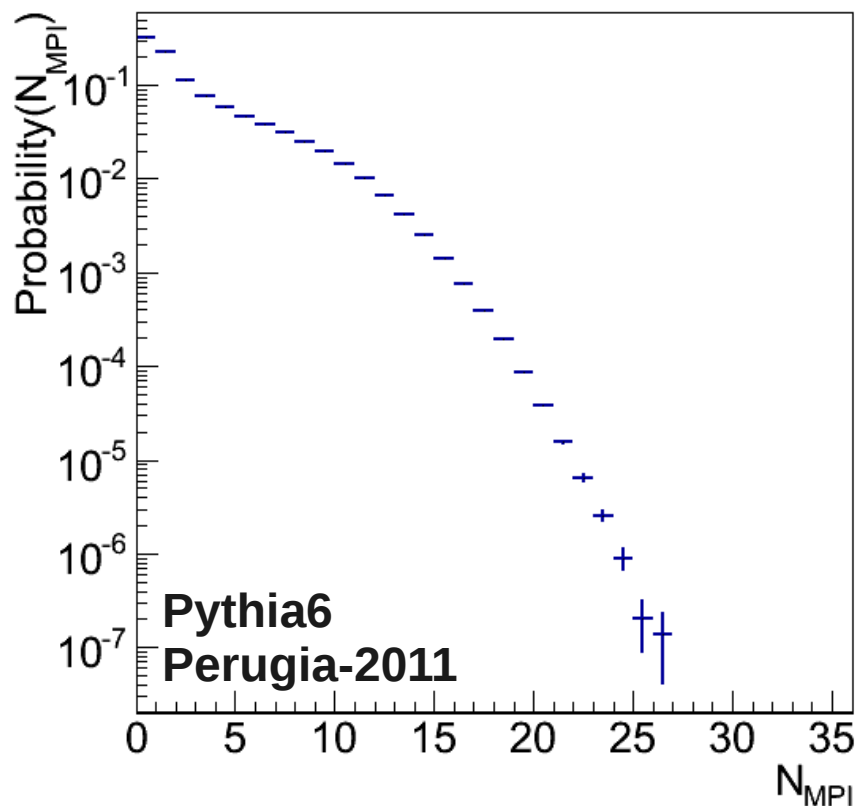
$$\langle N_{const} \rangle = \frac{1}{N_{trig}} \text{Constant}$$

$$\langle N_{assoc, near side} \rangle = \frac{1}{N_{trig}} \sqrt{2\pi} (A_1 \sigma_1 + A_2 \sigma_2)$$

$$\langle N_{assoc, away side} \rangle = \frac{1}{N_{trig}} \sqrt{2\pi} (A_3 \sigma_3)$$

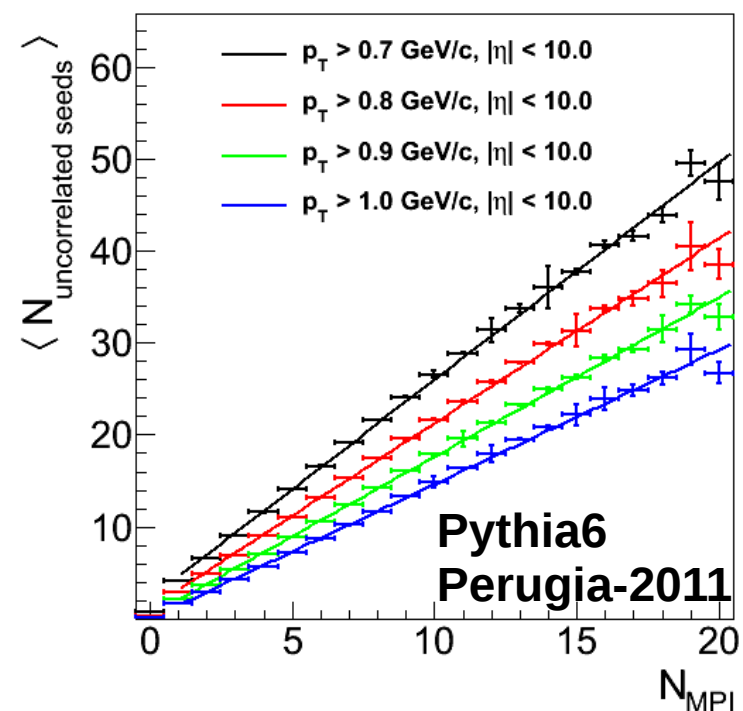
$$\langle N_{uncorrelated seeds} \rangle = \frac{\langle N_{trig} \rangle}{\langle 1 + N_{assoc, near}(p_T > p_{T, trig}) + N_{assoc, away}(p_T > p_{T, trig}) \rangle}$$

Assumption: Sensitivity on MPI



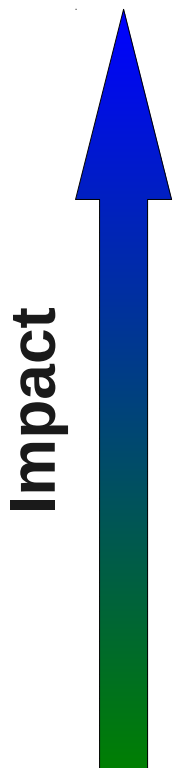
- Pythia simulations are based on multiple parton interactions (MPI)
- Pythia-MPI = number of (semi-)hard scatterings that occurred in the current event in the multiple interaction scenario

- Check dependency between N_{MPI} and $\langle N_{uncorrelated\ seeds} \rangle = \frac{\langle N_{trig} \rangle}{\langle 1 + N_{assoc, near + away}(p_T > p_{T, trig}) \rangle}$

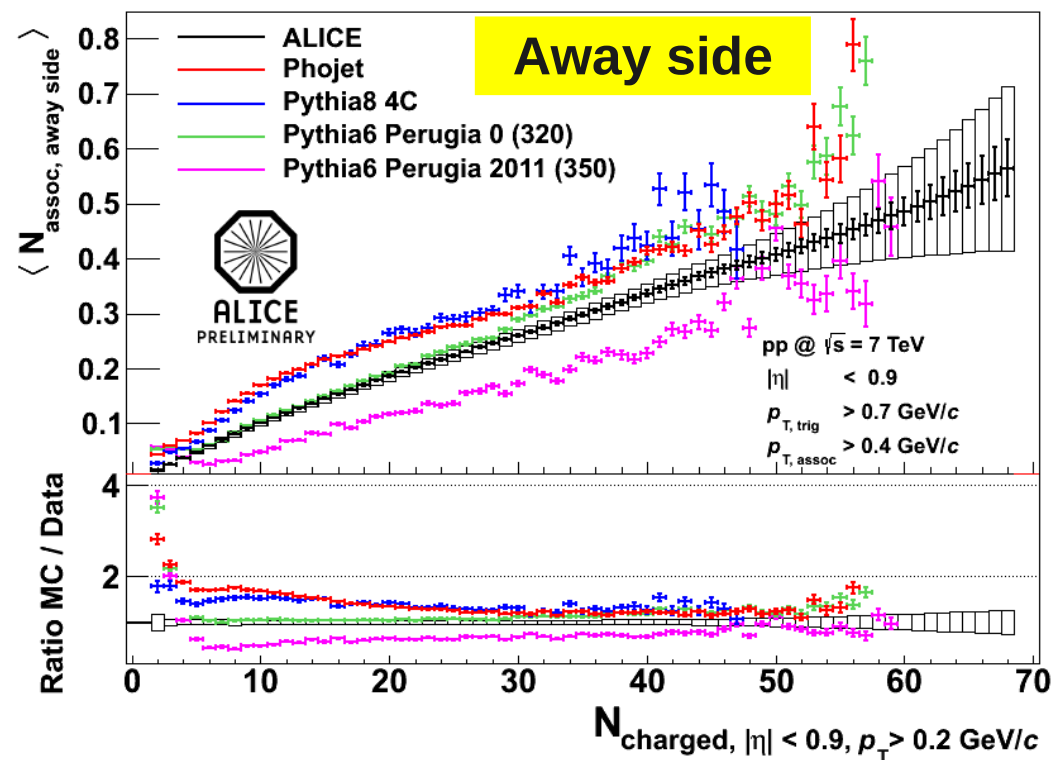
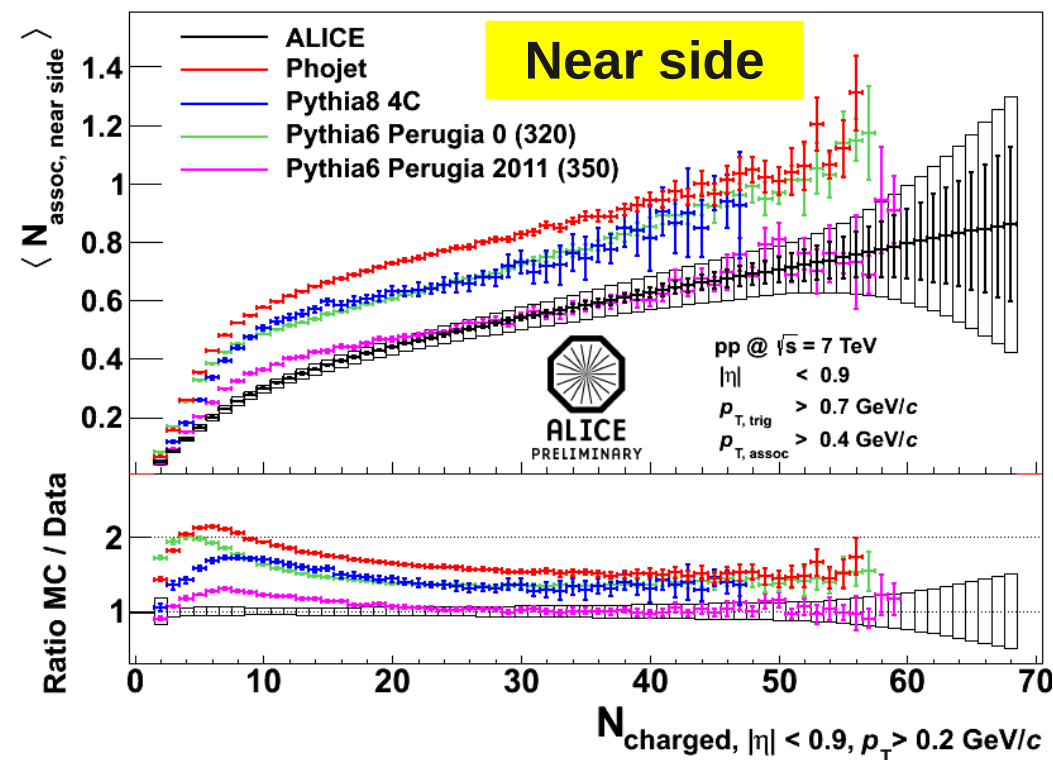


- Dependence is approximately linear
→ **Analysis can probe MPI**
- See backup slides for more details

