

# Rencontres de Blois 2014

Hadronic  $b$  decays and the Unitarity triangle angle  $\gamma$  at LHCb

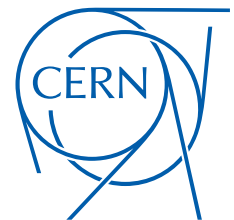
---

Jeremy Dalseno

on behalf of the LHCb collaboration

J.Dalseno [at] bristol.ac.uk

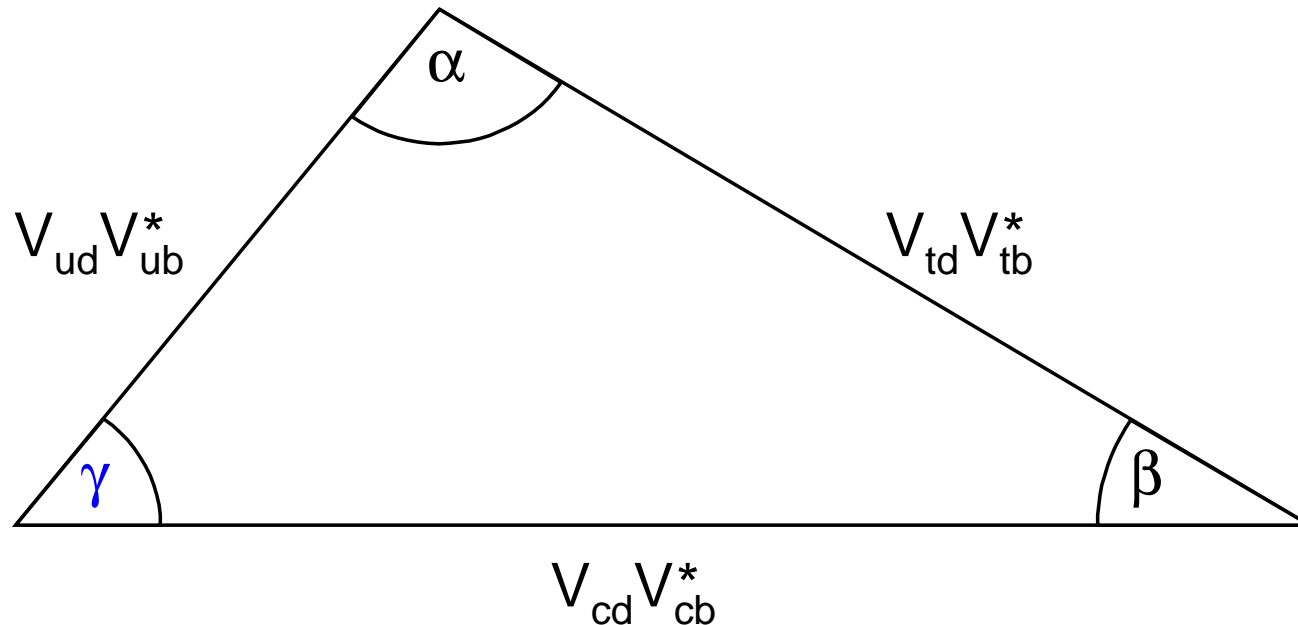
20 May 2014



# Outline

1.  $B^\pm \rightarrow D[K_S^0 \pi^+ \pi^-] K^\pm$
2.  $B^\pm \rightarrow D[K_S^0 K^\pm \pi^\pm] K^\pm$
3.  $B_c^+ \rightarrow J/\psi 3\pi^+ 2\pi^-$
4.  $\Lambda_b^0 \rightarrow \bar{K}^0 p \pi^-$

$$\phi_3 = \gamma \equiv -\arg\left(\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*}\right)$$



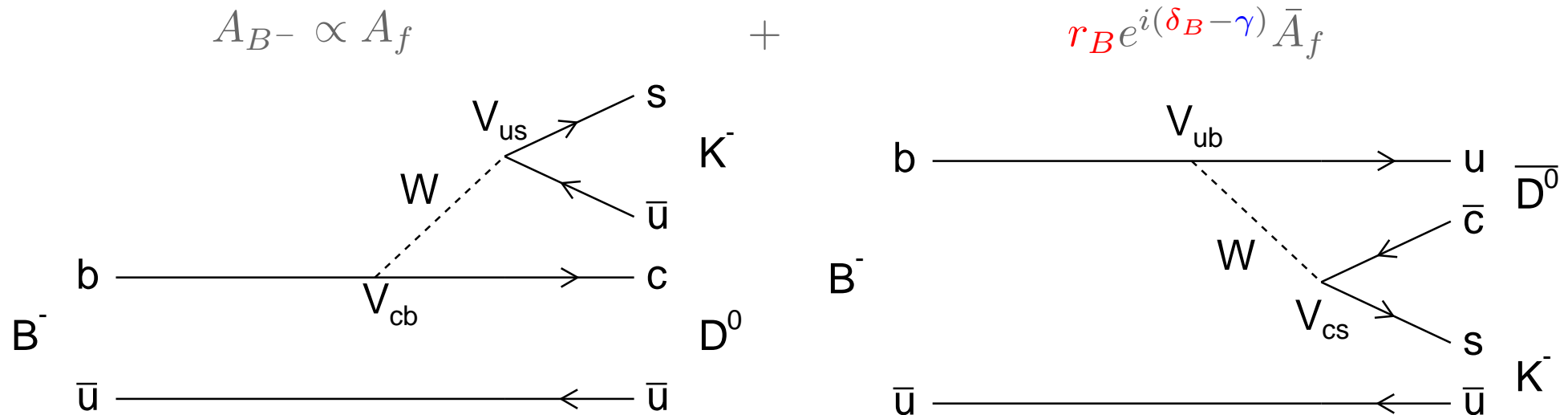
# $\gamma$ from $B$ Decays

Theoretically cleanest Standard Model measurement of  $\gamma$  from  $B \rightarrow DK$  decays

$|\delta\gamma| \lesssim \mathcal{O}(10^{-7})$  from electroweak corrections: J. Brod and J. Zupan, JHEP **1401** (2014) 051

When  $D^0$  and  $\bar{D}^0$  decay to the same final state,  $f$

Interference between the dominant  $b \rightarrow c\bar{u}s$  with the corresponding DCS  $b \rightarrow u\bar{c}s$



Amplitude ratio:  $r_B = |A(B \rightarrow \bar{D}K)| \div |A(B \rightarrow DK)|$

Strong phase difference between  $A(B \rightarrow \bar{D}K)$  and  $A(B \rightarrow DK)$ :  $\delta_B$

# GGSZ Method

Measure  $r_B$ ,  $\delta_B$  and  $\gamma$ , through interference in the Dalitz plot of  $D$  decays to  $CP$  eigenstates

A. Bondar, Proceedings of BINP Special Analysis Meeting on Dalitz Analysis, 24-26 Sep. 2002, unpublished

A. Giri, Y. Grossman, A. Soffer, J. Zupan, Phys. Rev. D **68** (2003) 054018

eg.  $D^0 \rightarrow K_S^0 \pi^+ \pi^-$  and  $\bar{D}^0 \rightarrow K_S^0 \pi^+ \pi^-$

Dalitz plots defined as scatterplot of  $m_+^2 (K_S^0 \pi^+)$  vs  $m_-^2 (K_S^0 \pi^-)$

Contains complete quantum information of the decay including phase relationships

$$|A(B^- \rightarrow DK^-)|^2 = \left| A_{D^0} + r_B e^{i(\delta_B - \gamma)} A_{\bar{D}^0} \right|^2$$

$$B^{\pm} \rightarrow D[K_S^0 \pi^+ \pi^-] K^{\pm}$$

First model-dependent measurement of  $\gamma$  from LHCb using the GGSZ method

Integrated data sample of  $1 \text{ fb}^{-1}$  recorded at centre-of-mass energy of 7 TeV

Due to the long  $K_S^0$  lifetime, data divided in 2 depending on  $K_S^0$  reconstruction

“Long”: Pion tracks located within the silicon vertex detector

“Downstream”:  $K_S^0$  decayed beyond the silicon vertex detector

Most dangerous background is  $B^{\pm} \rightarrow D[K_S^0 \pi^+ \pi^-] \pi^{\pm}$  where  $\pi^{\pm}$  was misidentified as  $K^{\pm}$

Excellent RICH PID performance suppresses this by  $\mathcal{O}(10^2)$  for minimal signal loss

Partially reconstructed backgrounds

Mostly contains real  $D[K_S^0 \pi^+ \pi^-]$  decays, but involve processes with additional particles

eg.  $B^{\pm} \rightarrow D\rho^{\pm}$ ,  $B^{\pm} \rightarrow D^* h^{\pm}$  where  $h = K$  or  $\pi$

Combinatorial

Suppressed by  $B$  candidate displacement from primary  $pp$  interaction vertex

# Yield Extraction

Analysis performed in 2 stages

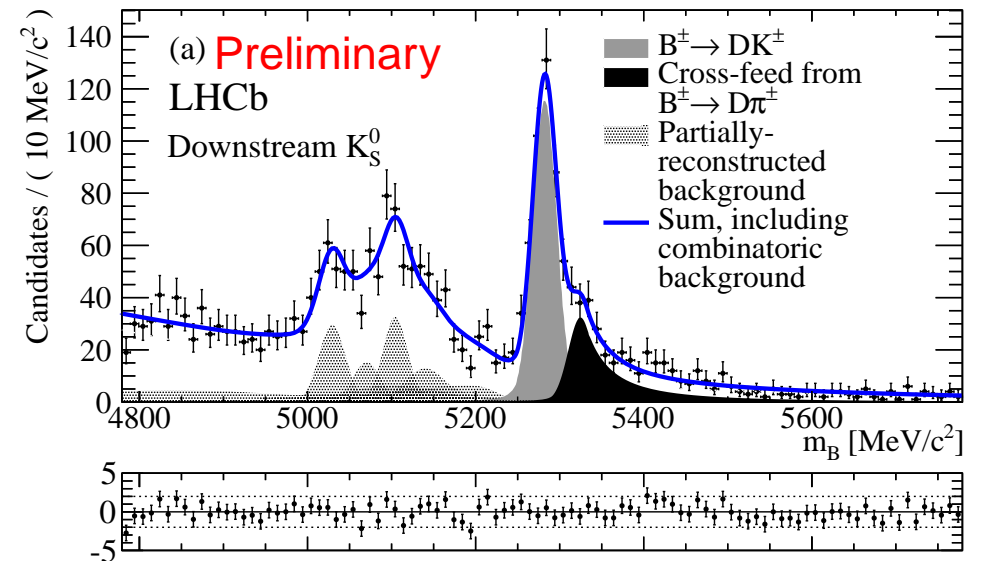
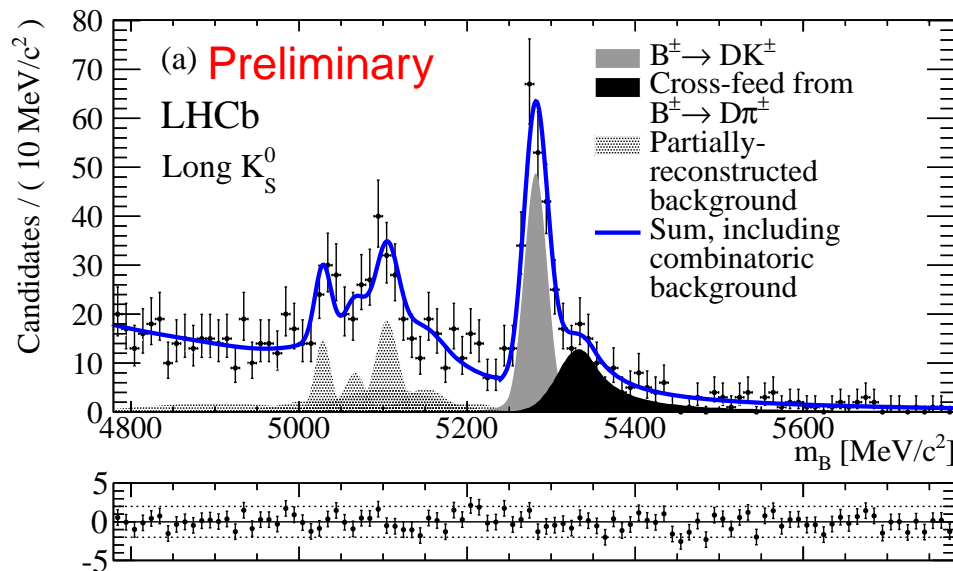
Determine signal yield from fit to the  $B^\pm$  candidate mass