- Data (including ITS and TPC)
 - pp @ $\sqrt{s} = 0.9$ TeV:
 - 7 million events
 - pp @ $\sqrt{s} = 2.76$ TeV:
 - 34 million events
 - pp @ $\sqrt{s} = 7.0$ TeV:
 - 270 million events
- Event cuts
 - Minimum bias trigger (hit in V0 or SPD)
 - One distinct reconstructed vertex within $|z_{\text{vertex}}| < 10$ cm of good quality
 - At least one track in ITS-TPC acceptance ($p_T > 0.2$ GeV/c, $|\eta| < 0.9$)
- Track cuts
 - Full refit procedure during the tracking in ITS and TPC
 - At least 1 hit per track in one of the first 3 ITS layers (first 3 out of 6)
 - At least 70 clusters per track in the TPC drift volume (out of 159)
 - $\chi^2/\text{TPC cluster} < 4$
 - Reject tracks with kink topology
 - p_T dependent DCA_{xy} cut corresponding to 7σ of track distribution ($\text{DCA}_{xy,\text{max}} = 0.3$ cm)
 - $\text{DCA}_z < 2$ cm

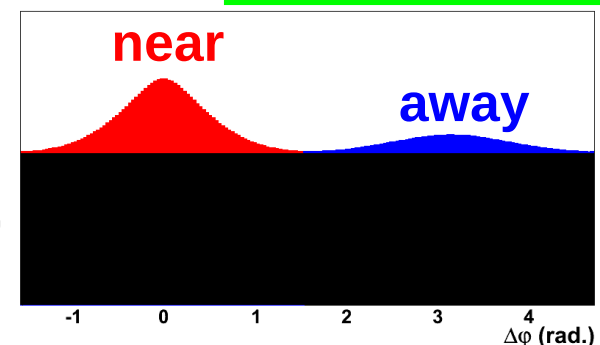


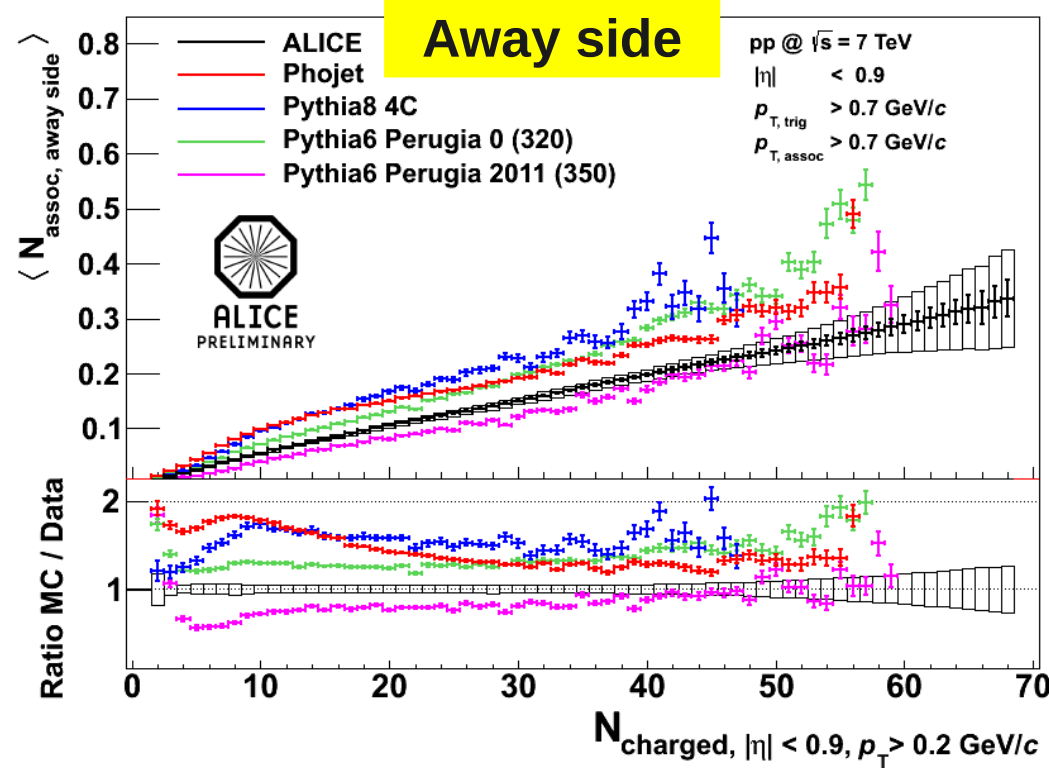
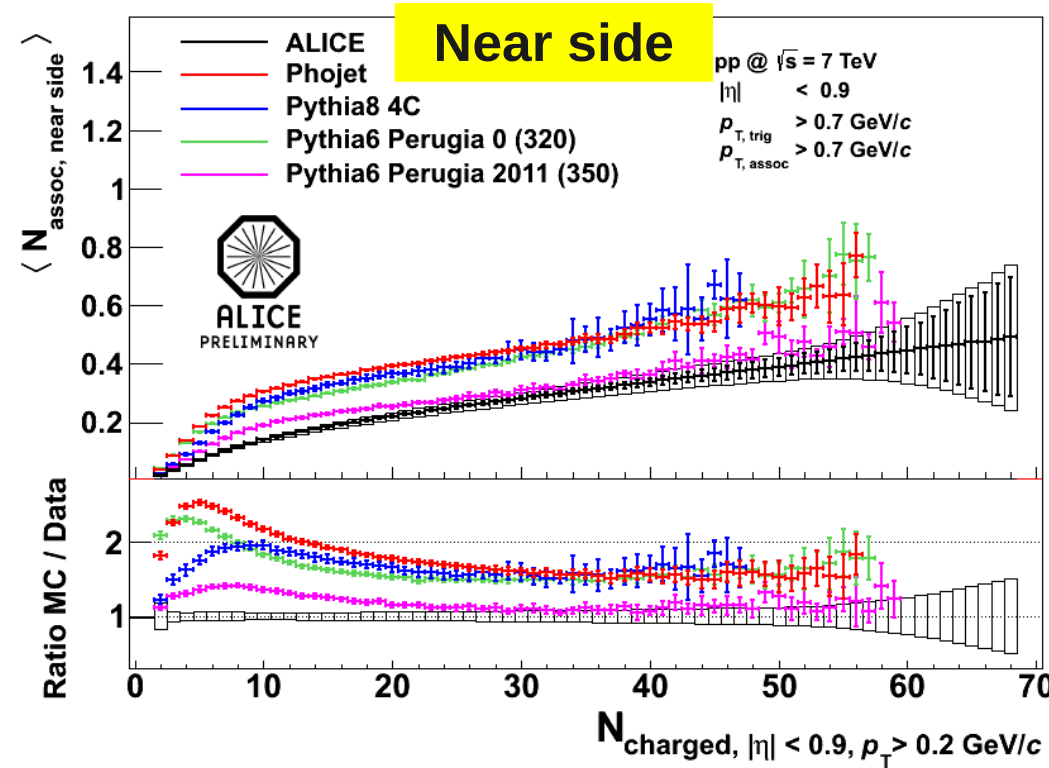
- Correction chain
 - Reconstruction efficiency
 - Contamination with tracks from secondary particles
 - Two-track and detector effects
 - Multiplicity correction
 - Contamination from strange particles
 - Vertex reconstruction efficiency
 - Trigger efficiency
- Sources of systematic uncertainties
 - Uncertainty of ITS-TPC efficiency
 - Particle composition in MC
 - Track cut dependence
 - Correction procedure
 - Event generator dependence
 - Transport MC dependence
 - Signal extraction
 - Vertex quality cut dependence
 - Pileup events
 - Influence of resonances
 - Material budget
 - Strangeness correction



- Per-trigger yield at near and away side rises with N_{charged}
- Near side yield is overestimated by Phojet, Pythia8, and Pythia6 Perugia-0 by up to 100%, while P2011 agrees well
- Away side is underestimated by Perugia-2011 by up to 50%, best agreement between ALICE data and Perugia-0

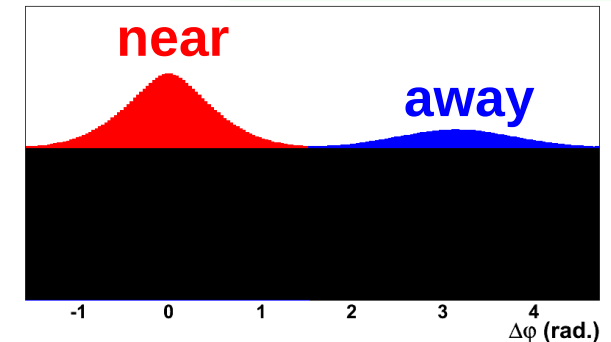
$p_{T, trig} > 0.7 \text{ GeV}/c$
 $p_{T, assoc} > 0.4 \text{ GeV}/c$