Gives the signal and background fractions for the subsequent Dalitz analysis

Perform fit simultaneously with control sample  $B^\pm \rightarrow D[K_S^0 \pi^+ \pi^-] \pi^\pm$

“Long”  $K_S^0$

“Downstream”  $K_S^0$



$B^\pm \rightarrow DK^\pm$  yield:  $217 \pm 17$  events

$B^\pm \rightarrow DK^\pm$  yield:  $420 \pm 27$  events

# Dalitz Amplitude

Amplitude model fixed to that determined by the BaBar Collaboration

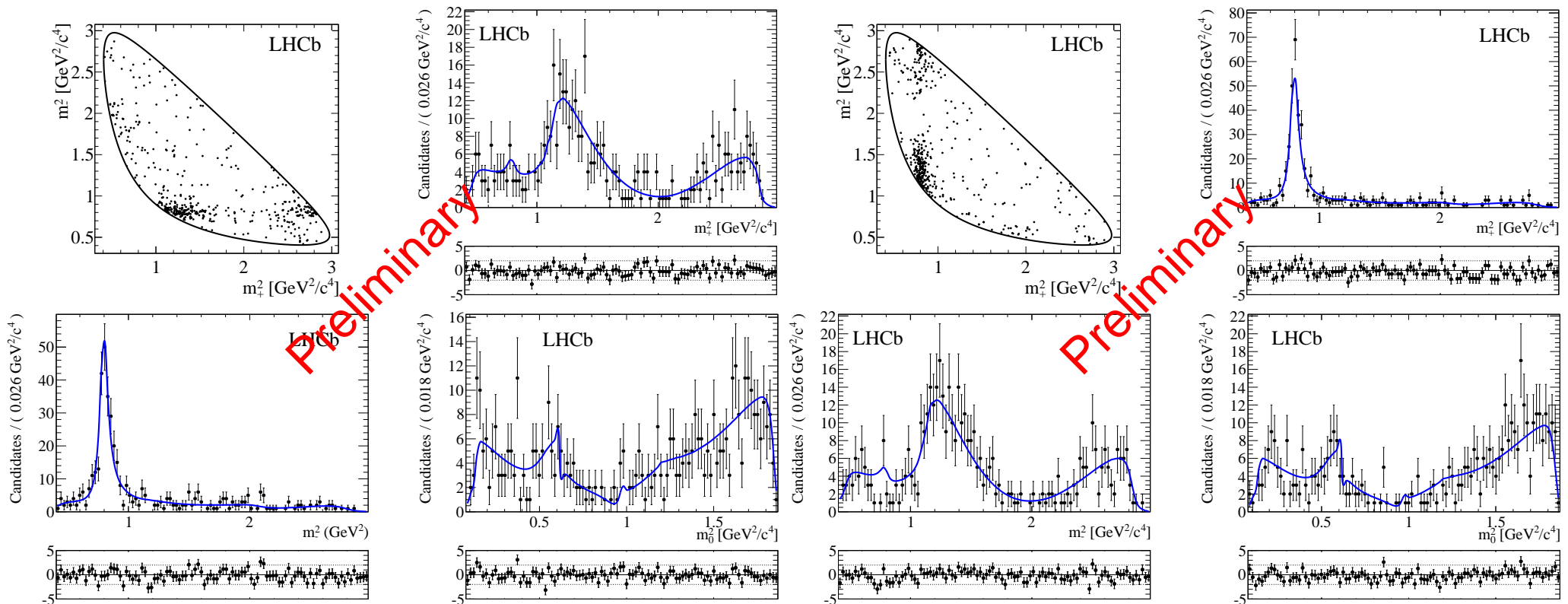
P. del Amo Sanchez *et al.* (BaBar Collab.), Phys. Rev. Lett. 105 (2010) 081803

Restrict fit region to  $\sim 3\sigma$  around  $B^+$  mass

$\gamma$  manifests as a difference in the structure between these 2 Dalitz plots

$$B^- \rightarrow DK^-$$

$$B^+ \rightarrow DK^+$$



# Results

Technical detail: Instead of fitting for  $r_B$ ,  $\delta_B$  and  $\gamma$  directly

Fit for transformed parameters

$$x_{\pm} \equiv r_B \cos(\delta_B \pm \gamma)$$

$$y_{\pm} \equiv r_B \sin(\delta_B \pm \gamma)$$

## Preliminary Results

$$x_+ = -0.084 \pm 0.045 \pm 0.009 \pm 0.003$$

$$y_+ = -0.032 \pm 0.048 \pm 0.009 \pm 0.007$$

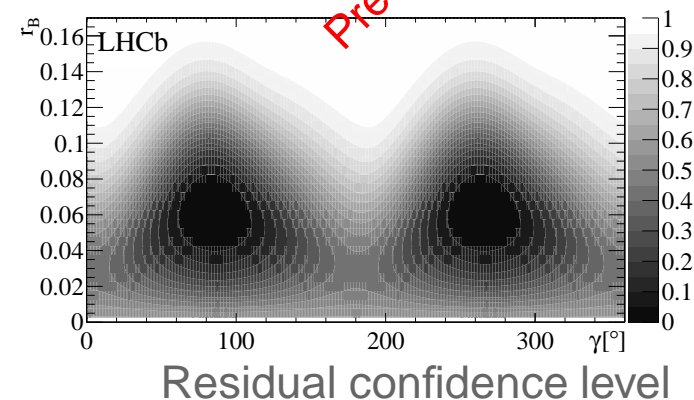
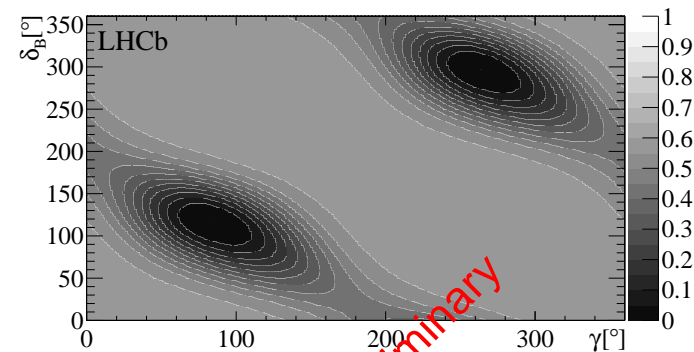
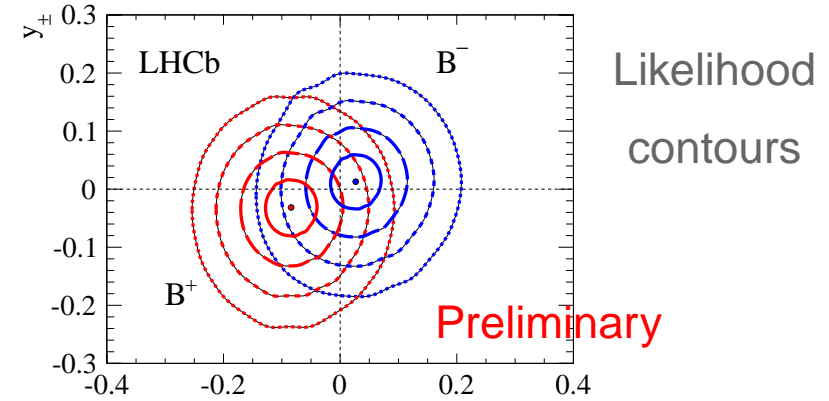
$$x_- = +0.027 \pm 0.044_{-0.008}^{+0.010} \pm 0.001$$

$$y_- = +0.013 \pm 0.048_{-0.006}^{+0.008} \pm 0.003$$

Uncertainties

1: statistical, 2: systematic, 3: model

Convert to  $\gamma$ , negligible  $D^0$  mixing effect





# Results

LHCb:  $1 \text{ fb}^{-1}$

**Preliminary Results**

$$\gamma = (84_{-42}^{+49})^\circ$$

Belle: 657M  $B\bar{B}$  pairs

PRD **81** (2010) 112002

$$\gamma = (78_{-15}^{+14})^\circ$$

Includes  $B \rightarrow D^{(*)} K$

BaBar: 468M  $B\bar{B}$  pairs

PRL 105 (2010) 121801

$$\gamma = (68 \pm 15)^\circ$$

Includes  $B \rightarrow D^{(*)} K^{(*)}$

Includes  $D \rightarrow K_S^0 K^+ K^-$

There are also model-independent binned Dalitz measurements with input from CLEO

J. Libby *et al.* (CLEO Collab.) Phys. Rev. D. **82** (2010) 112006

LHCb:  $1 \text{ fb}^{-1}$

PLB **718** (2012) 43

$$\gamma = (44_{-38}^{+43})^\circ$$

Includes  $D \rightarrow K_S^0 K^+ K^-$

$\gamma$  solution consistent with Standard Model chosen

Uncertainties comparable

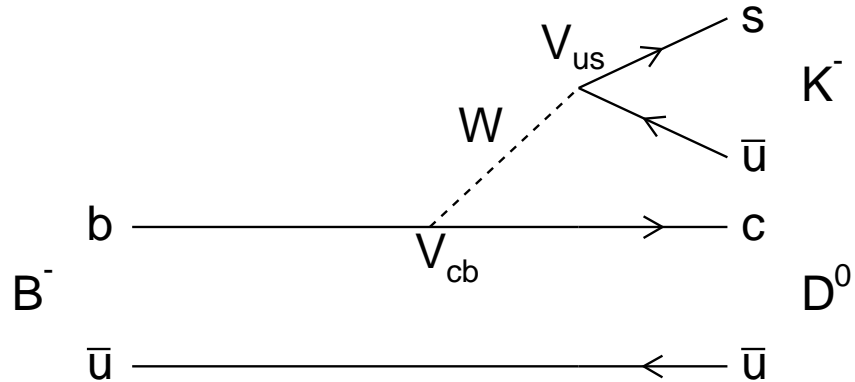
Belle: 772M  $B\bar{B}$  pairs

PRD **85** (2012) 112014

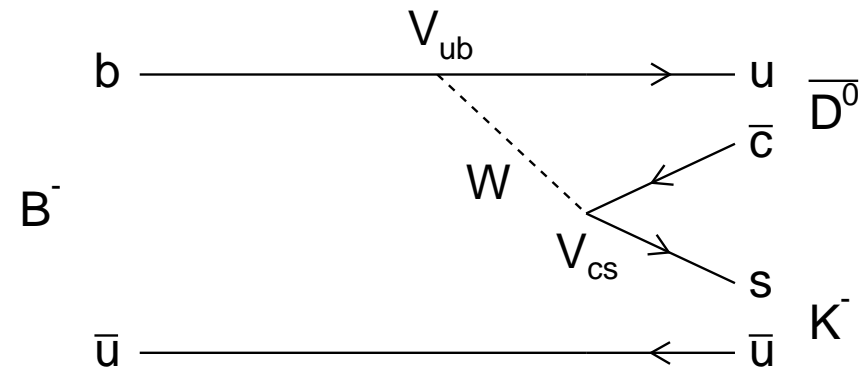
$$\gamma = (77 \pm 16)^\circ$$

# ADS-Like Adaptation

Colour-favoured

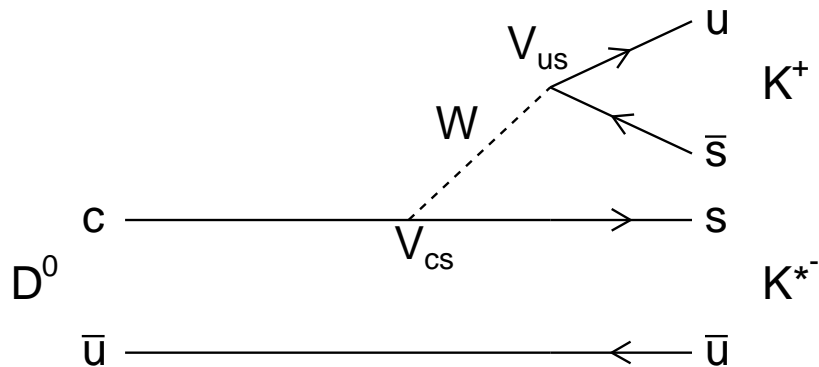


Colour-suppressed

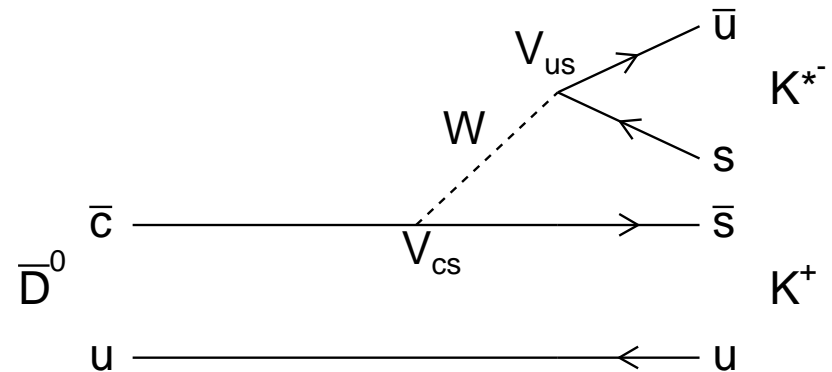


Difference in magnitudes mean that resulting asymmetries tend to be small, however

$K^*(892)^-$  from spectator (suppressed)



$K^*(892)^-$  from  $W$  (favoured)



Amplitudes of similar magnitude can enhance the effect of  $CP$  asymmetries

D. Atwood, I. Dunietz, A. Soni, Phys. Rev. Lett. **78** (1997) 3257

# ADS Method

Singly Cabibbo Suppressed (SCS)  $D$  decays across the Dalitz plot

Y. Grossman, Z. Ligeti and A. Soffer, Phys. Rev D **67** (2003) 071301

Consider  $B^- \rightarrow DK^-$  followed by  $D \rightarrow K_S^0 K^+ \pi^-$

For a given  $B$  charge, 2 possibilities for kaon charge configuration

Charged kaons with Opposite Sign (OS)

$$\Gamma_{OS}^- \propto r_B^2 + r_D^2 + 2r_B r_D \kappa_f \cos(\delta_B - \gamma + \delta_f)$$

Charged kaons with Same Sign (SS)

$$\Gamma_{SS}^- \propto 1 + r_B^2 r_D^2 + 2r_B r_D \kappa_f \cos(\delta_B - \gamma - \delta_f)$$

Amplitude ratio:  $r_D = |A(D^0 \rightarrow K_S^0 K^+ \pi^-)| \div |A(\bar{D}^0 \rightarrow K_S^0 K^+ \pi^-)|$

3-body decay, so resonant structure varies across the Dalitz plot,  $m_{K_S^0 K}^2$  vs  $m_{K_S^0 \pi}^2$

Decay rate in region of a resonance depends on integral of the interference term in that region

Coherence factor  $\kappa_f$ , and average strong phase difference  $\delta_f$

# ADS Method

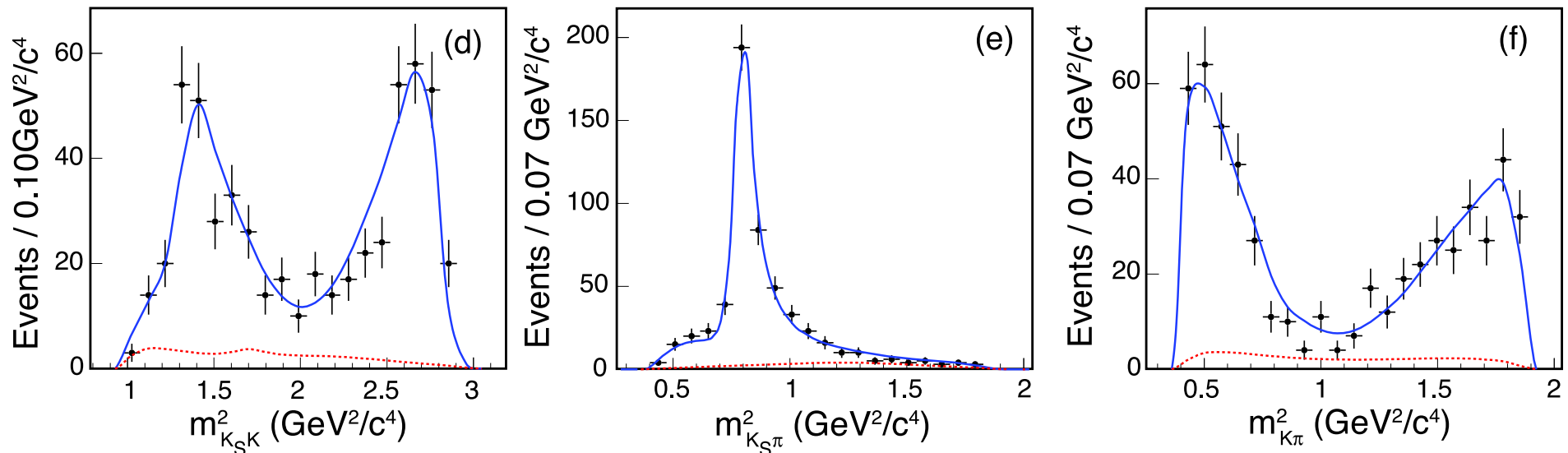
$$\kappa_f e^{-i\delta_f} \propto \int A_{K_S^0 K^- \pi^+}^*(m_{K_S^0 K}^2, m_{K_S^0 \pi}^2) A_{K_S^0 K^+ \pi^-}(m_{K_S^0 K}^2, m_{K_S^0 \pi}^2) dm_{K_S^0 K}^2 dm_{K_S^0 \pi}^2$$

$K_S^0 K^- \pi^+$  and  $K_S^0 K^+ \pi^-$  are flavour non-specific final states

Correlated  $D^0 \bar{D}^0$  pairs can tag the  $D$  flavour

Amplitudes measured by the CLEO Collaboration

J. Insler *et al.* (CLEO Collab.) Phys. Rev. D. **85** (2012) 092016



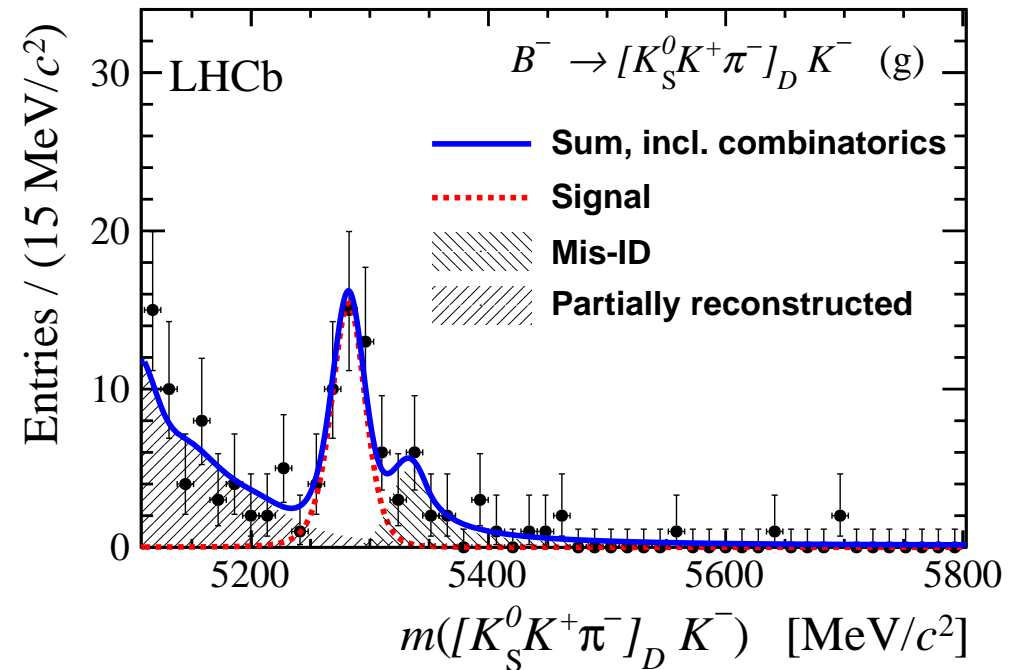
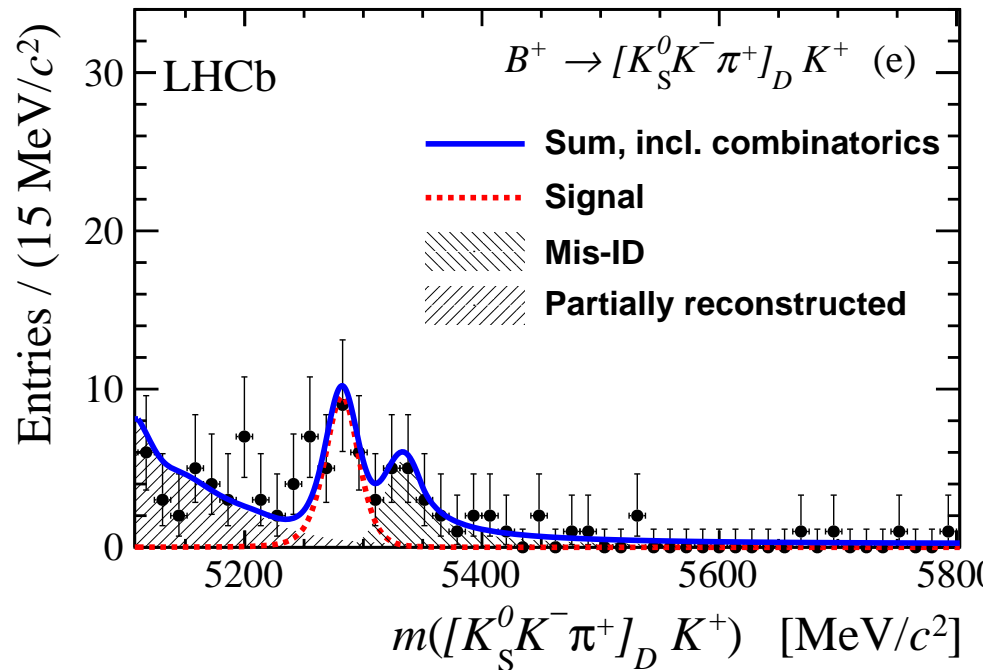
# Results

World's first measurement of  $\gamma$  using SCS  $D \rightarrow K_S^0 K^+ \pi^-$  decays

Full LHCb data sample of  $3 \text{ fb}^{-1}$ :  $1 \text{ fb}^{-1}$  @ 7 TeV and  $2 \text{ fb}^{-1}$  @ 8 TeV