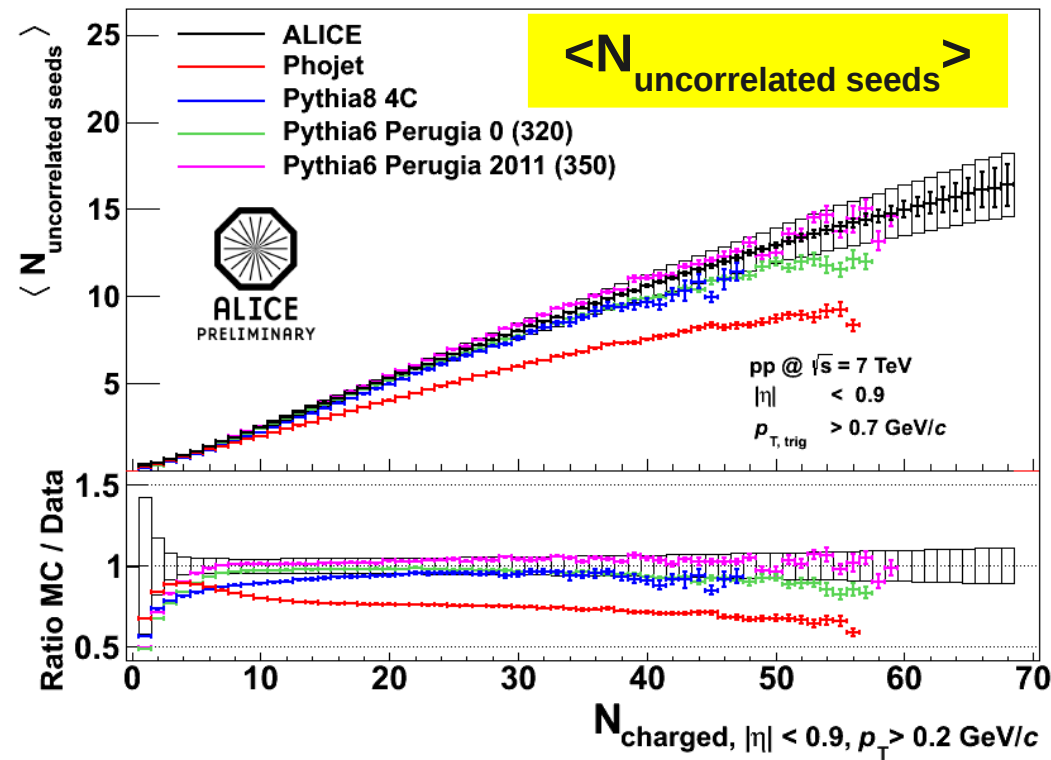
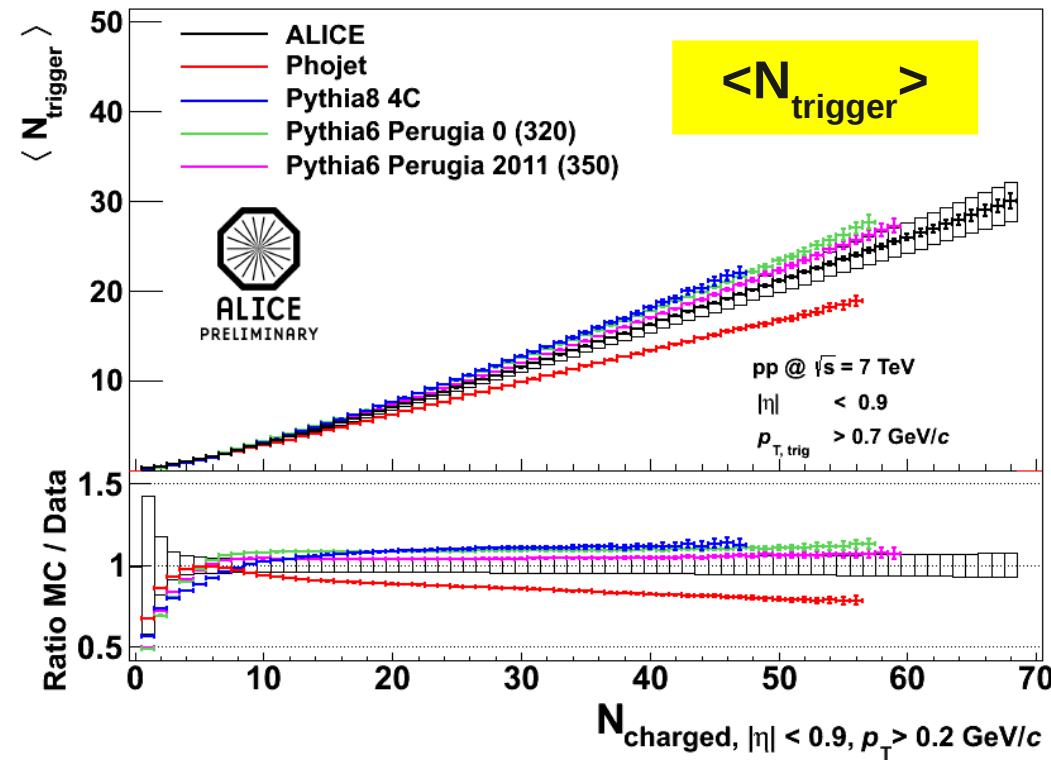




- Per-trigger yield at near and away side rises with $N_{charged}$
- Near side yield is overestimated by Phojet, Pythia8, and Pythia6 Perugia-0 by up to 100%, while P2011 agrees well
- Away side is underestimated by Perugia-2011 by up to 50%

$p_{T, trig} > 0.7 \text{ GeV}/c$
 $p_{T, assoc} > 0.7 \text{ GeV}/c$

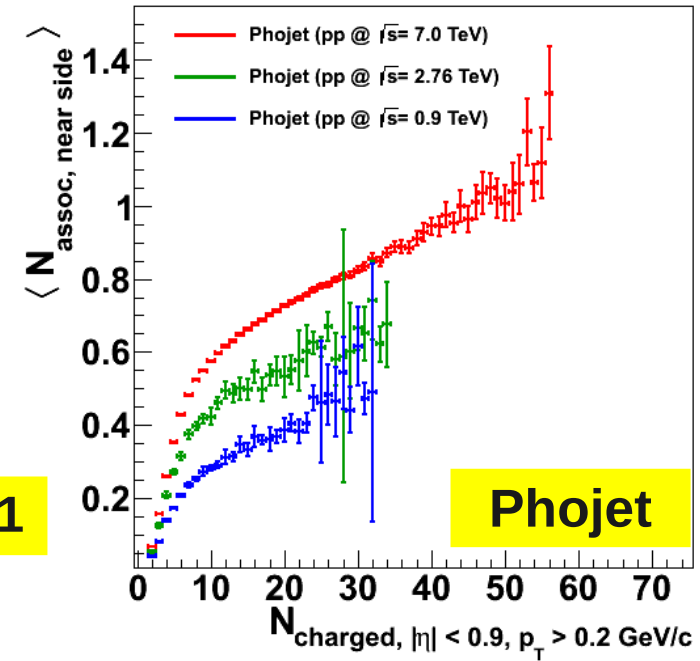
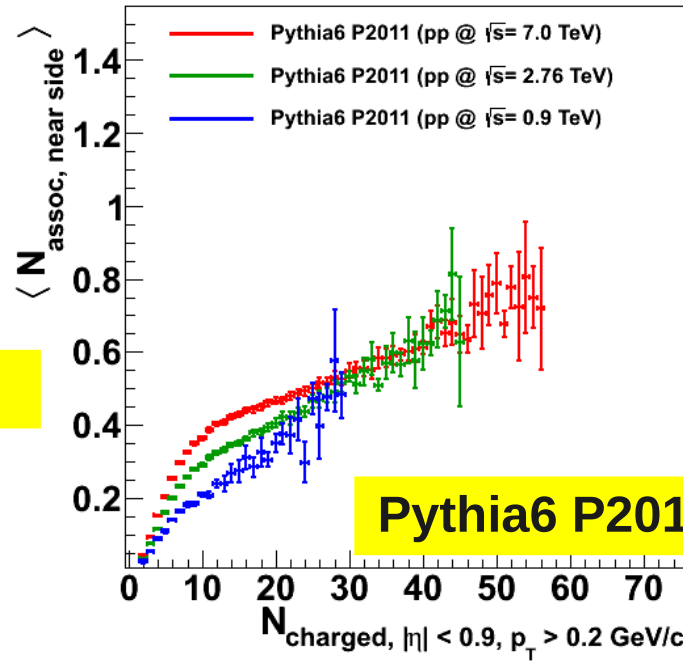
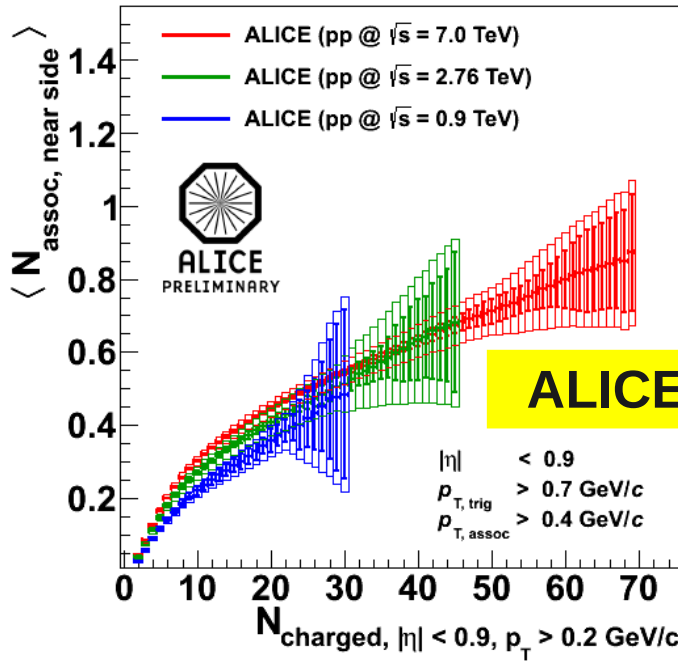




- Number of trigger particles ($p_T > 0.7 \text{ GeV}/c$) rises stronger than linear with N_{charged}
 \rightarrow rise of mean- p_T with N_{charged}
- Phojet is much softer while Pythia tunes reproduce data fairly well

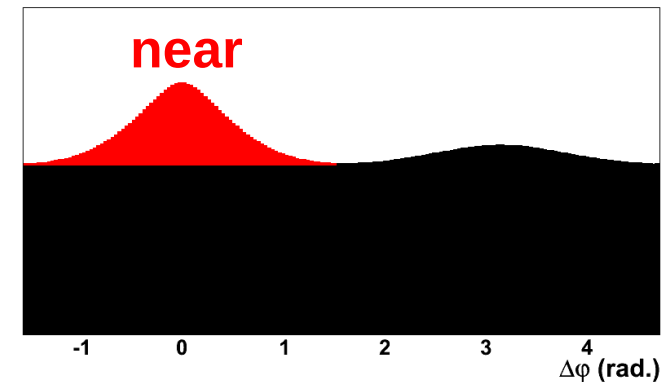
$$\langle N_{\text{uncorrelated seeds}} \rangle = \frac{\langle N_{\text{trig}} \rangle}{\langle 1 + N_{\text{assoc, near+away}}(p_T > p_{T,\text{trig}}) \rangle}$$