R. Aaij *et al.* (LHCb Collab.) Phys. Lett. B **733** (2014) 36

$$\Gamma_{\text{OS}}^+ \propto r_B^2 + r_D^2 + 2r_B r_D \kappa_f \cos(\delta_B + \gamma + \delta_f) \quad \Gamma_{\text{OS}}^- \propto r_B^2 + r_D^2 + 2r_B r_D \kappa_f \cos(\delta_B - \gamma + \delta_f)$$

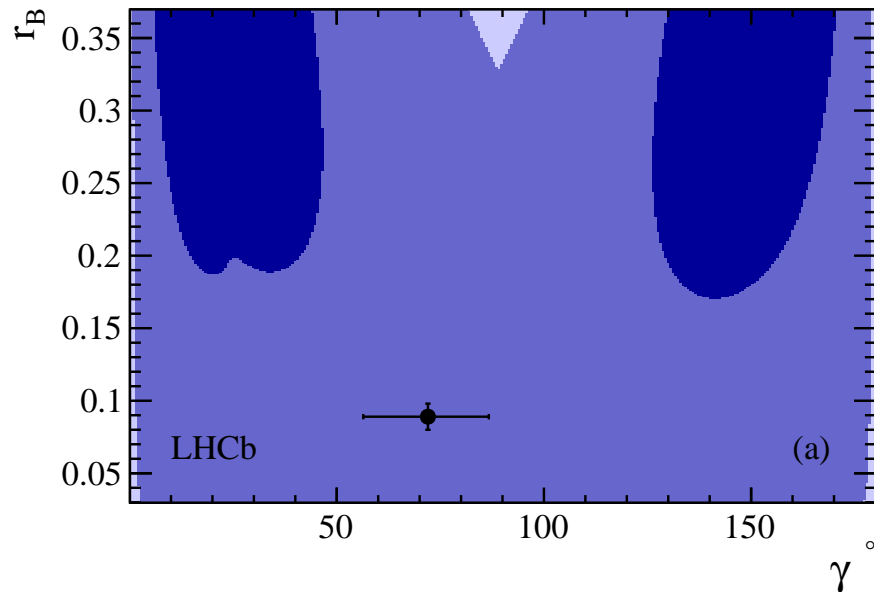


$\gamma$  manifests as a difference in the rates when 2 kaons have opposite charge

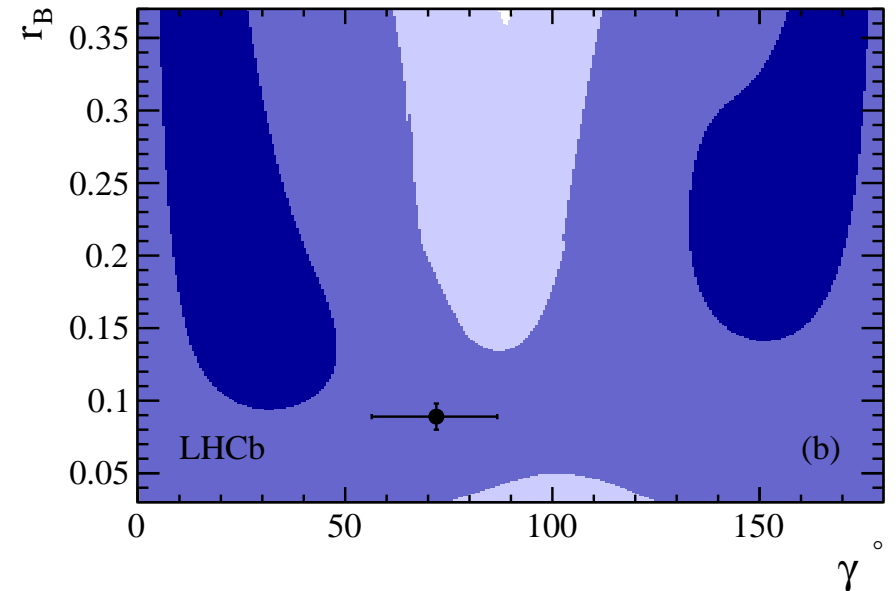
# Results

$\gamma$  constraint accounting for  $D^0$  mixing effects, contours represent change in likelihood

Whole Dalitz plot



$K^*(892)$  region



$n\sigma$  contours with  $n = 1$  (dark blue),  $n = 2$  (medium blue) and  $n = 3$  (light blue)

Data point: LHCb average from other  $B \rightarrow DK$  modes

R. Aaij *et al.* (LHCb Collab.) Phys. Lett. B **726** (2013) 151

Agreement within  $2\sigma$

Constraint tighter in  $K^*(892)$  region because coherence factor is larger

$$B_c^+ \rightarrow J/\psi 3\pi^+ 2\pi^-$$

$B_c^-$  ( $b\bar{c}$ ) the only meson containing 2 heavy quarks of different flavour

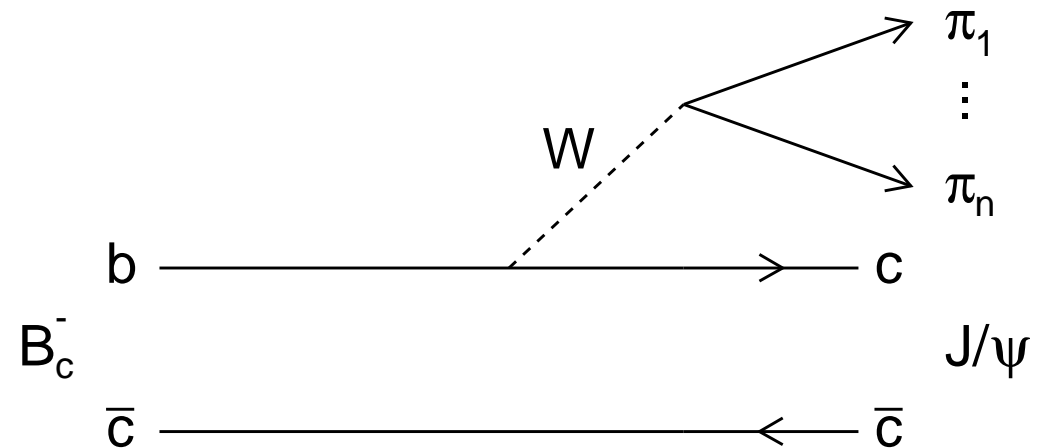
Test of QCD factorisation

Form factor of  $B_c \rightarrow J/\psi W^*$

Spectral fragmentation of the  $W^*$  into  $n\pi$

Measure ratio of branching fractions

$$R_{5\pi} = \frac{\mathcal{B}(B_c^+ \rightarrow J/\psi 3\pi^+ 2\pi^-)}{\mathcal{B}(B_c^+ \rightarrow J/\psi \pi^+)}$$



Predictions range from 0.95 to 1.1

A. V. Luchinsky, Phys. Rev. D **86** (2012) 074024

# Results

World's first measurement

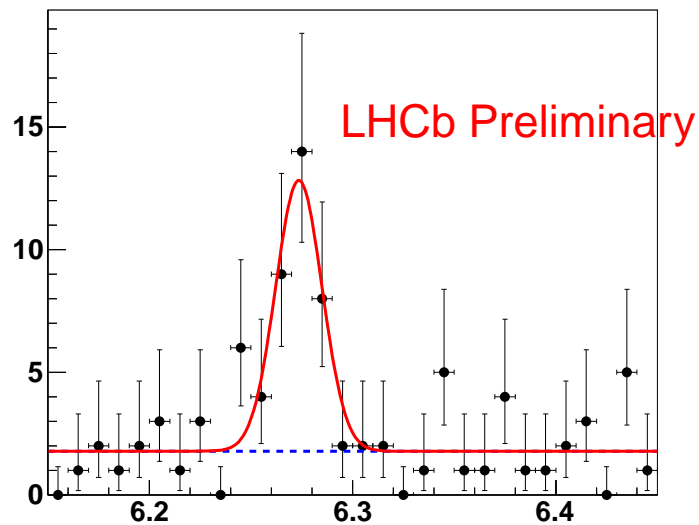
Full LHCb data sample of  $3 \text{ fb}^{-1}$ :  $1 \text{ fb}^{-1}$  @ 7 TeV and  $2 \text{ fb}^{-1}$  @ 8 TeV

R. Aaij *et al.* (LHCb Collab.), arXiv:1404.0287 (2014)

$J/\psi$  reconstructed in di-muon channel

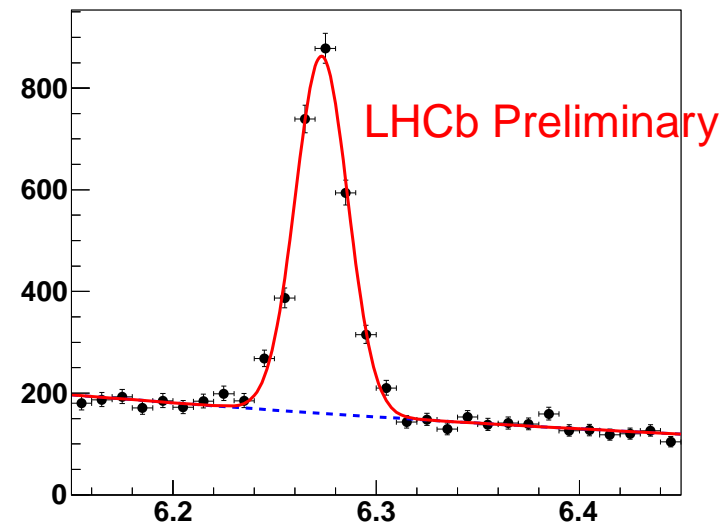
5 pion distribution generated according to various QCD factorisation models

$$B_c^+ \rightarrow J/\psi 3\pi^+ 2\pi^-$$



Yield:  $32 \pm 8$  events

$$B_c^+ \rightarrow J/\psi \pi^+$$



Yield:  $2271 \pm 63$  events

$4.5\sigma$  significance



# Results

Efficiency ratio from MC

$$\frac{\epsilon(B_c^+ \rightarrow J/\psi\pi^+)}{\epsilon(B_c^+ \rightarrow J/\psi 3\pi^+ 2\pi^-)} = 123.8 \pm 5.6$$

Error from MC statistics only

Ratio of branching fractions

$$\begin{aligned} R_{5\pi} &= \frac{N(B_c^+ \rightarrow J/\psi 3\pi^+ 2\pi^-)}{N(B_c^+ \rightarrow J/\psi\pi^+)} \\ &\times \frac{\epsilon(B_c^+ \rightarrow J/\psi\pi^+)}{\epsilon(B_c^+ \rightarrow J/\psi 3\pi^+ 2\pi^-)} \\ &= 1.74 \pm 0.44 \pm 0.24 \end{aligned}$$

Uncertainty 1: statistical, 2: systematic

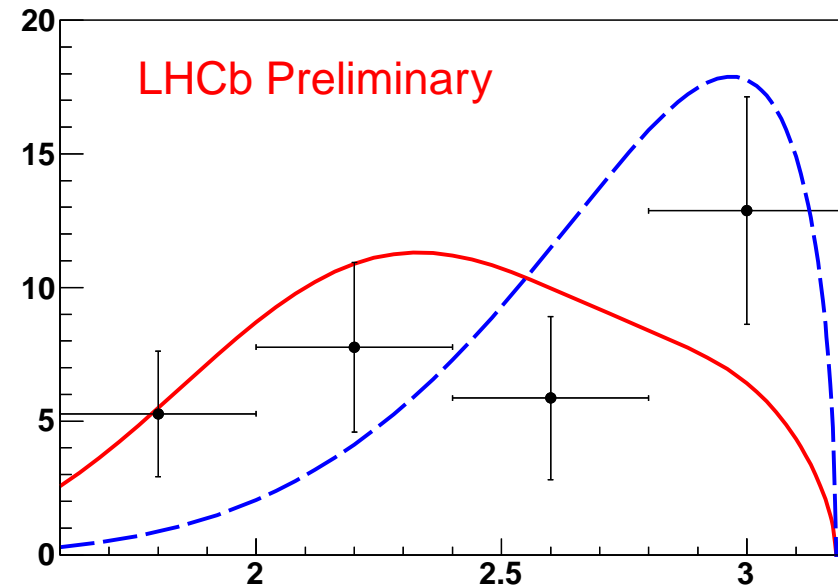
Consistent with theoretical predictions

Consistent with analogous measurements  
with  $B^0$  and  $B^+$

Dominant systematic uncertainty on  $5\pi$  model

Affects  $\epsilon(B_c^+ \rightarrow J/\psi 3\pi^+ 2\pi^-)$

Background-subtracted  $5\pi$  distribution



Red: Model prediction

Blue: 5-body phase space

Reweight to data distribution

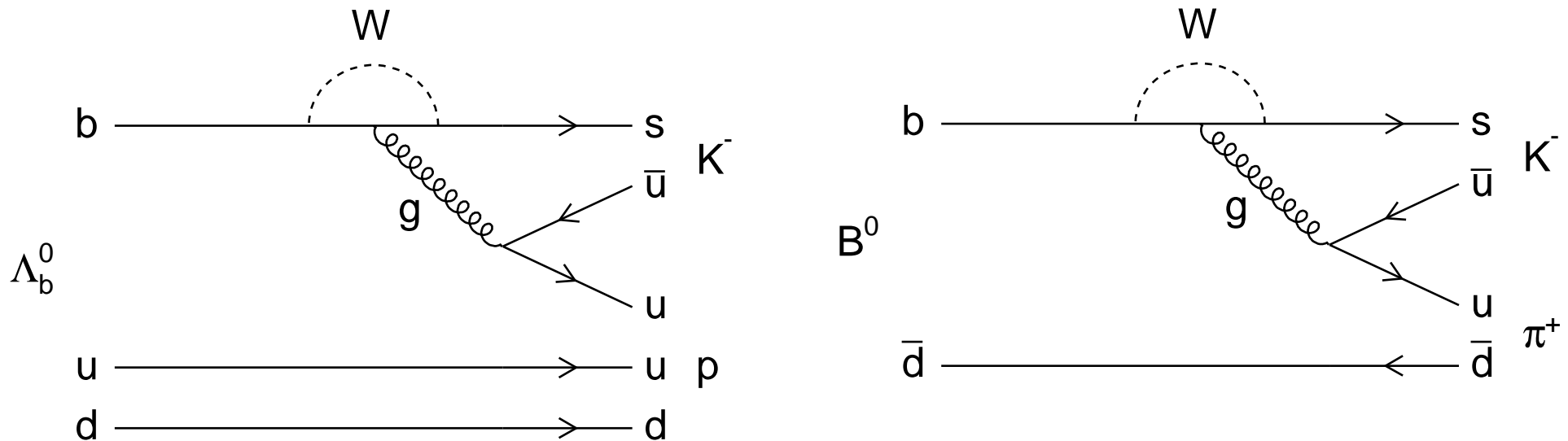
$$\Lambda_b^0 \rightarrow \bar{K}^0 p \pi^-$$

No hadronic charmless 3-body decays yet observed in  $b$  baryons

Interesting area to search for  $CP$  violating effects

Analogous to large  $CP$  violating effects in hadronic charmless 3-body  $B$  mesons decays

R. Aaij *et al.* (LHCb Collab.), PRL **111** (2013) 101801; PRL **112** (2014) 011801



Unknown heavy particle in the loop may cause unexpected  $CP$  violating effects

Potential for New Physics

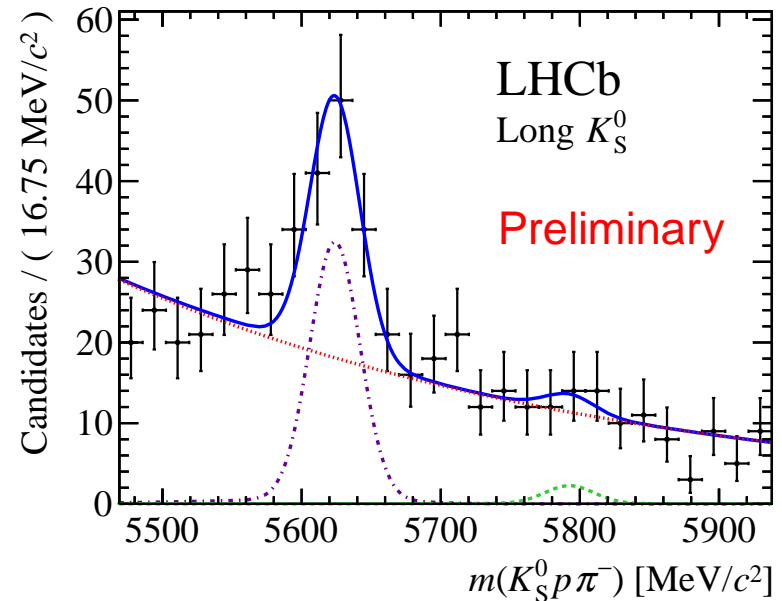
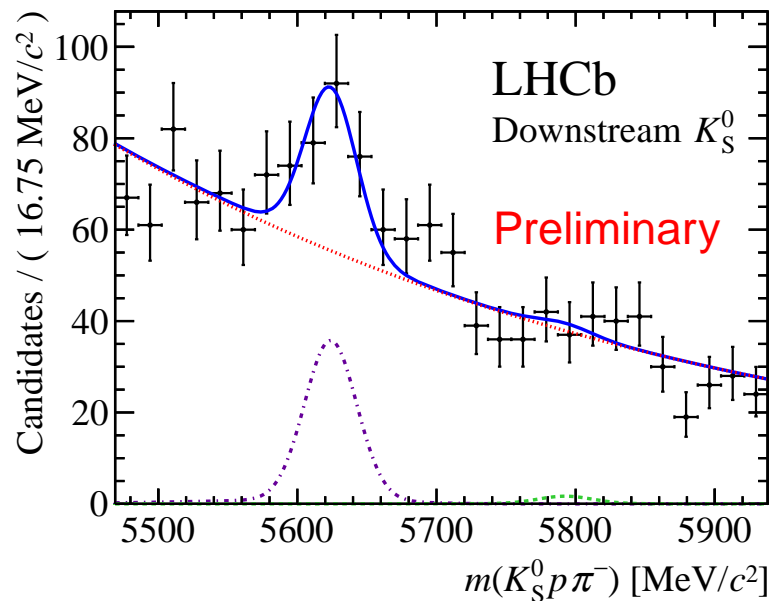
# Results

LHCb data sample of  $1 \text{ fb}^{-1}$  @ 7 TeV

R. Aaij *et al.* (LHCb Collab.), arXiv:1402.0770 (2014)

Veto significant background from  $\Lambda_b^0 \rightarrow \Lambda_c^+ [pK_S^0] h^-$

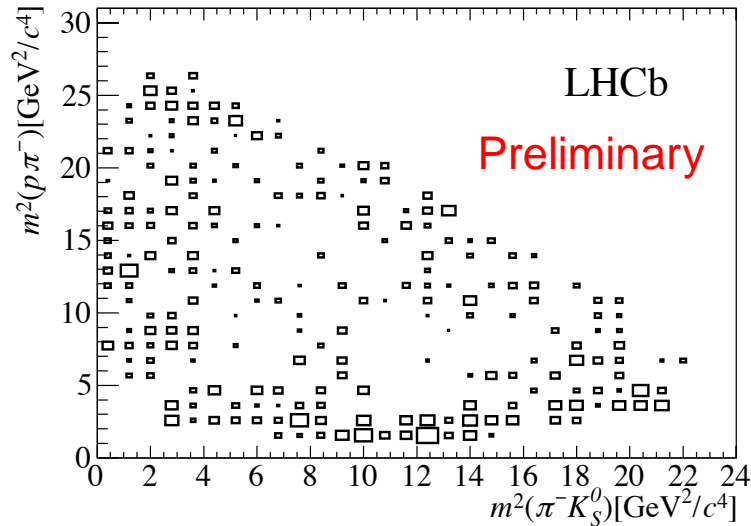
$B^0 \rightarrow K_S^0 \pi^+ \pi^-$  used as normalisation channel



$8.6\sigma$  significance including systematic uncertainties, first observation

Green curve shows concurrent search for  $\Xi_b^0(usb)$  baryon, not significant

# Results



Background subtracted  $\Lambda_b^0 \rightarrow \bar{K}^0 p \pi^-$  Dalitz plot

Signal detection efficiency weighted by Dalitz plot

No clear peaking structure except for low  $p\pi^-$  mass

Could be from excited nucleon states

$$\mathcal{B}(\Lambda_b^0 \rightarrow \bar{K}^0 p \pi^-) = (1.26 \pm 0.19 \pm 0.09 \pm 0.34 \pm 0.05) \times 10^{-5}$$

Uncertainties 1: statistical, 2: systematic, 3:  $f_{\Lambda_b^0}/f_d$ , 4:  $\mathcal{B}(B^0 \rightarrow K_S^0 \pi^+ \pi^-)$

Measure integrated direct  $CP$  violation over the Dalitz plot

$$\mathcal{A}_{CP}^{\text{Raw}} = (N_{\bar{f}} - N_f) / (N_{\bar{f}} + N_f)$$

Remove production and detection asymmetries with  $\Lambda_b^0 \rightarrow \Lambda_c^+ [\bar{K}^0 p] \pi^-$  control sample

$$\mathcal{A}_{CP}(\Lambda_b^0 \rightarrow \bar{K}^0 p \pi^-) = 0.22 \pm 0.13 \text{ (stat)} \pm 0.03 \text{ (syst)}$$

# Summary

First model-dependent measurement of  $\gamma$  at LHCb using  $B^\pm \rightarrow D[K_S^0 \pi^+ \pi^-] K^\pm$

Consistent with Standard Model expectations

Similar precision to model independent methods

First ADS-like constraint of  $\gamma$  with  $B^\pm \rightarrow D[K_S^0 K^\pm \pi^\pm] K^\pm$

Amplitude from CLEO

$\gamma$  consistent with other LHCb measurements

First evidence of  $B_c^+ \rightarrow J/\psi 3\pi^+ 2\pi^-$

Branching fraction consistent with expectations from QCD factorisation

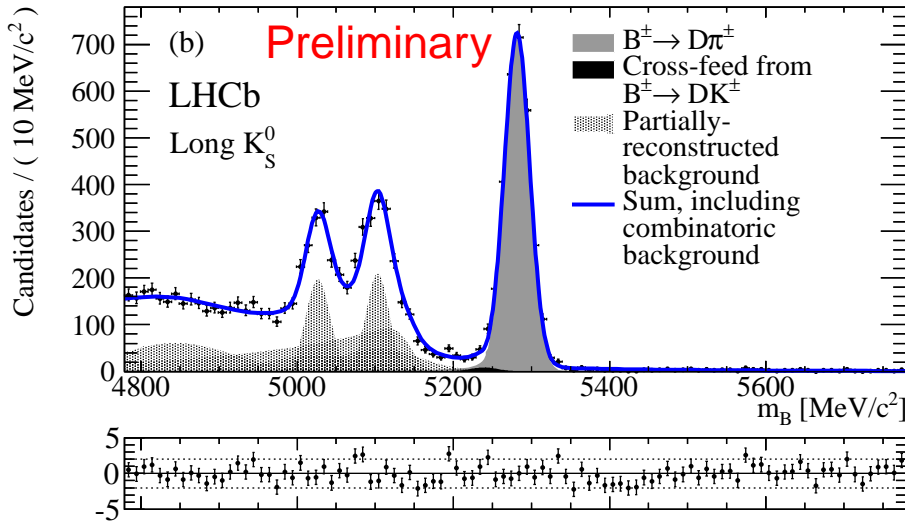
First observation of 3-body hadronic charmless  $b$  baryon decays