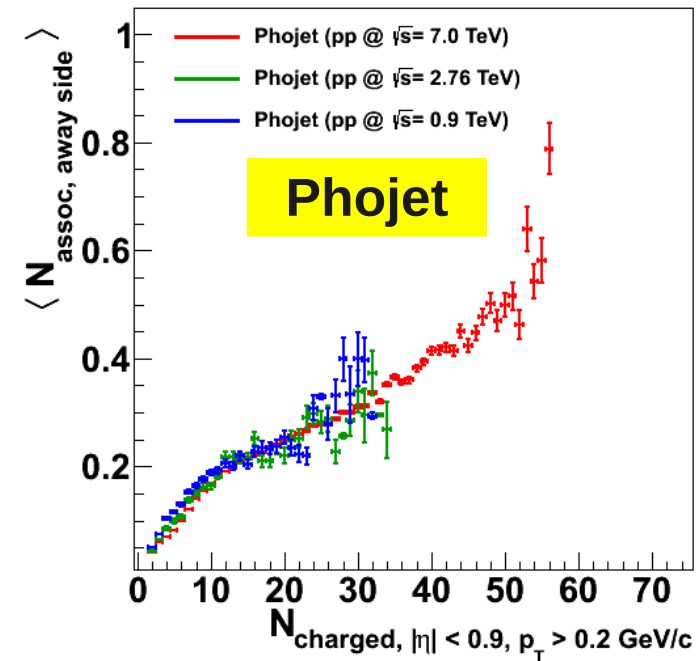
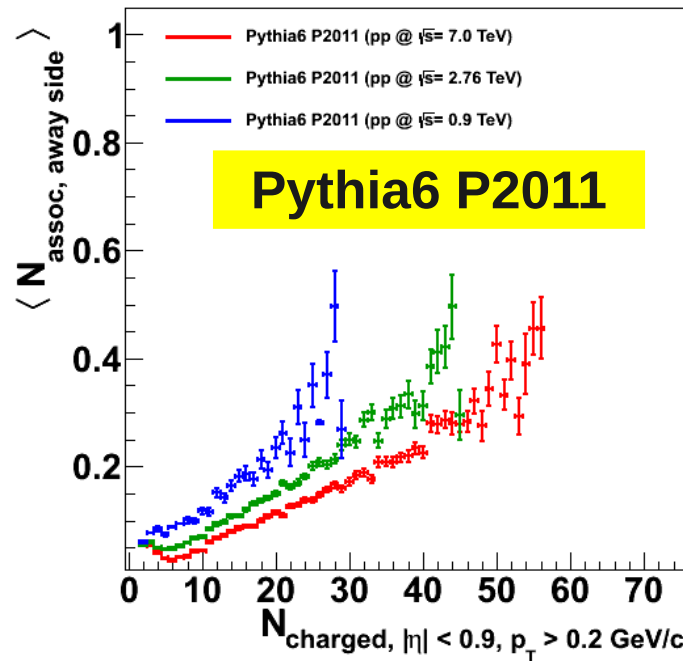
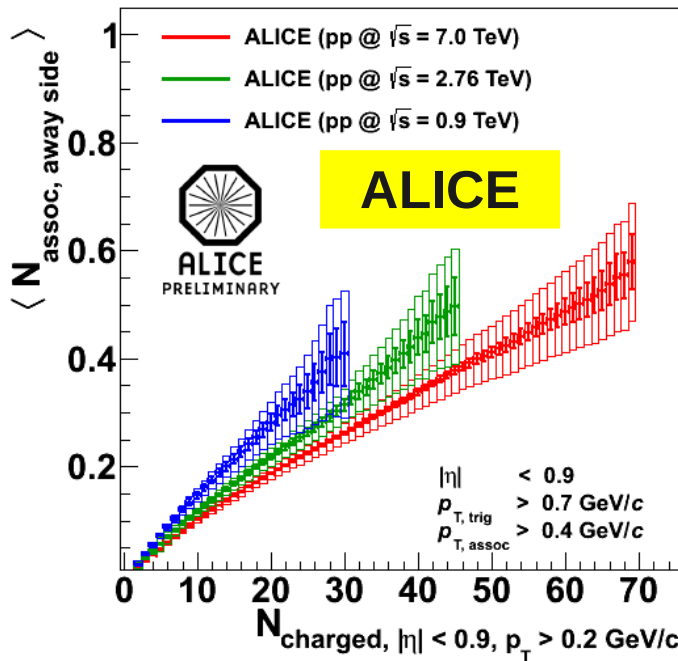
- At low and intermediated multiplicities, $N_{\text{uncorrelated seeds}}$ rises linearly with multiplicity



- Near side yield at same multiplicity bin grows with increasing center-of-mass energy
- Splitting between slopes for different \sqrt{s} is largest for Phojet

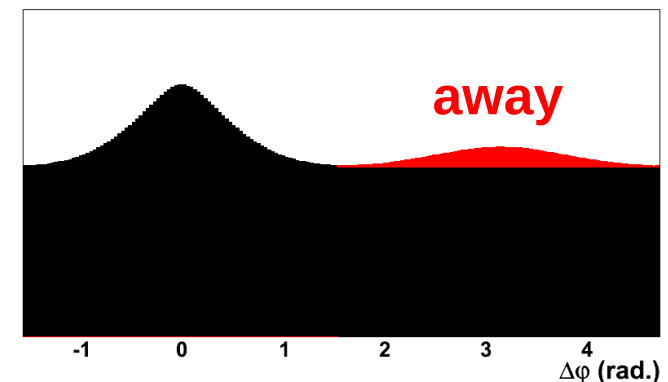
$p_{T, \text{trig}} > 0.7$ GeV/c
 $p_{T, \text{assoc}} > 0.4$ GeV/c

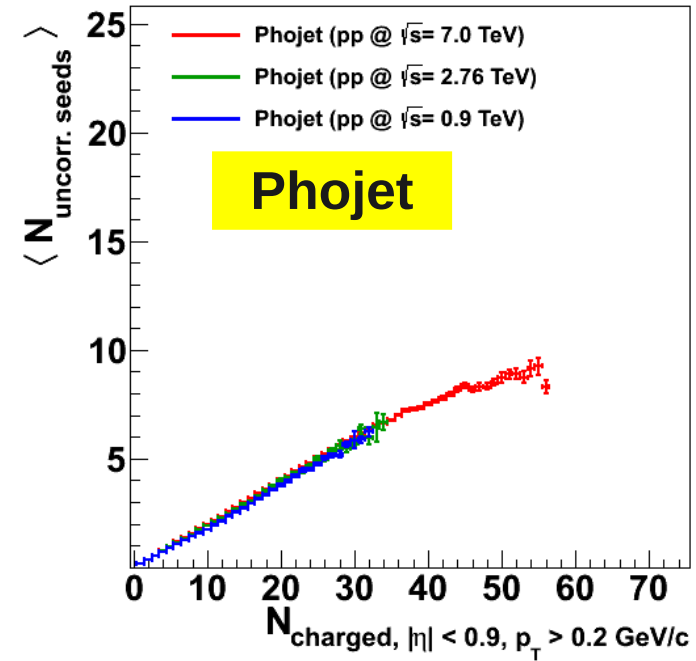
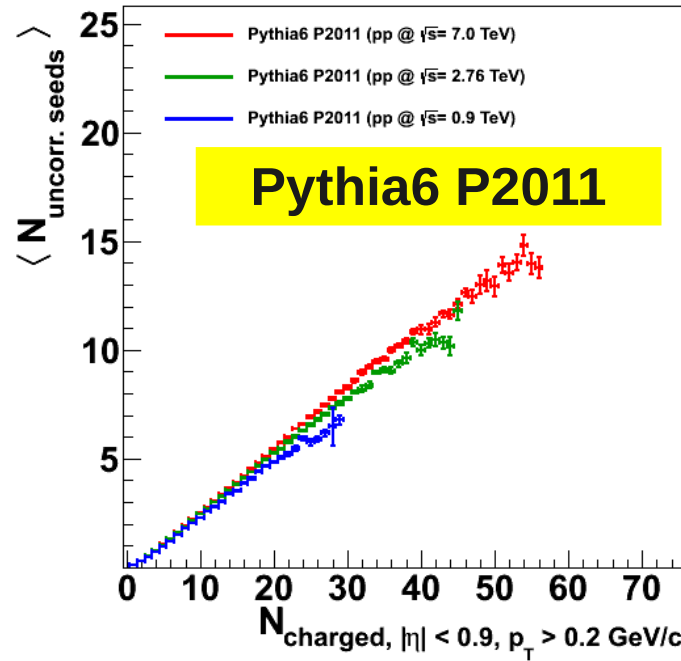
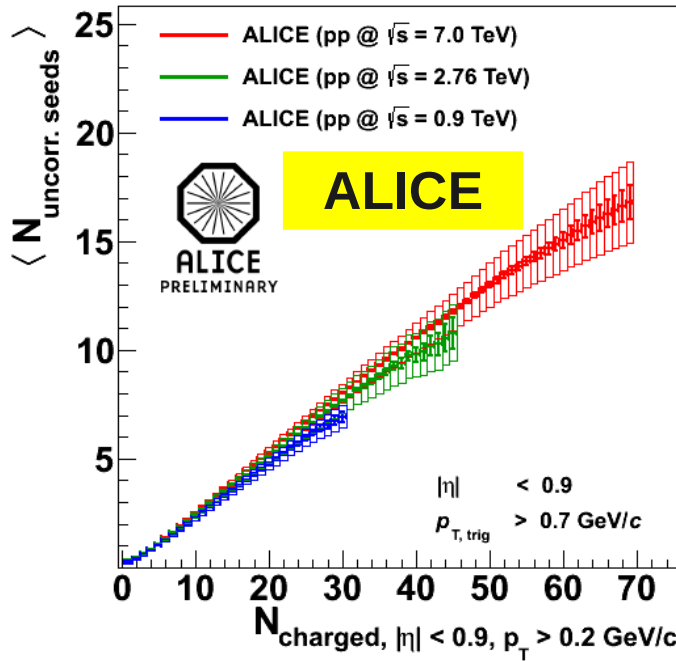




- Away side yield at same multiplicity bin shrinks with increasing \sqrt{s}
- Pythia6 Perugia-2011 underestimates ALICE data
- Phojet shows almost no \sqrt{s} dependence

$p_{T, \text{trig}} > 0.7$ GeV/c
 $p_{T, \text{assoc}} > 0.4$ GeV/c

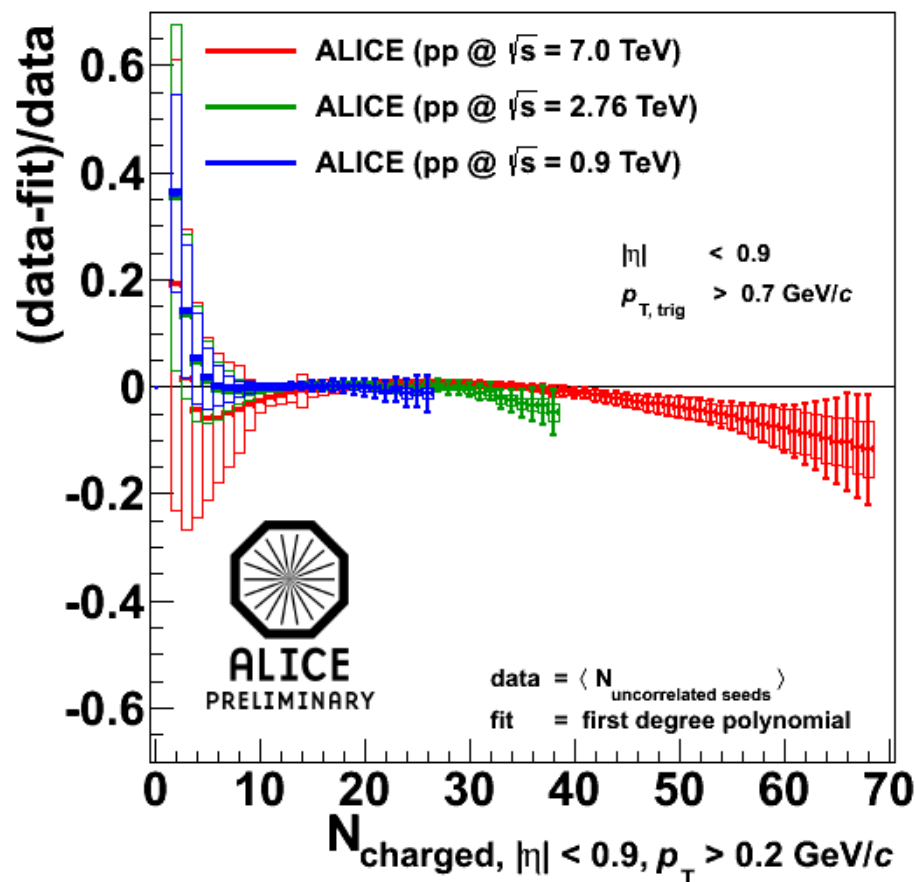
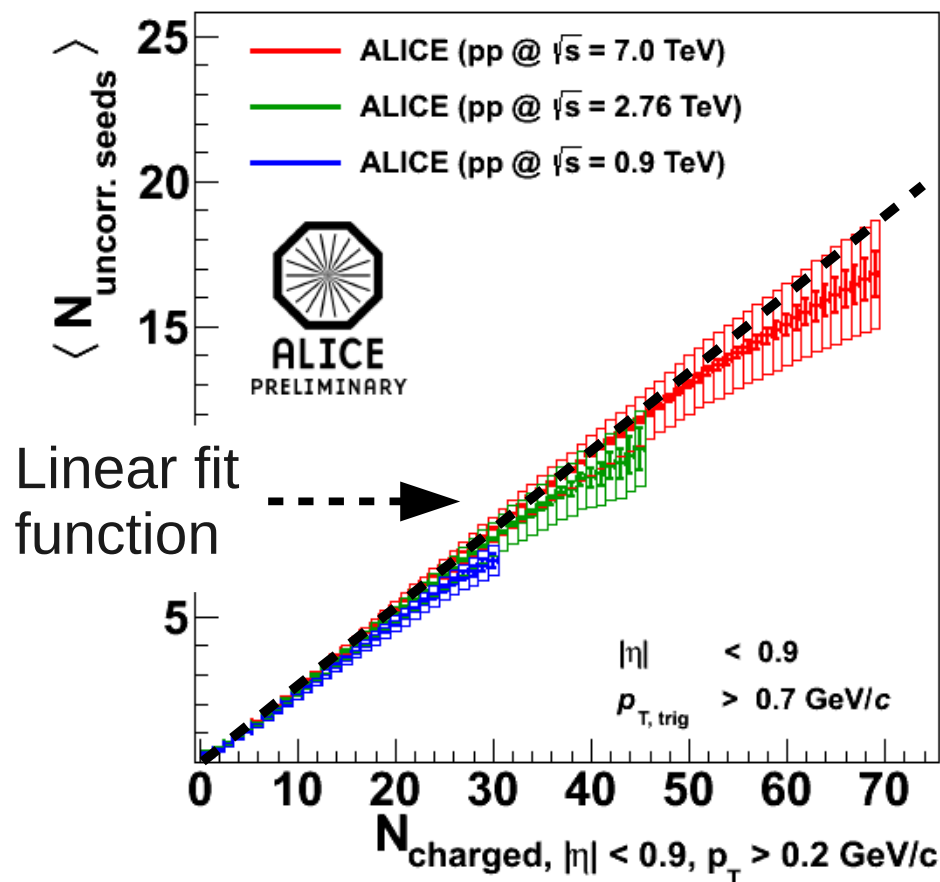




$$\langle N_{\text{uncorrelated seeds}} \rangle = \frac{\langle N_{\text{trig}} \rangle}{\langle 1 + N_{\text{assoc, near+away}}(p_T > p_{T, \text{trig}}) \rangle}$$

- Only small \sqrt{s} dependence
- In low and intermediate multiplicity region: $N_{\text{uncorr. seeds}}$ grows linearly with N_{charged}
- At high multiplicities, the number of $N_{\text{uncorr. seeds}}$ stagnates \rightarrow Multiplicity increase only by selecting events with highly populated jets, limit in N_{MPI}

$\langle N_{\text{uncorrelated seeds}} \rangle$ and linear fit



- Compare distribution with linear fit in intermediate N_{charged} range
- At high multiplicities, hint of deviation from linear dependence - this would indicate a limit in MPI

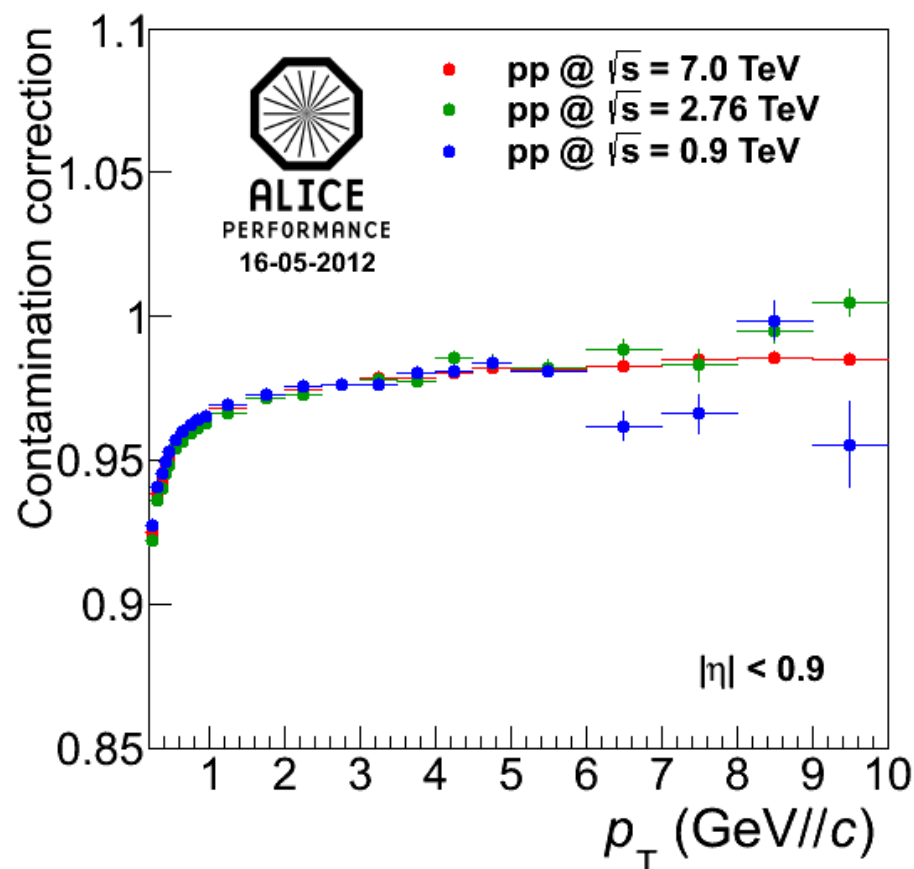
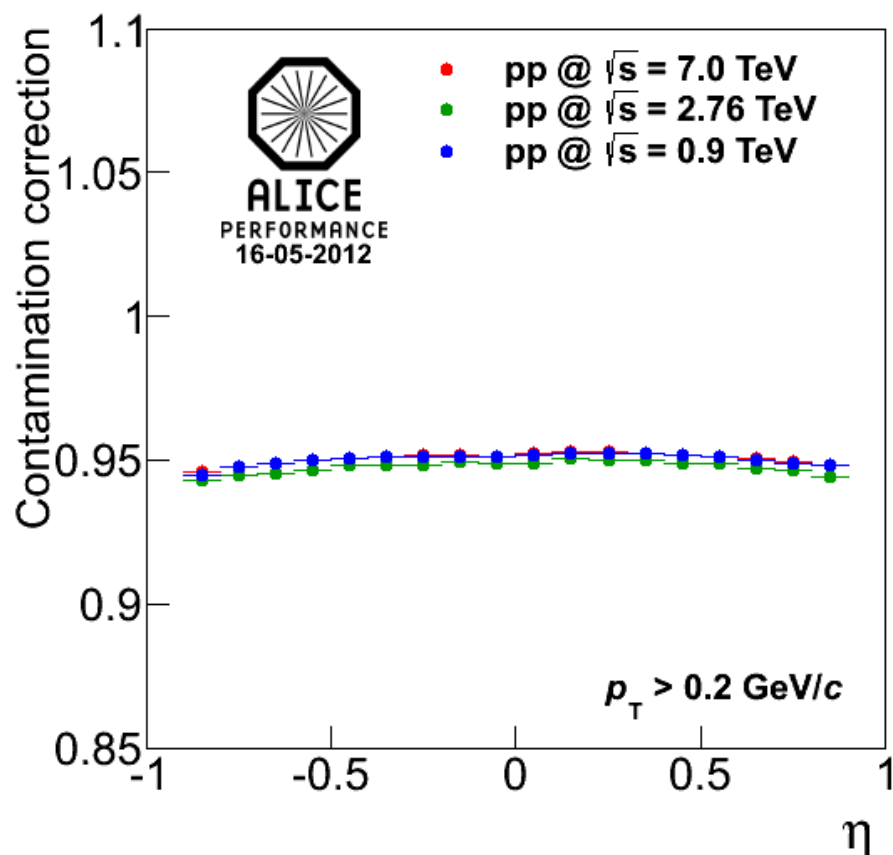
Summary

- Study of the per-trigger yield at the near side and the away side as well as the number of uncorrelated seeds using a two-particle correlation analysis
- Analysis of ALICE data at $\sqrt{s} = 0.9, 2.76, \text{ and } 7.0 \text{ TeV}$
- At high multiplicities, hint of deviation from linear dependence - this would indicate a limit in MPI
- Pythia studies show that the analysis approach can probe number of multi parton interactions (MPI)
- Pythia Perugia-2011 gives best description of ALICE results
 - However, at intermediate N_{charged} , the away side yield is underestimated by 50%
- Phojet, Pythia6-Perugia-0, and Pythia8 show large discrepancies to ALICE results
 - e.g. per-trigger near side yield is overestimated by all MCs by 100% at low and intermediated N_{charged}