No evidence for direct  $CP$  at this time

# Backup

$$B^{\pm} \rightarrow D[K_S^0 \pi^+ \pi^-] \pi^{\pm}$$

“Long”  $K_S^0$



“Downstream”  $K_S^0$

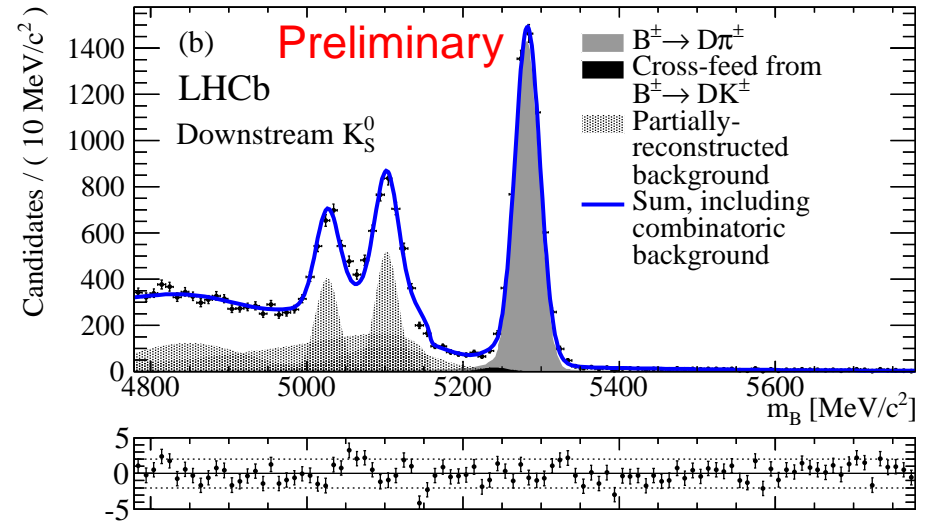


Table 1: Fitted signal and background yields in the signal invariant mass region ( $|B$  mass after refit - world average|  $< 50$  MeV/c<sup>2</sup>) for components contributing to the  $CP$  fit.

Fit component	$B^{\pm} \rightarrow DK^{\pm}, long$	$B^{\pm} \rightarrow DK^{\pm}, downstream$
Signal	$217 \pm 17$	$420 \pm 27$
Cross-feed background (from $B^{\pm} \rightarrow D\pi^{\pm}$ )	$35.9 \pm 0.7$	$76 \pm 1$
Combinatoric $D$ background	$5^{+7}_{-3}$	$31^{+11}_{-9}$
Random $Dh$ background	$28^{+5}_{-8}$	$45^{+18}_{-19}$
$D^*\pi$ background	$0.36 \pm 0.08$	$6 \pm 7$
$D\rho$ background	$2.2 \pm 0.5$	$4 \pm 11$
$B_s \rightarrow DK^*$ background	$0.9 \pm 0.2$	$4 \pm 2$

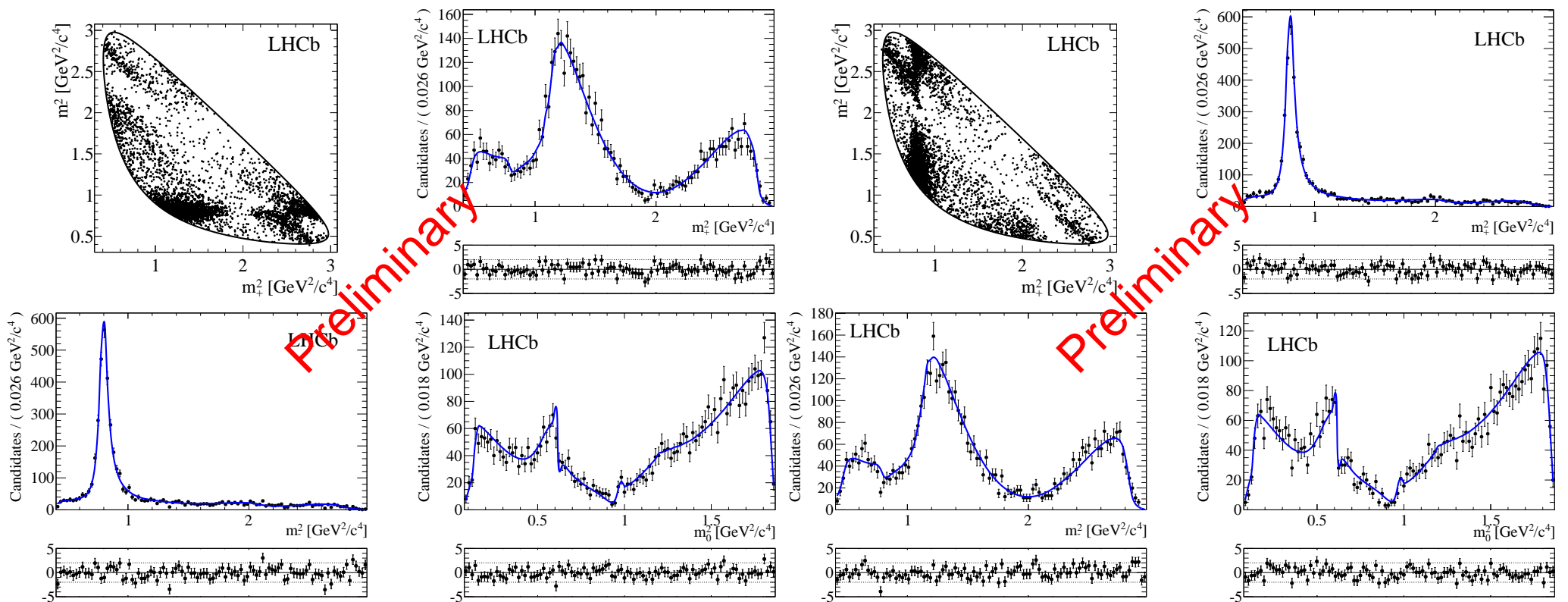
  

Fit component	$B^{\pm} \rightarrow D\pi^{\pm}, long$	$B^{\pm} \rightarrow D\pi^{\pm}, downstream$
Signal	$2906 \pm 56$	$5960 \pm 80$
Cross-feed background (from $B^{\pm} \rightarrow DK^{\pm}$ )	$27 \pm 2$	$53 \pm 3$
Combinatoric $D$ background	$15^{+19}_{-10}$	$99^{+36}_{-27}$
Random $Dh$ background	$76^{+15}_{-22}$	$146^{+33}_{-41}$
$D^*\pi$ background	$6.6 \pm 0.4$	$22.0 \pm 0.7$

$$B^\pm \rightarrow D[K_S^0 \pi^+ \pi^-] \pi^\pm$$

$$B^- \rightarrow D \pi^-$$

$$B^+ \rightarrow D \pi^+$$





$$B^\pm \rightarrow D[K_S^0 \pi^+ \pi^-] K^\pm$$

	Description	$\delta x_- (\times 10^{-3})$	$\delta y_- (\times 10^{-3})$	$\delta x_+ (\times 10^{-3})$	$\delta y_+ (\times 10^{-3})$
(a)	$K$ -matrix 1st solution	-0.132	0.044	0.250	-2.346
(b)	$K$ -matrix 2nd solution	-0.086	-0.339	0.122	-0.528
(c)	Remove slowly varying part in $P$ -vector	-0.144	-0.317	0.097	-0.762
(d)	Generalised LASS → relativistic Breit-Wigner	-0.713	-1.846	3.042	6.584
(e)	Gounaris-Sakurai → relativistic Breit-Wigner	0.077	-0.849	0.145	0.818
(f)	$m + \delta m$	-0.063	-0.561	0.181	0.256
(g)	$m - \delta m$	-0.128	-0.161	-0.098	-1.104
(h)	$\Gamma + \delta\Gamma$	-0.059	-0.365	-0.048	-0.423
(i)	$\Gamma - \delta\Gamma$	-0.158	-0.333	0.273	-0.489
(j)	$m + \delta m$	-0.106	-0.346	0.096	-0.464
(k)	$m - \delta m$	-0.102	-0.351	0.085	-0.456
(l)	$\Gamma + \delta\Gamma$	-0.102	-0.344	0.081	-0.467
(m)	$\Gamma - \delta\Gamma$	-0.105	-0.351	0.097	-0.453
(n)	$m + \delta m$	-0.082	-0.355	0.078	-0.421
(o)	$m - \delta m$	-0.125	-0.342	0.106	-0.498
(p)	$\Gamma + \delta\Gamma$	-0.100	-0.369	0.071	-0.432
(q)	$\Gamma - \delta\Gamma$	-0.109	-0.328	0.112	-0.489
(r)	$r_{\text{BW}} = 0.0 \text{ GeV}^{-1}$	-0.154	-0.385	-0.116	-0.338
(s)	$r_{\text{BW}} = 3.0 \text{ GeV}^{-1}$	-0.308	-0.281	1.225	-0.386
(t)	Add $K^*(1410)$ and $\rho(1450)$	-0.124	-0.286	0.023	-0.701

Table 2: Summary of the model related systematic uncertainties for each alternative model.

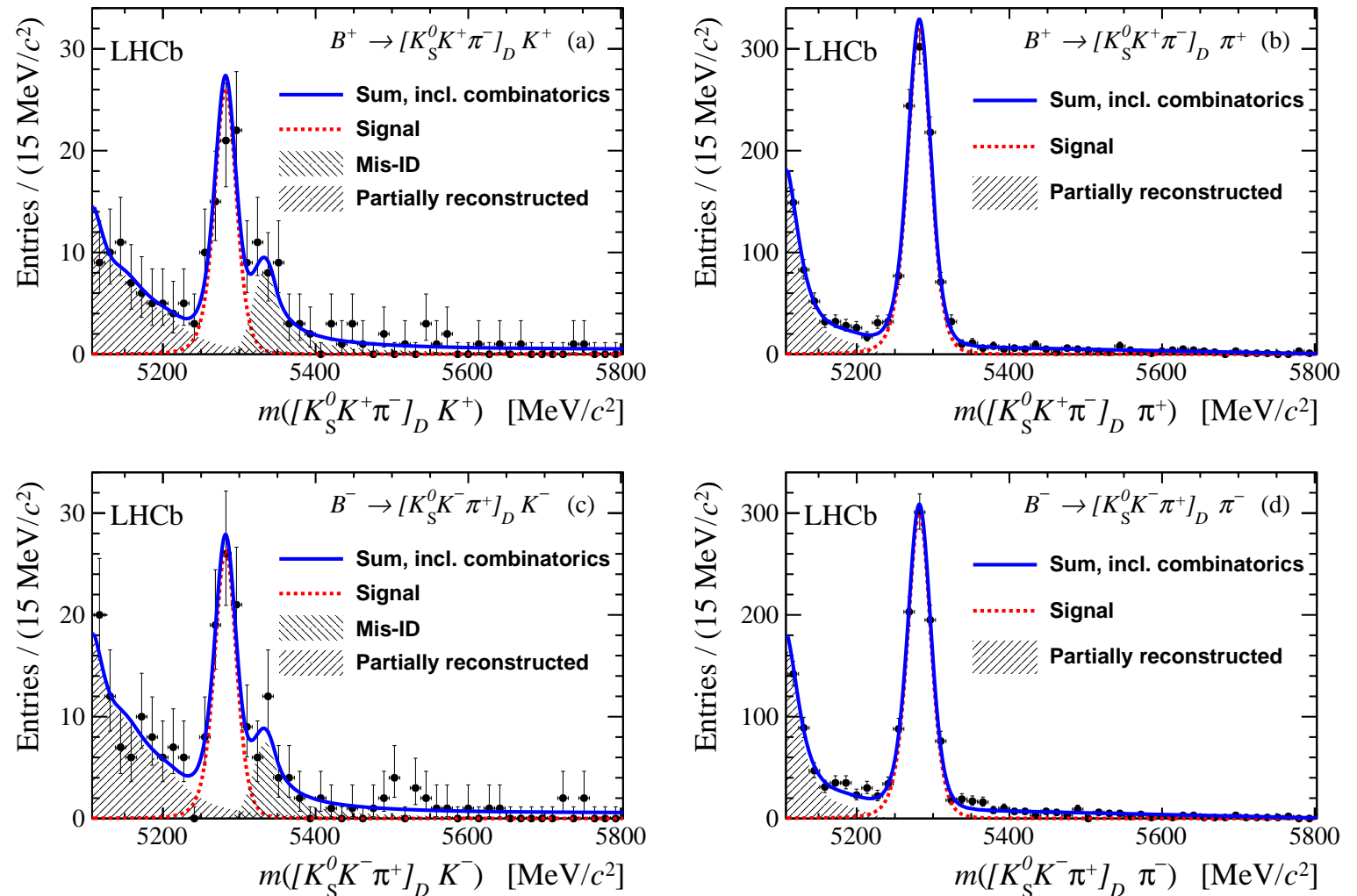
$$B^\pm \rightarrow D[K_S^0 \pi^+ \pi^-] K^\pm$$

Source of uncertainty	$\delta x_- (\times 10^{-3})$	$\delta y_- (\times 10^{-3})$	$\delta x_+ (\times 10^{-3})$	$\delta y_+ (\times 10^{-3})$
Combinatoric $D$ yield estimate	1.0	4.3	2.7	4.9
Inclusion of semileptonic background	3.1	2.8	0.63	3.2
Charged kaon detection asymmetry	0.022	0.030	0.0041	0.025
Amplitudes for backgrounds				
Combinatoric $D$	3.5	3.4	4.7	6.4
Random $Dh$	0.10	0.16	0.066	0.16
$B_s$ partially-reconstructed	0.59	0.59	0.15	0.73
$r_{B^\pm \rightarrow D\pi^\pm}$	1.8	1.9	1.6	1.1
Efficiency over the phase space	5.7	0.35	6.9	0.31
$CP$ fit bias	5.7	5.1	-1.3	2.6
Total experiment or fit related	+9.6 -7.7	+8.2 -6.4	+9.0 -9.1	+9.2 -8.8
Total model related	0.9	2.5	3.3	7.4

Table 3: Summary of absolute values of systematic uncertainties.

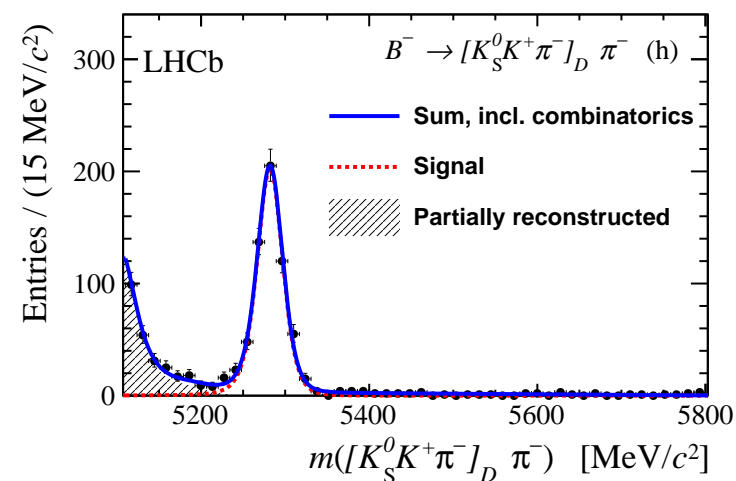
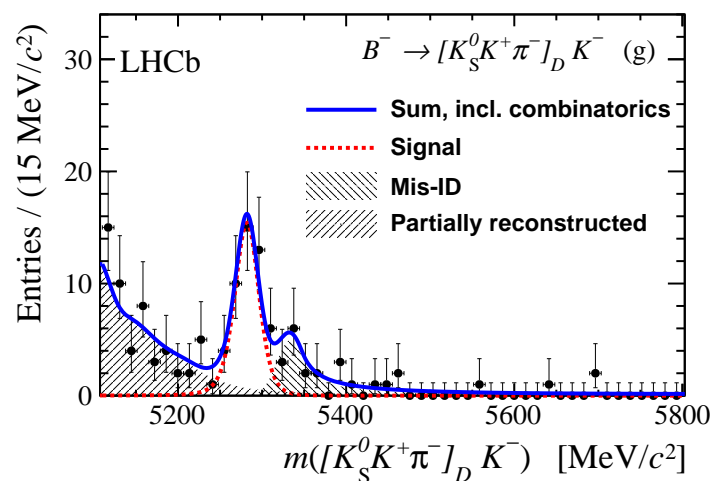
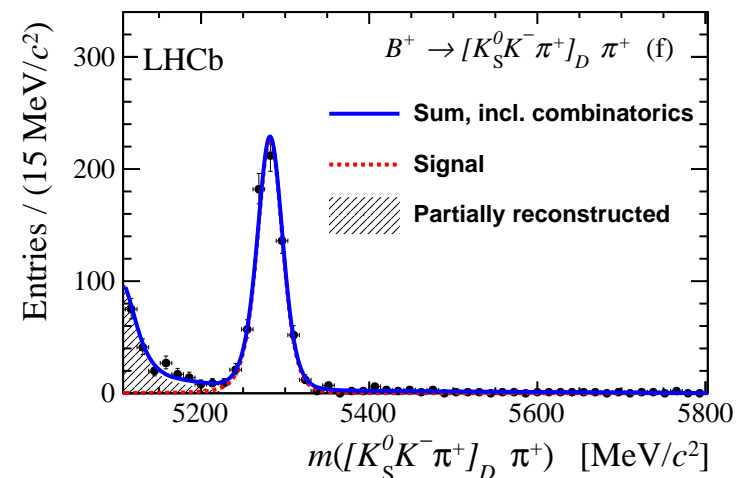
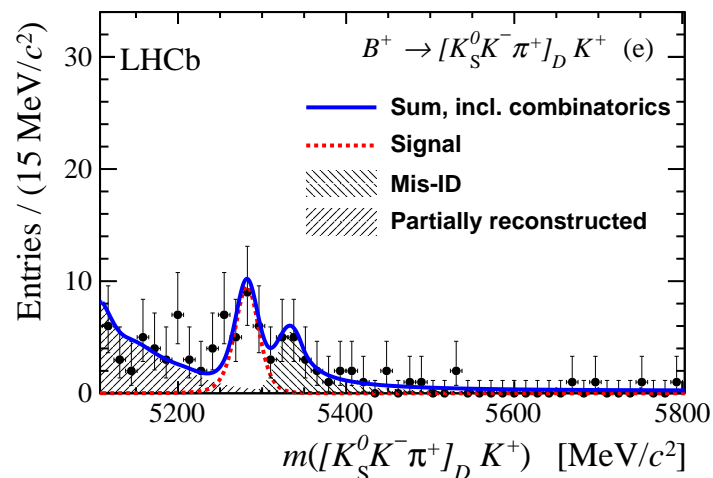
$$B^\pm \rightarrow D[K_S^0 K^\pm \pi^\pm] K^\pm$$

SS candidates



$$B^\pm \rightarrow D[K_S^0 K^\pm \pi^\pm] K^\pm$$

OS candidates



$$B^\pm \rightarrow D[K_S^0 K^\pm \pi^\pm] K^\pm$$

Table 1: Signal yields and their statistical uncertainties derived from the fit to the whole Dalitz plot region, and in the restricted region of phase space around the  $K^*(892)^\pm$  resonance.

Mode	Whole Dalitz plot		$K^*(892)^\pm$ region	
	$DK^\pm$	$D\pi^\pm$	$DK^\pm$	$D\pi^\pm$
SS	$145 \pm 15$	$1841 \pm 47$	$97 \pm 12$	$1365 \pm 38$
OS	$71 \pm 10$	$1267 \pm 37$	$26 \pm 6$	$553 \pm 24$

Table 2: Results for the observables measured in the whole Dalitz plot region, and in the restricted region of phase space around the  $K^*(892)^\pm$  resonance. The first uncertainty is statistical and the second is systematic. The corrections for production and detection asymmetries are applied, as is the efficiency correction defined in Eq. (5).

Observable	Whole Dalitz plot	$K^*(892)^\pm$ region
$\mathcal{R}_{SS/OS}$	$1.528 \pm 0.058 \pm 0.025$	$2.57 \pm 0.13 \pm 0.06$
$\mathcal{R}_{DK/D\pi, SS}$	$0.092 \pm 0.009 \pm 0.004$	$0.084 \pm 0.011 \pm 0.003$
$\mathcal{R}_{DK/D\pi, OS}$	$0.066 \pm 0.009 \pm 0.002$	$0.056 \pm 0.013 \pm 0.002$
$\mathcal{A}_{SS, DK}$	$0.040 \pm 0.091 \pm 0.018$	$0.026 \pm 0.109 \pm 0.029$
$\mathcal{A}_{OS, DK}$	$0.233 \pm 0.129 \pm 0.024$	$0.336 \pm 0.208 \pm 0.026$
$\mathcal{A}_{SS, D\pi}$	$-0.025 \pm 0.024 \pm 0.010$	$-0.012 \pm 0.028 \pm 0.010$
$\mathcal{A}_{OS, D\pi}$	$-0.052 \pm 0.029 \pm 0.017$	$-0.054 \pm 0.043 \pm 0.017$

$$B^{\pm} \rightarrow D[K_S^0 K^{\pm} \pi^{\pm}] K^{\pm}$$

Table 3: Absolute values of systematic uncertainties, in units of  $10^{-2}$ , for the fit to the whole Dalitz plot.

Observable	Eff. correction	Fit PDFs	Prod. and det. asymms.	PID	Total
$\mathcal{R}_{SS/OS}$	2.40	0.50	—	0.01	2.45
$\mathcal{R}_{DK/D\pi, SS}$	0.01	0.38	—	0.02	0.38
$\mathcal{R}_{DK/D\pi, OS}$	0.01	0.19	—	0.01	0.19
$\mathcal{A}_{SS, DK}$	0.14	0.44	1.71	0.01	1.78
$\mathcal{A}_{OS, DK}$	0.36	2.13	0.99	0.01	2.37
$\mathcal{A}_{SS, D\pi}$	0.02	0.05	0.99	< 0.01	0.99
$\mathcal{A}_{OS, D\pi}$	0.03	0.10	1.71	< 0.01	1.72

Table 4: Absolute values of systematic uncertainties, in units of  $10^{-2}$ , for the fit in the restricted region.