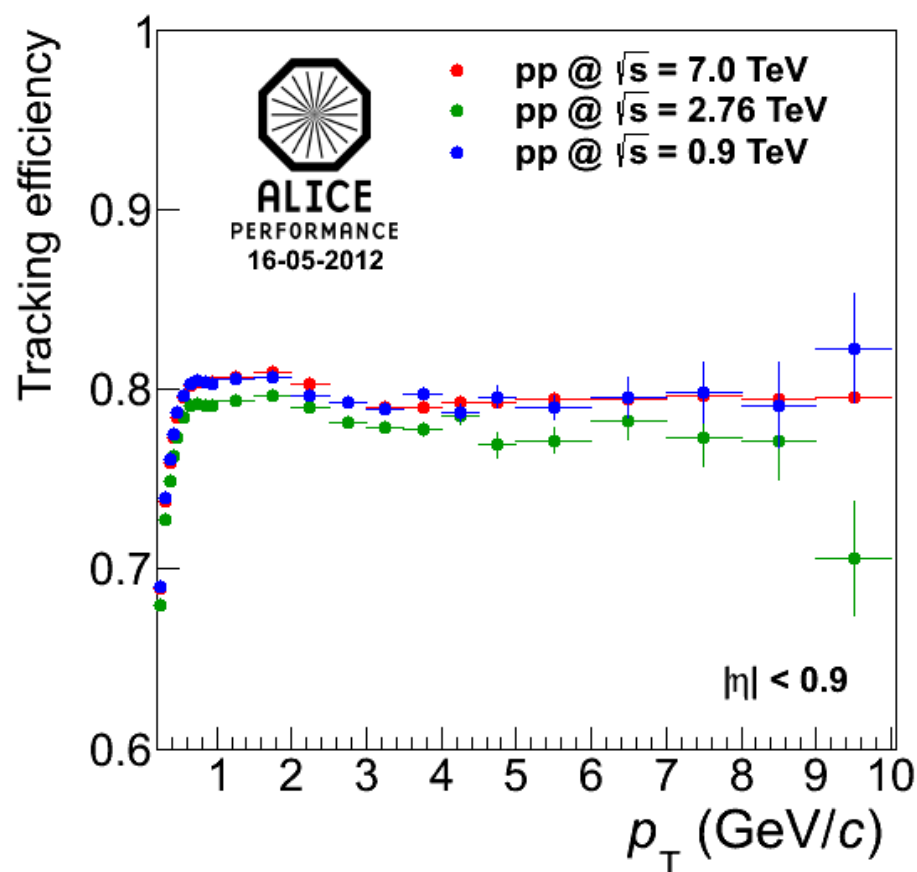
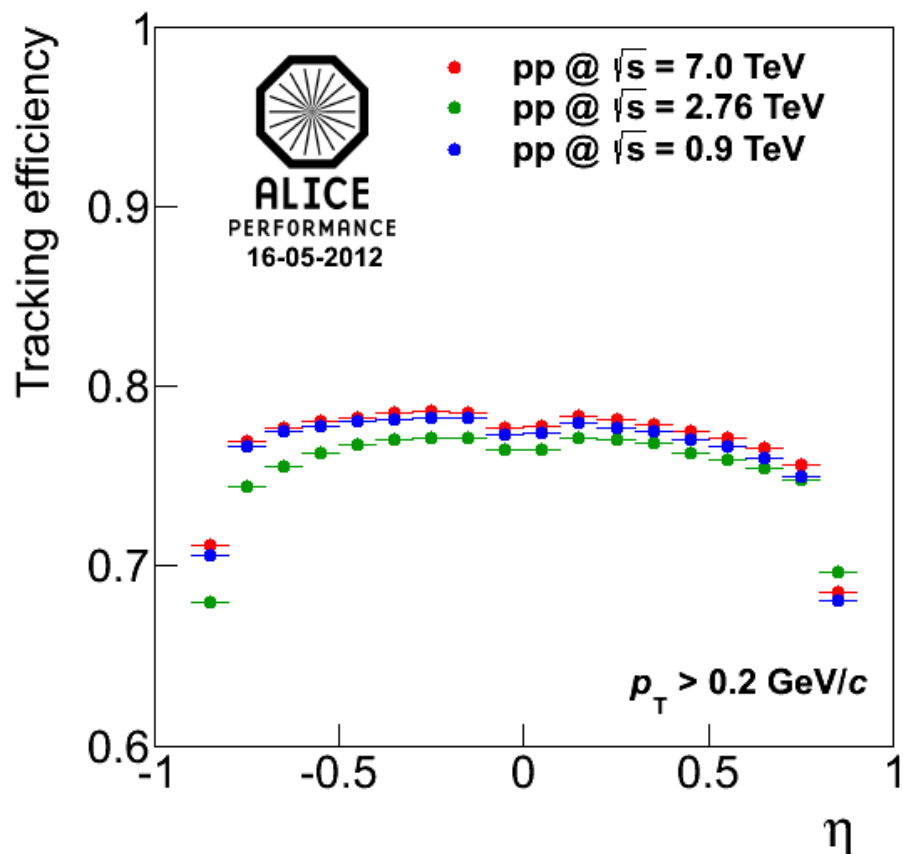
Backup





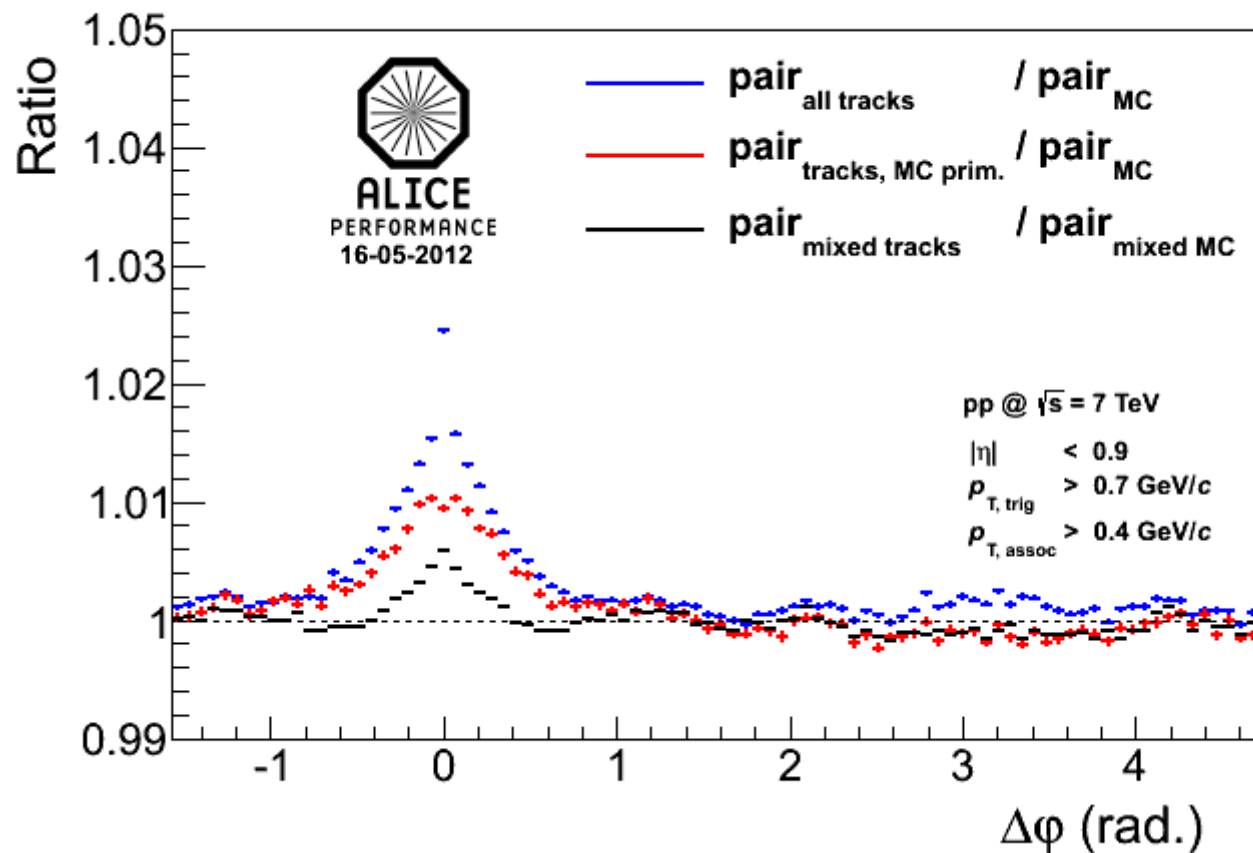
- Contamination of track sample from secondary particles shows p_T dependence, but almost no eta dependence
- Overall contamination $\sim 6\%$

- At high momenta, the statistics is low
- Estimate contamination by extrapolation from intermediate p_T



- Reconstruction efficiency shows strong p_T dependence and slight eta dependence
- Overall tracking efficiency is $\sim 80\%$

- At high momenta, the statistics is low
- Estimate tracking efficiency by extrapolation from intermediate p_T



- A fraction of the near side peak after single track correction is due to detector effects (black) → limited flatness in φ distribution give rise to structures in $\Delta\varphi$
- Remaining peak comes from split tracks, resonances, gamma conversion
- Correction on total yield is very small

- Multiplicity correction via normalized and extended correlation matrix

- Normalization:

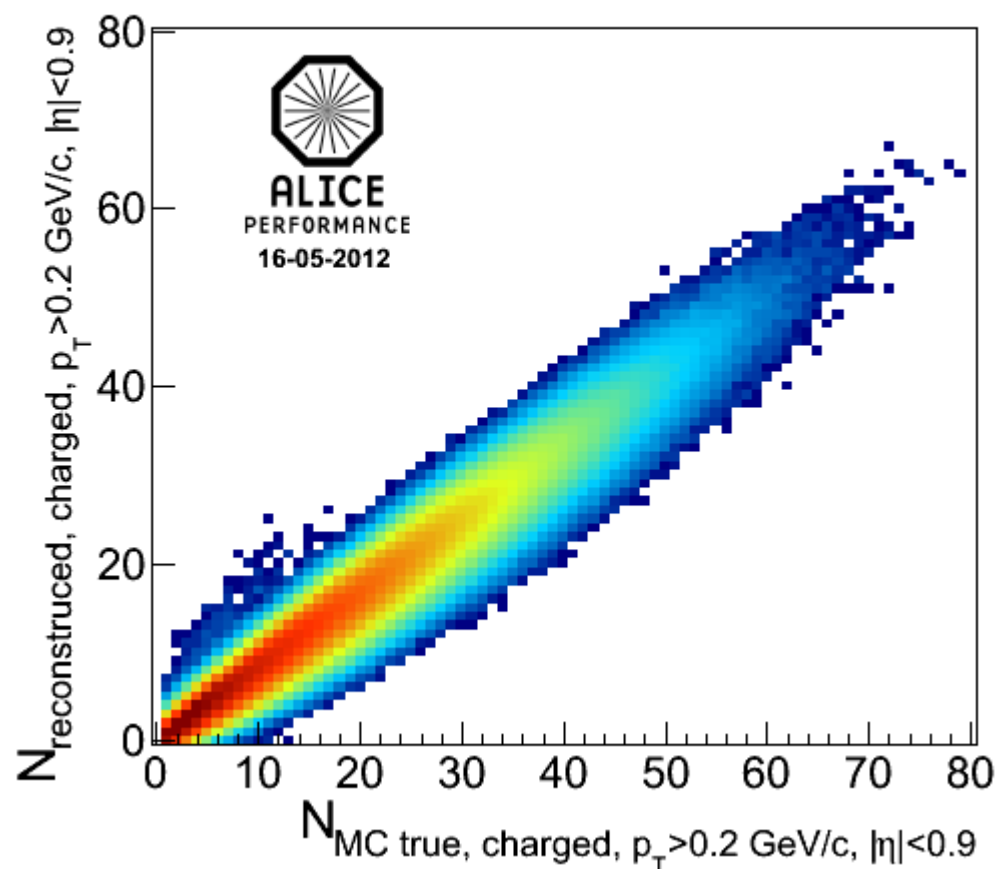
$$- \sum_{N_{rec}} R(N_{mc}, N_{rec}) = 1$$