Observable	Eff. correction	Fit PDFs	Prod. and det. asymms.	PID	Total
$\mathcal{R}_{SS/OS}$	6.08	0.53	—	0.01	6.10
$\mathcal{R}_{DK/D\pi, SS}$	0.01	0.25	—	0.02	0.25
$\mathcal{R}_{DK/D\pi, OS}$	0.01	0.21	—	0.01	0.21
$\mathcal{A}_{SS, DK}$	0.13	2.27	1.71	0.01	2.85
$\mathcal{A}_{OS, DK}$	0.04	2.38	0.99	0.01	2.57
$\mathcal{A}_{SS, D\pi}$	0.04	0.17	0.99	< 0.01	1.00
$\mathcal{A}_{OS, D\pi}$	0.06	0.09	1.71	< 0.01	1.72

$$B_c^+ \rightarrow J/\psi 3\pi^+ 2\pi^-$$

Table 2: Relative systematic uncertainties for the ratio  $R_{5\pi}$ . The total uncertainty is the quadratic sum of the individual components.

Source	Uncertainty [%]
Fit model	6.6
Decay model	
$m_{3\pi^+2\pi^-}$ reweighting	7.7
$\psi(2S)$ mass veto	3.1
Data-simulation agreement	
Hadron interactions	$4 \times 2.0$
Track quality selection	$4 \times 0.6$
Trigger	1.1
Pion identification	0.7
Selection variables	1.0
$B_c^+$ lifetime	0.9
Stability for various data taking conditions	2.5
Acceptance	0.8
Total	13.9

$$\Lambda_b^0 \rightarrow \Lambda_c^+ [\bar{K}^0 p] \pi^-$$

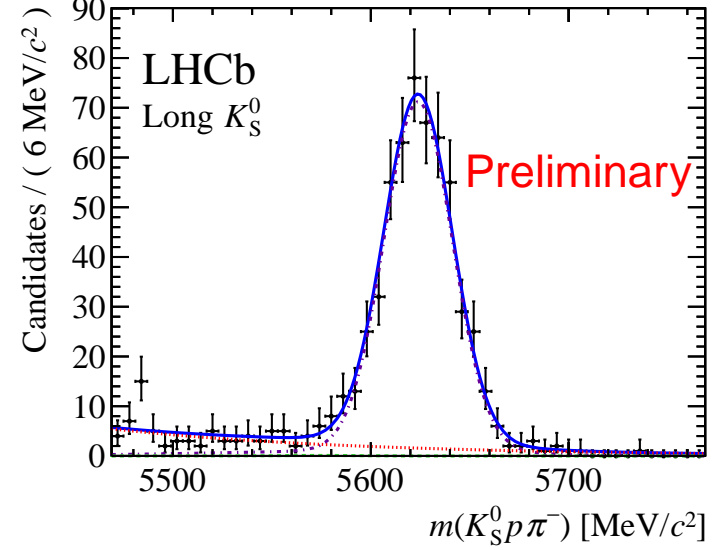
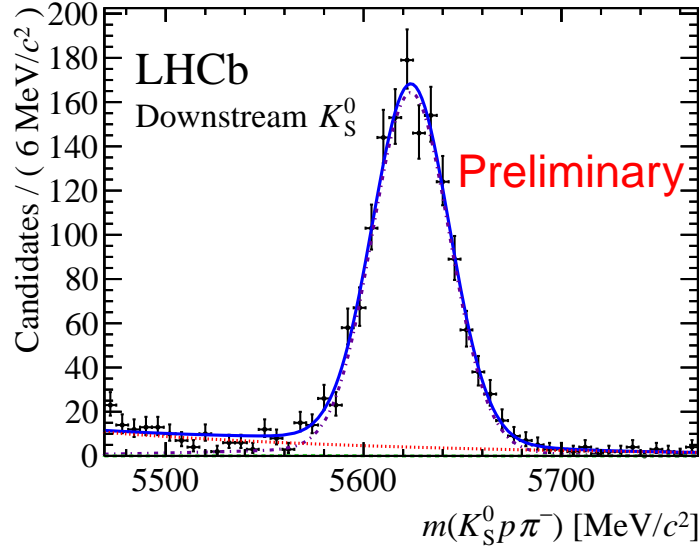


Table 1: Fitted yields and efficiency for each channel, separated by  $K_S^0$  type. Yields are given with both statistical and systematic uncertainties, whereas for the efficiencies only the uncertainties due to the limited Monte Carlo sample sizes are given. The three rows for the  $B^0 \rightarrow K_S^0 \pi^+ \pi^-$  decay correspond to the different BDT selections for charmless signal modes and the channels containing  $\Lambda_c^+$  or  $D_s^-$  hadrons.

Mode	Downstream		Long	
	Yield	Efficiency ( $\times 10^{-4}$ )	Yield	Efficiency ( $\times 10^{-4}$ )
$\Lambda_b^0 \rightarrow K_S^0 p \pi^-$	$106.1 \pm 21.5 \pm 3.7$	$5.40 \pm 0.12$	$90.9 \pm 14.6 \pm 1.0$	$2.26 \pm 0.06$
$\Lambda_b^0 \rightarrow K_S^0 p K^-$	$11.5 \pm 10.7 \pm 1.2$	$5.34 \pm 0.11$	$19.6 \pm 8.5 \pm 0.8$	$2.87 \pm 0.07$
$\Xi_b^0 \rightarrow K_S^0 p \pi^-$	$5.3 \pm 15.7 \pm 0.7$	$5.35 \pm 0.10$	$6.4 \pm 8.5 \pm 0.5$	$2.67 \pm 0.07$
$\Xi_b^0 \rightarrow K_S^0 p K^-$	$10.5 \pm 8.8 \pm 0.5$	$6.12 \pm 0.10$	$6.3 \pm 5.6 \pm 0.4$	$2.91 \pm 0.07$
$\Lambda_b^0 \rightarrow \Lambda_c^+ (\rightarrow p K_S^0) \pi^-$	$1391.6 \pm 39.6 \pm 24.8$	$4.85 \pm 0.09$	$536.8 \pm 24.6 \pm 3.5$	$1.71 \pm 0.05$
$\Lambda_b^0 \rightarrow \Lambda_c^+ (\rightarrow p K_S^0) K^-$	$70.0 \pm 10.3 \pm 3.3$	$4.69 \pm 0.07$	$37.4 \pm 7.1 \pm 2.7$	$1.66 \pm 0.03$
$\Lambda_b^0 \rightarrow D_s^- p$	$6.3 \pm 5.1 \pm 0.6$	$2.69 \pm 0.05$	$6.5 \pm 3.7 \pm 0.2$	$0.89 \pm 0.03$
$B^0 \rightarrow K_S^0 \pi^+ \pi^- (K_S^0 p h)$	$913.5 \pm 45.0 \pm 12.2$	$5.57 \pm 0.09$	$495.7 \pm 31.8 \pm 7.5$	$2.86 \pm 0.06$
$B^0 \rightarrow K_S^0 \pi^+ \pi^- (\Lambda_c^+ h)$	$1163.8 \pm 60.7 \pm 18.8$	$7.38 \pm 0.11$	$589.0 \pm 33.3 \pm 17.3$	$3.27 \pm 0.06$
$B^0 \rightarrow K_S^0 \pi^+ \pi^- (D_s^- p)$	$1317.8 \pm 77.1 \pm 25.7$	$7.76 \pm 0.11$	$614.1 \pm 38.3 \pm 14.8$	$3.47 \pm 0.07$



$$\Lambda_b^0 \longrightarrow \bar{K}^0 p \pi^-$$

Control sample  $B^0 \rightarrow K^0 \pi^+ \pi^-$  with selection criteria of  $\Lambda_b^0 \rightarrow \bar{K}^0 p \pi^-$

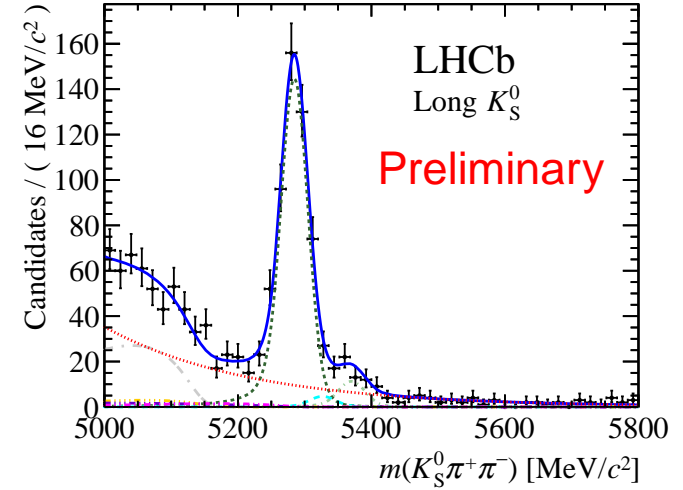
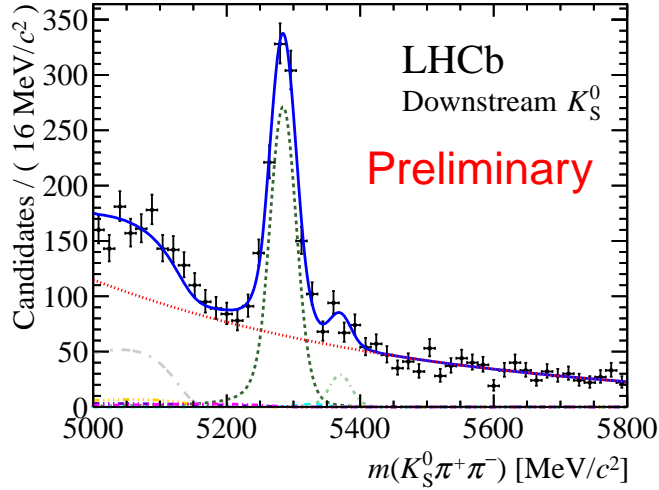


Table 2: Relative systematic uncertainties on the branching fraction ratios (%) with respect to  $B^0 \rightarrow K_S^0 \pi^+ \pi^-$  decays. The total is obtained from the sum in quadrature of all contributions except that from knowledge of the fragmentation fractions.

	Simulation	$\Delta_{\text{PHSP}}$	PID	Fit model	Fit bias	Veto	Total	$f_{\Lambda_b^0}/f_d$
Downstream								
$\mathcal{B}(\Lambda_b^0 \rightarrow K_S^0 p \pi^-)$	6	4	6	1	<1	3	10	27
$\mathcal{B}(\Lambda_b^0 \rightarrow K_S^0 p K^-)$	6	58	2	8	4	4	59	27
$\mathcal{B}(\Xi_b^0 \rightarrow K_S^0 p \pi^-)$	4	64	6	12	7	-	66	-
$\mathcal{B}(\Xi_b^0 \rightarrow K_S^0 p K^-)$	4	47	2	4	3	-	47	-
$\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda_c^+ (\rightarrow p K_S^0) \pi^-)$	5	-	6	2	<1	<1	8	27
$\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda_c^+ (\rightarrow p K_S^0) K^-)$	5	-	4	5	<1	1	8	27
$\mathcal{B}(\Lambda_b^0 \rightarrow D_s^- (\rightarrow K_S^0 K^-) p)$	6	-	6	7	6	-	12	27
Long								
$\mathcal{B}(\Lambda_b^0 \rightarrow K_S^0 p \pi^-)$	6	3	4	2	1	<1	8	27
$\mathcal{B}(\Lambda_b^0 \rightarrow K_S^0 p K^-)$	6	42	4	4	1	1	43	27
$\mathcal{B}(\Xi_b^0 \rightarrow K_S^0 p \pi^-)$	5	47	5	8	2	-	49	-
$\mathcal{B}(\Xi_b^0 \rightarrow K_S^0 p K^-)$	5	37	5	6	4	-	39	-
$\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda_c^+ (\rightarrow p K_S^0) \pi^-)$	6	-	4	3	<1	<1	8	27
$\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda_c^+ (\rightarrow p K_S^0) K^-)$	5	-	6	8	1	<1	11	27
$\mathcal{B}(\Lambda_b^0 \rightarrow D_s^- (\rightarrow K_S^0 K^-) p)$	6	-	8	4	2	-	11	27