- Extension:

- Fit slice of correlation matrix with Gaussian function and extract sigma and mean
- Used extrapolated sigma and mean for extended correlation matrix

- Correction:

$$Observable(N_{mc}) = \sum_{N_{rec}} Observable(N_{rec}) \cdot R_{1,extended}(N_{mc}, N_{rec})$$

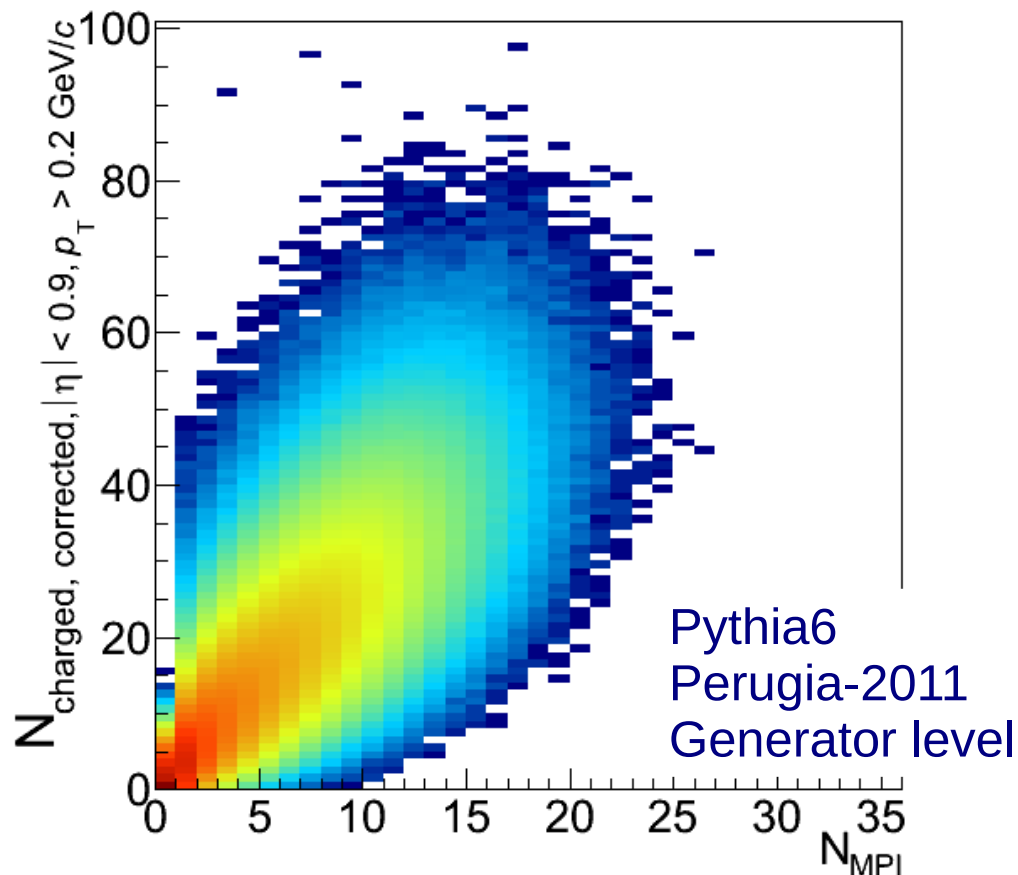
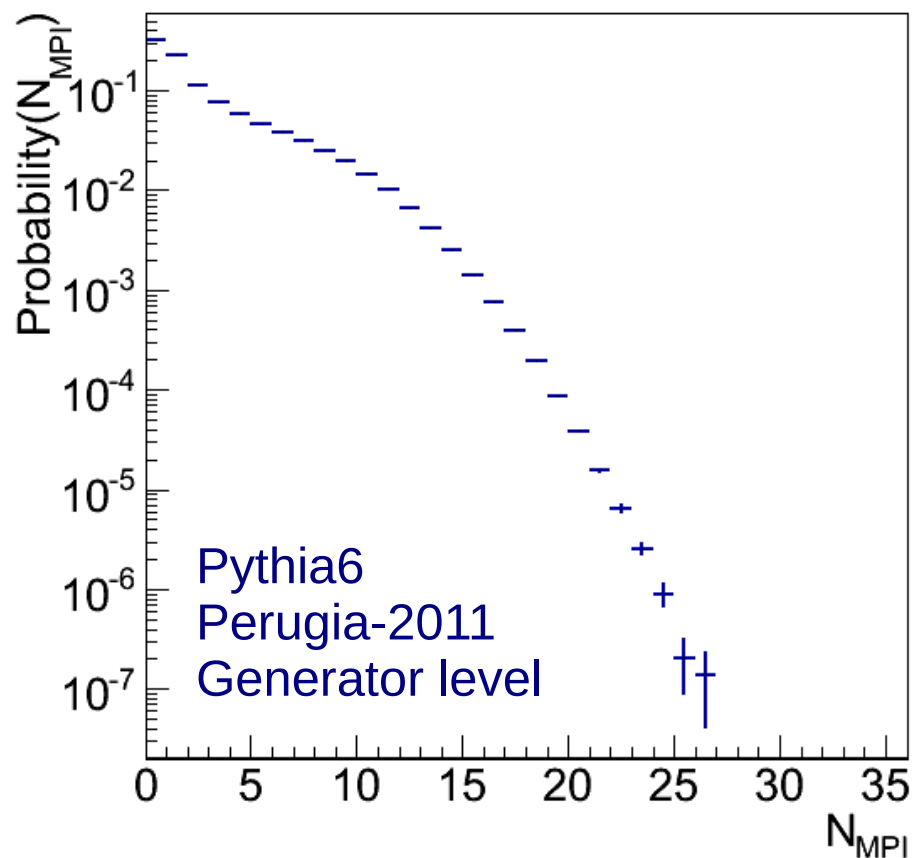


Assumption: $N_{\text{uncorrelated seeds}} \rightarrow N_{\text{MPI}}$

- We measure $N_{\text{uncorrelated seeds}}$

$$\langle N_{\text{uncorrelated seeds}} \rangle = \frac{\langle N_{\text{trig}, p_T > p_{T,\text{trig}}} \rangle}{\langle 1 + N_{\text{assoc}, \text{near}, p_T > p_{T,\text{trig}}} + N_{\text{assoc}, \text{away}, p_T > p_{T,\text{trig}}} \rangle}$$

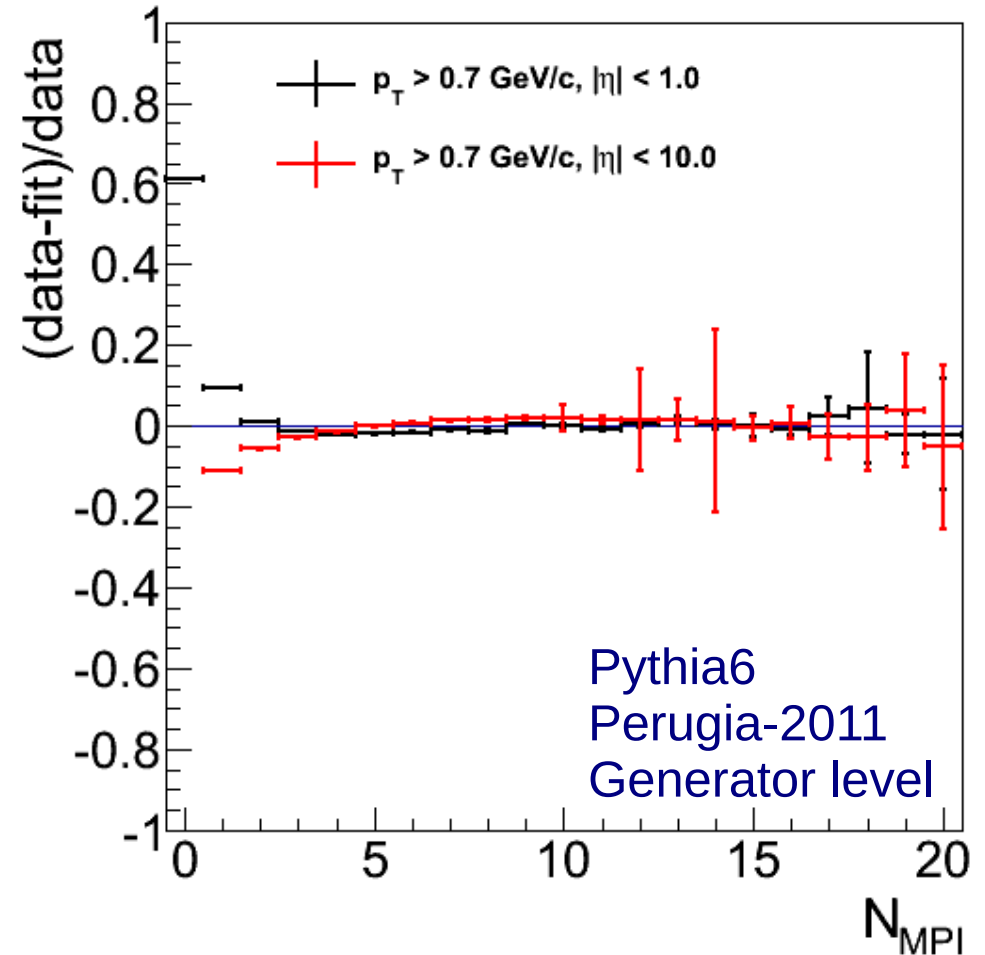
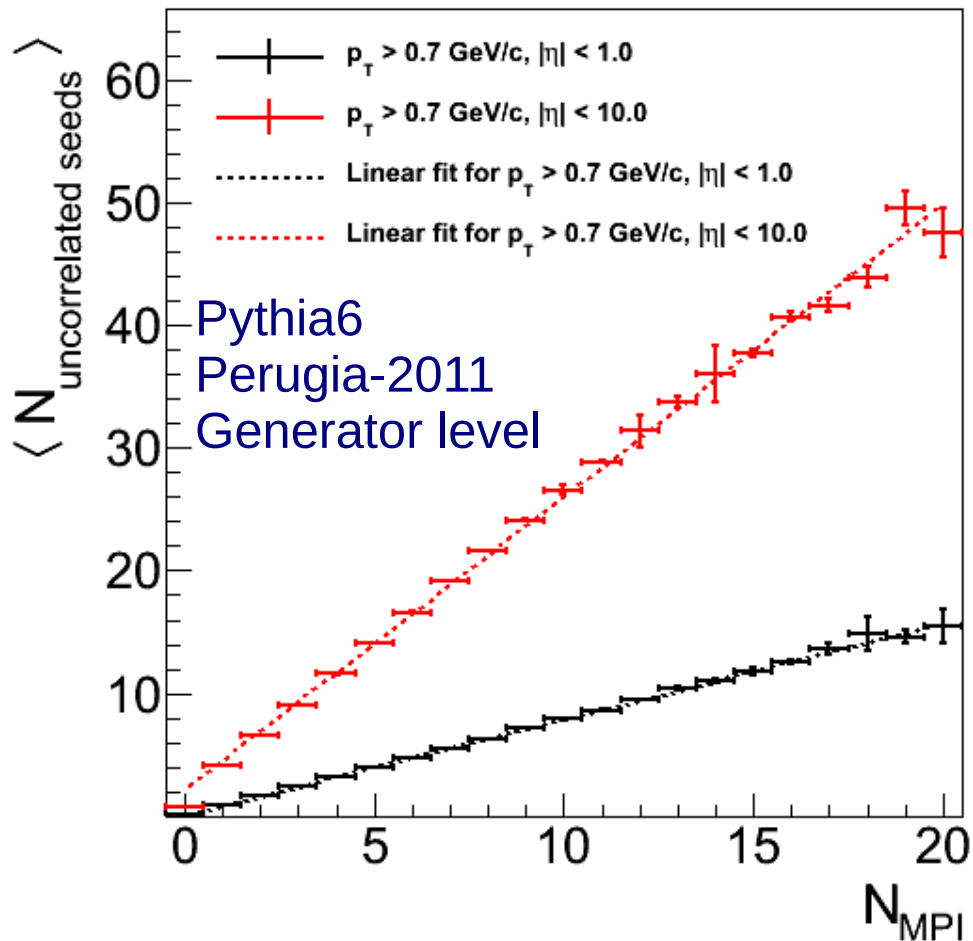
- We assume that $N_{\text{uncorrelated seeds}}$ scales with the number of multiple parton interactions
- Can we demonstrate a direct dependence in Pythia simulations
 - Perform two-particle correlation analysis of Pythia6 simulations as function of N_{MPI} = number of multiple parton interactions
 - N_{MPI} (Pythia definition) = number of hard or semi-hard scatterings that occurred in the current event in the multiple interaction scenario; is 0 for a low- p_T event



- Spectrum of multiple parton interactions in Pythia6 Perugia-2011

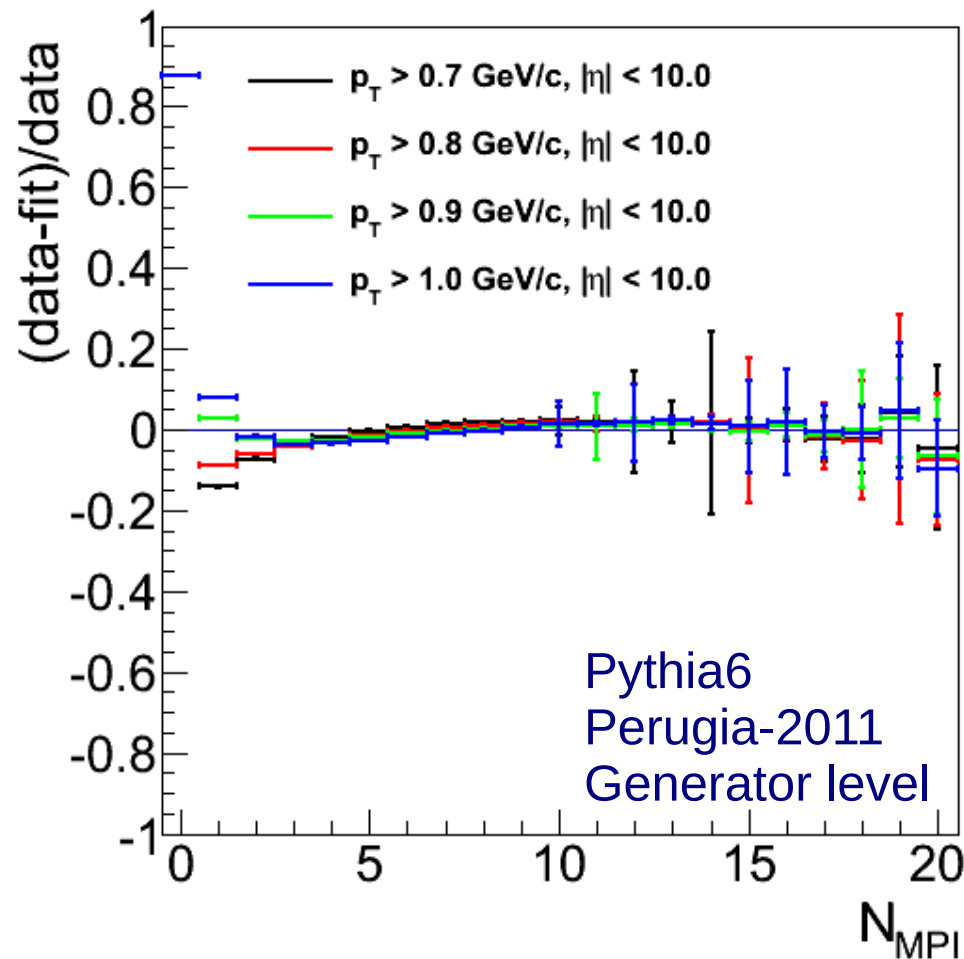
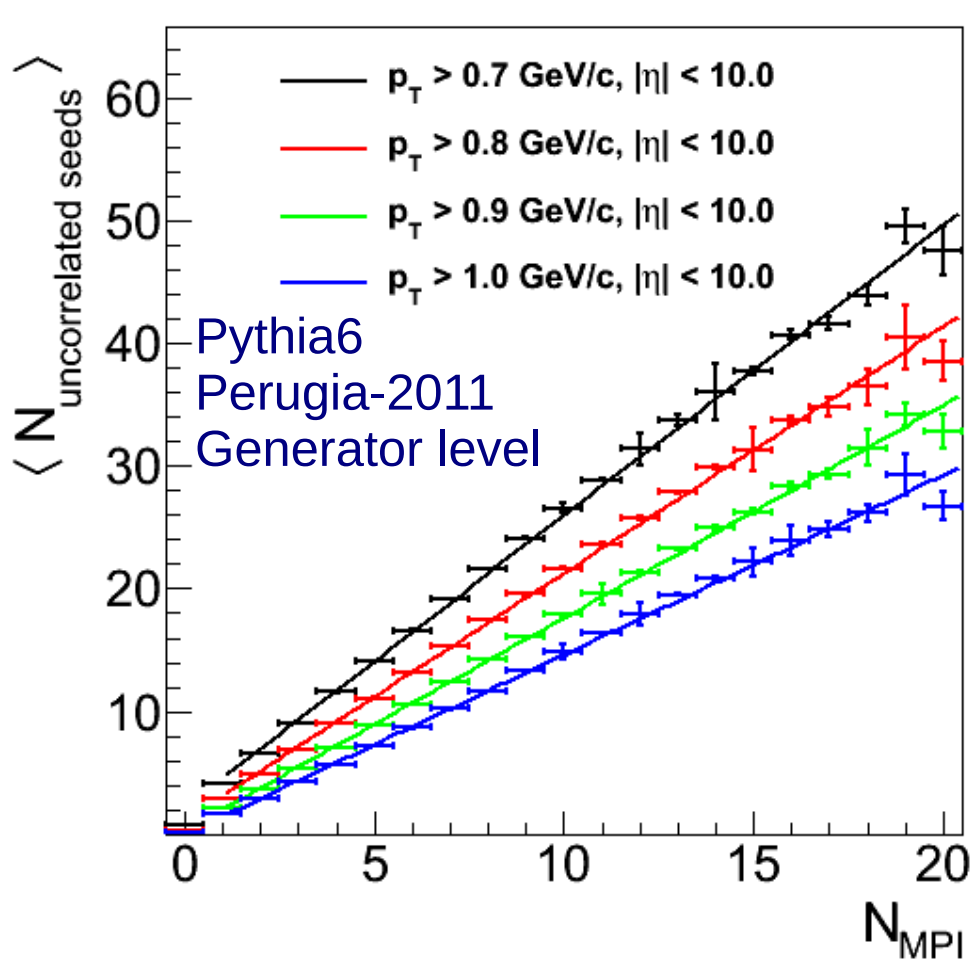
- Correlation of measured multiplicity to number of multiple parton interactions

$$N_{\text{uncorrelated seeds}} \sim N_{\text{MPI}}$$



- Agreement with linear fit is better when accepting tracks at full η acceptance and not only the tracks in the ALICE acceptance

$$N_{\text{uncorrelated seeds}} \sim N_{\text{MPI}}$$



- Linear dependence is given for several p_T thresholds

For an a priori unknown multiplicity distribution $P(n)$ of the mini-jet, we measure

$$\frac{\langle n(n-1) \rangle}{2\langle n \rangle} = \frac{1}{2} \left(\frac{\langle n^2 \rangle}{\langle n \rangle} - 1 \right)$$

For steadily falling $P(n)$ and small $\langle n \rangle$ this is in good approximation:

$$\frac{1}{2} \left(\frac{\langle n^2 \rangle}{\langle n \rangle} - 1 \right) \rightarrow \frac{\langle n \rangle}{1 - P(0)} - 1 \quad (= \langle n \rangle \text{ with trigger condition} - 1)$$

Which is the mean number of associated particles.

Example 1 (geom. row):

$$P(n) = (1-q)q^n$$

$$\langle n \rangle = \frac{q}{1-q}$$

$$\langle n^2 \rangle = 2\langle n \rangle^2$$

$$\frac{1}{2} \left(\frac{\langle n^2 \rangle}{\langle n \rangle} - 1 \right) = \langle n \rangle$$

$$\frac{\langle n \rangle}{1 - P(0)} - 1 = \langle n \rangle$$

Relation is exact !

Example 2 (Poisson):

$$P(n) = \frac{\mu^n e^{-\mu}}{n!}$$

$$\langle n \rangle = \mu$$

$$\langle n^2 \rangle = \mu^2 + \mu$$

$$\frac{1}{2} \left(\frac{\langle n^2 \rangle}{\langle n \rangle} - 1 \right) = \frac{\mu}{2}$$

$$\frac{\langle n \rangle}{1 - P(0)} - 1 = \frac{\mu}{1 - e^{-\mu}} - 1 = \frac{\mu}{2} - \frac{\mu^2}{6} + \dots$$

Example 3 (Log Series):

$$P(n) = \frac{-1}{\ln(1-p)} \frac{p^n}{n}$$

$$\langle n \rangle = \frac{-1}{\ln(1-p)} \frac{p}{(1-p)}$$

$$\langle n^2 \rangle = \frac{\langle n \rangle}{(1-p)}$$

$$\frac{1}{2} \left(\frac{\langle n^2 \rangle}{\langle n \rangle} - 1 \right) = \frac{p}{2(1-p)}$$

$$\frac{\langle n \rangle}{1 - P(0)} - 1 = \frac{p}{2(1-p)} + \frac{p^2}{3(1-p)} + p^3 \dots$$

Expect $P(n)$ to be steadily falling, choose $p_{T,\text{trig}}$ such that $\langle n \rangle$ is low